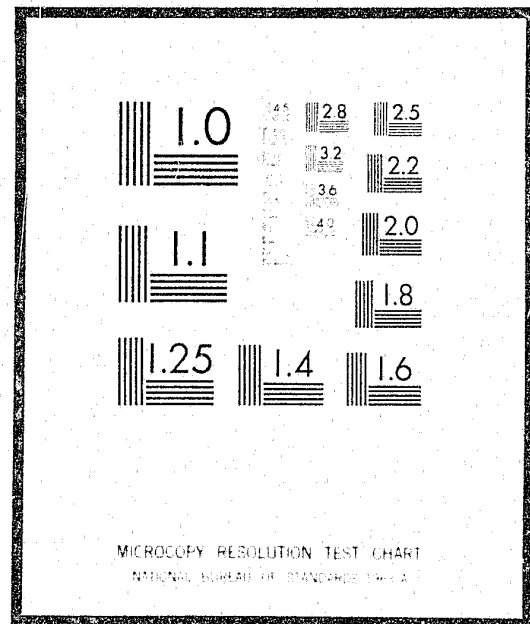


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Vol. 2

## AUTOMATIC VEHICLE MONITORING SYSTEMS STUDY Report of Phase 0

### Vol. 2. Problem Definition and Derivation of AVM System Selection Techniques

Prepared by

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Prepared for

National Science Foundation  
Washington, D.C.

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## PREFACE

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## FOREWORD

This report was prepared for distribution to public safety planners for the purpose of providing them with a compact source of information regarding improvements in efficiency and cost benefits obtainable with various classes of operational and proposed automatic vehicle monitoring (AVM) systems. An AVM system can contribute to emergency patrol effectiveness by reducing response times and by enhancing officer safety as well as by providing essential administrative control and public relations information. This complete report and the Executive Summary (Vol. 1) were prepared by the Jet Propulsion Laboratory of the California Institute of Technology using the results of studies sponsored by the National Science Foundation.

Special computer programs are described which can simulate and synthesize AVM systems tailored to the needs of small, medium and large urban areas. These analyses can be applied by state and local law enforcement agencies and by emergency vehicle operators to help decide on what degree and type of automation will best suit their individual performance requirements and also the possible reduction in the number of vehicles needed which could substantially reduce operating expenses.

G. R. Hansen

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ADMINISTRATIVE SERVICES

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## ABSTRACT

A set of planning guidelines is presented to help law enforcement agencies and vehicle fleet operators decide which automatic vehicle monitoring (AVM) system could best meet their performance requirements. Improvements in emergency response times and resultant cost benefits obtainable with various operational and planned AVM systems may be synthesized and simulated by means of special computer programs for model city parameters applicable to small, medium and large urban areas. Design characteristics of various AVM systems and the implementation requirements are illustrated and costed for the vehicles, the fixed sites and the base equipments. Vehicle location accuracies for different RF links and polling intervals are analyzed. Actual applications and coverage data are tabulated for seven cities whose police departments actively cooperated in the JPL study. Volume 1 of this Report is the Executive Summary. Volume 2 contains the results of systems analyses.

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# AUTOMATIC VEHICLE MONITORING SYSTEMS STUDY

## EXECUTIVE SUMMARY

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AUTOMATIC VEHICLE MONITORING SYSTEMS

George R. Hansen

I. INTRODUCTION

In this report, the results of the first phase of a three-phase program to aggregate existing information on Automatic Vehicle Monitoring (AVM) Systems are presented in terms of performance, urban characteristics, operating modes, and cost in a way that will assist prospective AVM User Agencies to make valid comparisons and selections from among the many competing AVM techniques and AVM Systems. This phase (Phase 0) of the study was performed by the Jet Propulsion Laboratory (JPL) for the National Science Foundation (NSF). As originally conceived by NSF and JPL, the AVM Systems study program would include the following three phases:

- Phase 0 Problem Definition and Derivation of AVM System Selection Techniques (in this Report).
- Phase I Critical Research and Verification of the Efficacy of AVM System Selection Techniques Through Computerized System Simulation.
- Phase II Proof of Concept Experiment Demonstrating the Efficacy of Selected AVM Systems in Urban Environments.

In brief, the Phase 0 research was concentrated in three areas: (1) Compilation of a broad information base on AVM technology and urban characteristics, (2) adaptation of computerized analytical techniques needed in the AVM System selection process and in cost benefit trade-offs, and (3) application of AVM System selection process by manual iteration to small, medium and large model cities.

Frequent reference is made in this Report to "AVM techniques" and "AVM Systems". The term "AVM technique" is used to denote the technology required to acquire a fix on a vehicle, while "AVM System" is used to denote the integration of all functional elements required to locate and keep track of vehicles in some automated fashion.

## II. SUMMARY OF AVM SYSTEMS STUDY RESULTS

### A. WORK ACCOMPLISHED IN PHASE 0

A broad range of information concerning automatic vehicle monitoring (AVM) was compiled from the existing literature, including: (1) Various vehicle location sensing techniques, (2) all functional elements of the total AVM system, and (3) various sized cities with representative geography, topology, demography and urbanology. The information obtained from the literature was supplemented by data obtained directly from police department representatives of seven Southern California cities that participated in the User Group Advisory Committee (UGAC).

Several computerized analytical techniques were developed. City models representative of those characteristics that affect AVM selection were developed for use in the general cost benefit solutions. An analytical technique for predicting vehicle polling rates achievable for the various location sensing techniques in a full AVM system configuration was also developed. Algorithms were developed to estimate the accuracies achievable by a large variety of AVM systems using the probabilistic distributions for three independent variables: (1) vehicle speed, (2) inherent accuracies of location sensing techniques, and (3) vehicle polling intervals.

Preliminary analyses were performed to determine first-order cost estimates for AVM Systems as a function of the various vehicle location sensing techniques when used in small, medium and large cities. Preliminary analyses of the accuracies achievable with various AVM systems were also performed. Various AVM system configuration options were developed, and promising options were examined for possible cost benefits to seven UGAC cities.

### B. PRELIMINARY CONCLUSIONS

1. AVM Class should indicate effects on urban environment. From the viewpoint of the prospective AVM system user, the traditional classifications of vehicle locating systems (i.e., piloting, deadreckoning, triangulation, trilateration, and proximity) do not necessarily reflect the impact of an AVM installation on the local urban scene. It is believed that the prospective user's needs would be better met if vehicle monitoring classifications were based on system element types and functions as follows:

Class 0	Manual Monitoring. No AVM
Class I	AVM. No modification to the urban environment. (existing RF links)
Class II	AVM. Autonomous signposts throughout urban area
Class III	AVM. Sparsely distributed special RF sites
Class IV	AVM. Monitored signposts throughout urban area

2. AVM cost benefits obtainable by medium and large cities. The preliminary cost analysis indicates that the cost benefit break-even point occurs for a medium sized city with an area of about  $100 \text{ km}^2$  ( $40 \text{ mi}^2$ ) and with roughly 50 vehicles. In other words, cities larger in size could expect a positive and increasing benefit with size, up to a certain point. Conversely, cities below this medium size probably would not realize any cost benefit. This conclusion was based on 5-year estimates of AVM system costs and savings.

3. No cost benefits derived from monitored signpost systems. None of the Class IV systems produced a cost benefit for the cities studied, generally because the rental rates on telephone lines raise the equipment costs excessively.

4. AVM System accuracies greater than technique accuracies. In general, the 95% total system accuracy can be expected to be significantly greater than the inherent accuracy of the location sensing technique. Usually the system accuracy is no less than three times the inherent technique accuracy.

5. Vehicle polling intervals determine AVM system accuracies. It appears that the polling interval will dominate system accuracy and that the polling interval can only be shortened at the expense of RF resources dedicated to AVM purposes. Because of the present and predicted future demand on RF resources, this is one area that demands optimization.

6. Critical research required for verification of selection technique. The results of the first phase of the AVM study effort should be used with caution and should not be construed as specific recommendations at this point. The second phase of the analytical work should be completed to verify the results of the first phase.

### C. PROGRAM RECOMMENDATIONS

1. It is recommended that the second phase (Phase I) of the AVM Systems study proceed.

2. It is further recommended that mission agencies such as the Law Enforcement Assistance Administration (LEAA) and/or the Department of Transportation (DOT) sponsor the Proof of Concept Experiment, or third phase. The tests presently planned jointly by the city of Los Angeles and DOT could effectively serve this purpose. This could be accomplished by closely coordinating the analytical techniques developed in this study with the Los Angeles Police Department, the Southern California Rapid Transit District, LEAA and DOT and making the analytical tools available to the city for use in the design of the experiment.

## III. CLASSES OF AVM SYSTEMS

### A. CLASSIFICATION RATIONALE

Traditionally, AVM systems have been classified in the literature according to the method used to locate the vehicle within an urban area. Recognizing that all AVM systems have certain elements in common and that some systems have unique elements, an alternate classification scheme was developed for the purpose of this study. This classification not only implies the type of AVM system but also suggests the physical impact that the system elements and functions will have on the local urban environment. The following groupings of system elements suggested the classification scheme:

#### Functional Elements Common to All AVM Systems

- (1) Existing communications system.
- (2) Vehicle polling subsystem.
- (3) Landline data links.
- (4) Telemetry data/polling handler.
- (5) Telemetry link (common to most).
- (6) In-vehicle equipment, such as data processor, telemetry data encoder, polling processor, and signpost sensor.
- (7) Vehicle location computer.
- (8) Information display subsystem.

#### Functional Elements Unique to Specific AVM Systems

- (9) Autonomous signposts; signpost sensor in vehicle (Class II).
- (10) Fixed synchronized RF transmitter sites (Class III).
- (11) Monitored signposts; vehicle sensor on signpost (Class IV).

A discussion of each of these AVM functional elements follows:

1. Existing communications system. As a practical consideration, AVM systems will probably be integrated with the existing voice communication and vehicle polling RF links, especially for the telemetered location data between the vehicle and the dispatch center.

2. Vehicle polling subsystem. This interrogation device or procedure enables the vehicle location computer (VLC), described in Element 7, to know which vehicle corresponds to which set of location data. Polling may be either an operating procedure or an active element that allows the dispatcher to obtain locations of specific vehicles.

3. Landline data link. This data link is a landline supplying data to the VLC (Element 7). It may either be relatively short, leading from the telemetry data/polling handler (Element 4) to the VLC, or it may be quite extensive, collecting data from monitored signposts throughout the covered urban area, or it may be somewhere in between these in its extent, bringing data from a relatively small number of fixed RF sites.

4. Telemetry data/polling handler. This device is included because AVM systems deal with data that are different (e. g., digital) in character from that used by the dispatcher in voice communication with the vehicles. Furthermore, if the vehicle polling subsystem (Element 2) provides for selective polling, then there are likely to be corresponding additional requirements on the communication system.

5. Telemetry link. Since it is tacitly assumed that the AVM system will not restrict the mobility of the fleet vehicles, some kind of communication-at-a-distance is essential. In some systems, the telemetry link is assumed to share or be in addition to the RF link now used for voice communications. In other systems the telemetry path might be between the vehicles and sparsely distributed synchronized RF sites. In still other AVM systems, the telemetry path may be relatively short, being only from the vehicles to signposts distributed throughout the urban area. In that case, the transmission medium could conceivably be sonic, optical, or even magnetic, instead of radio.

6. In-vehicle equipment. Depending on the AVM system, some or all of the four following devices may be carried in the vehicle:

a. Vehicle data processor. This device receives raw vehicle location data either from the officer or from signpost sensors. It does whatever data processing is done on-board, then adds the vehicle identification data, and passes this information along to the telemetry data encoder, described next.

b. Vehicle telemetry data encoder. This device puts the vehicle location data supplied by the vehicle data processor into the telemetry link (Element 5).

c. Vehicle polling processor. This device enables the vehicle to respond properly when polled, and may range in complexity from a clock to an RF signal decoder.

d. Signpost sensor. Where the densely distributed autonomous signpost concept is used (Class II), the signpost sensor must be carried in the vehicle. This sensor is required to read the signpost ID/location. Location data may be acquired by coded optical, infrared, sonic, or magnetic means besides radio.

7. Vehicle location computer (VLC). This device transforms the vehicle location data into location points or coordinates for use by the information display subsystem (Element 8). It also informs the display subsystem as to the identity of the vehicle to which the location data belongs. The VLC may also interface with the Computer-Aided Dispatch System.

8. Information display subsystem. This device indicates to the dispatcher where the vehicles are currently located (or were when last polled). It may also identify the vehicle's status. As in the case of manual aids used for vehicle location in Class 0, the possible range of complexity and sophistication may range from a simple printer to an elaborate electro-optical device supported by a computer. It should be noted that the display subsystem is virtually independent of the location technique used.



9. Autonomous signposts used in Class II AVM. Each autonomous wayside or buried signpost has a location ID and must be recognizable and readable by the signpost sensor in the vehicle. The signpost telemetry link to the vehicle may be by radio, pulsed light, infrared, sonic, or magnetic means.

10. Fixed synchronized RF transmitter sites used in Class III AVM. These RF sites are a relatively small number of special-purpose transmitters which broadcast synchronized signals that can be used to determine the locations of receivers on vehicles by means of navigation techniques. The characteristics of these signals could be FM phase, pulse, or noise correlation. Some of these sites may also receive retransmitted signals from the monitored vehicles.

11. Monitored signposts used in Class IV AVM. Each monitored wayside or buried signpost requires a vehicle sensor that will transmit the vehicle's ID data received and also identify its own location to the central collection station. These signposts may sense vehicle motion, or they may detect pulsed light, infrared, or ultrasonic signals or receive RF signals through buried antennas.

## B. AVM CLASS DESCRIPTIONS

The vehicle location system classes, based on their physical impact on the urban environment, are shown in the following list and are described in greater detail in subsequent paragraphs and accompanying figures. For reference, the traditional vehicle location classifications are noted as indentures.

- (1) Class 0 Manual Monitoring. No AVM
  - (a) Piloting
- (2) Class I AVM. No Modification to Urban Environment (Existing RF Links)
  - (a) Officer Update
  - (b) Dead Reckoning
  - (c) Navigation (Using Existing RF Beacons)
- (3) Class II AVM. Autonomous Signposts Throughout Urban Area

- (4) Class III AVM. Sparsely Distributed Special RF Sites
  - (a) Triangulation
  - (b) Trilateration
- (5) Class IV AVM. Monitored Signposts Throughout Urban Area
  - (a) Vehicle Proximity

1. Class 0 Manual Monitoring; No AVM. This baseline (piloting) class is included in the listing of vehicle location techniques purely for comparative purposes. In Class 0, the location monitoring methods (Figure 1) range from those relying solely on the dispatcher's memory, through manually updated mechanical and visual aids, to keyboard-updated computer displays which keep current each vehicle's location and status based on verbal or digital communications between dispatcher and vehicle.

2. Class I AVM with no modifications to urban environment. All AVM systems require the installation of certain equipment in the command center to accomplish the automation of vehicle monitoring. All AVM systems also require the installation of some device in or on the monitored vehicles. But systems in Class I require nothing further, though they perform utilize RF resources.

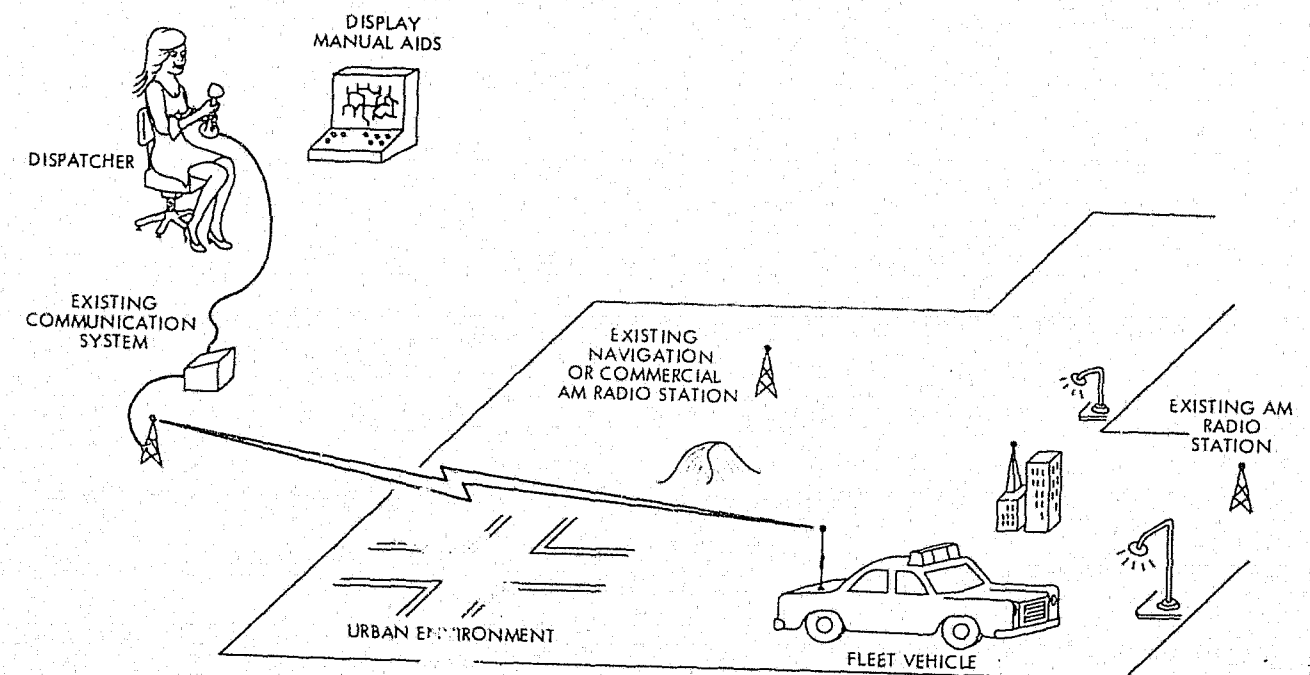


Figure 1. Class 0 Manual Monitoring, No AVM

A typical Class I AVM configuration is shown in Figure 2. Each AVM command center must contain a display subsystem, a vehicle location computer, a vehicle polling subsystem, and a telemetry data/polling handler, which are described in Section IV. Each vehicle requires location sensors, a data processor, a telemetry data encoder, and a polling processor. Class I AVM systems are based upon a variety of location techniques and algorithms which include the following: (a) Officer update techniques, in which the functions of the vehicle's sensors and its data processor are performed by an occupant of the vehicle. (b) Deadreckoning systems are included if the requisite updating does not require the installation of fixed location reference equipment in the environment. (c) If the AVM systems use existing navigation beacons or AM broadcasting stations, they are also included in Class I because the required stations are assumed to be part of the urban environment.

3. Class II AVM with autonomous signposts throughout urban areas.

The defining characteristic of Class II AVM systems is the installation of autonomous signposts in strategic wayside or buried locations at intersections throughout the covered urban area. These location reference sites are autonomous in that they communicate their identity only to the vehicles and not to the command center.

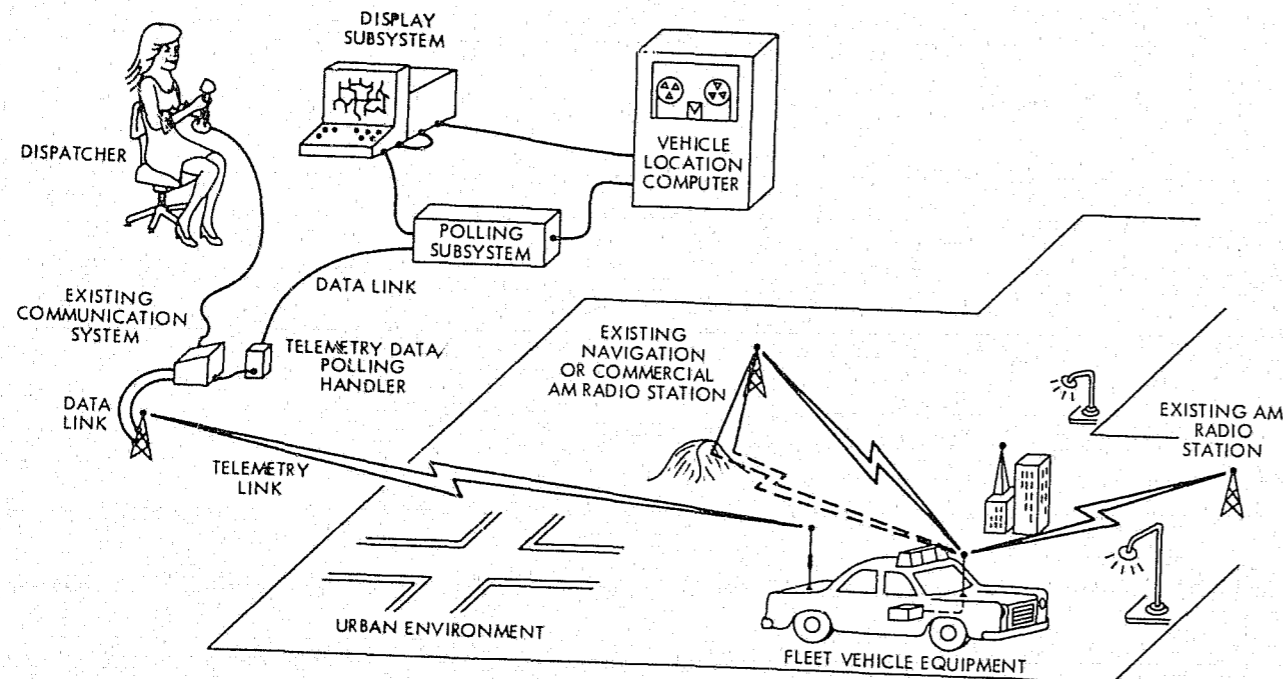


Figure 2. Class I AVM; No Modifications to Urban Physical Environment

The location information provided by the signposts to the vehicle may be either an identification code or the geographic coordinates of the location. Since the vehicle location accuracy provided by systems in Class II is dependent upon signpost spacing, greater accuracy can be achieved in critical areas by locally increasing the signpost density to one per intersection or per lane. A typical Class II system configuration is shown in Figure 3. Signpost systems can be "pure", in that all location information is derived from the fact that a monitored vehicle is (or was) near a signpost; or they can be "hybridized", with the fact of signpost proximity used either to augment, calibrate, or reinitialize the determination of vehicle locations obtained by other means, such as odometers. If a hybrid system does not require a data link in the environment, it is placed in Class II. If the hybrid system requires a data link from the signposts but no special-purpose fixed RF sites, it belongs in Class IV. If it has both a data link in the field and special-purpose fixed sites, it is in Class III.

4. Class III AVM with sparsely distributed special RF sites.

This AVM class includes those systems that require the installation of a relatively small number of special purpose fixed RF sites, where a "fixed site" either broadcasts or receives over a relatively large urban area with a radius of 5 to 11 km (3 to 7 miles).

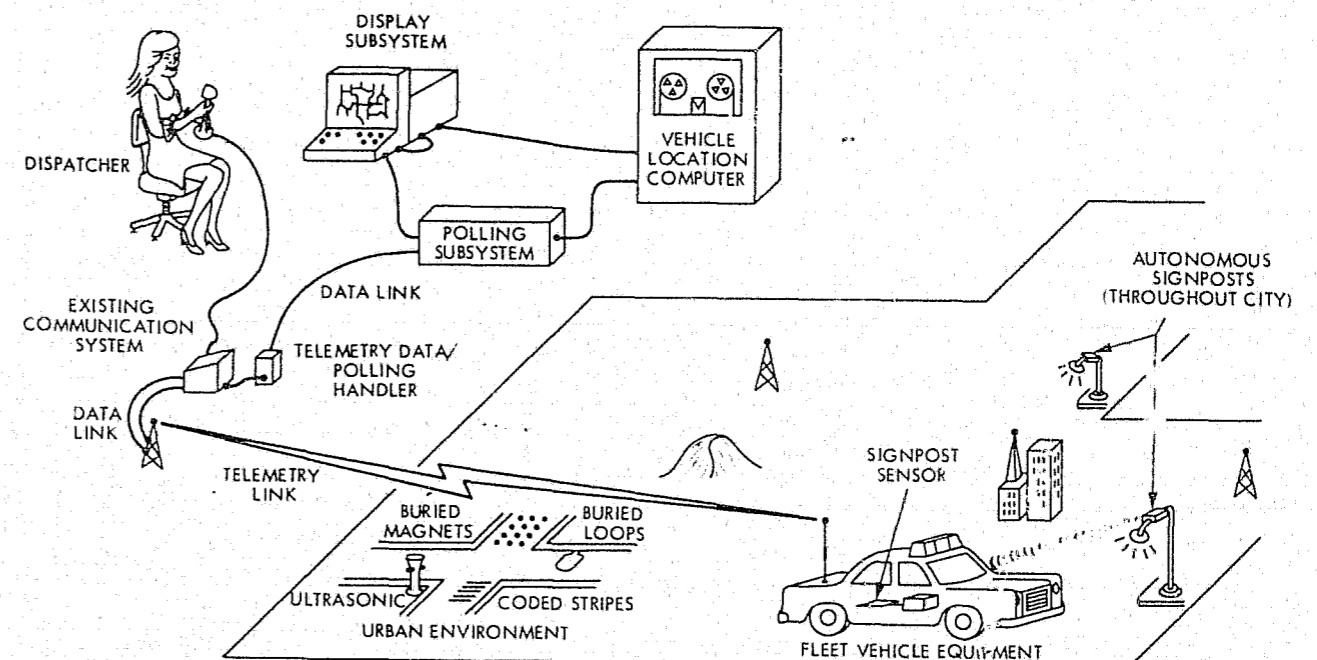


Figure 3. Class II AVM; Autonomous Signposts Throughout Urban Area

Data links in the environment are required to maintain synchronization for triangulation or trilateration purposes. Since the number of fixed sites is relatively small, these data synchronization links could be microwave rather than landline. Figure 4 shows a typical Class III configuration. It is optional only in Class III systems whether the telemetry link from the vehicle be along the existing communication system or through the special-purpose RF sites. In either case, RF resources are utilized for that link.

5. Class IV AVM with monitored signposts throughout urban area.

Systems in this class contain monitored signposts installed in strategic wayside or buried locations throughout the covered urban area for the purpose of sensing the proximity and identity of signals transmitted from vehicles. A Class IV data link does not share the use of RF resources with the existing communication system but uses telephone lines, which may make this class of AVM systems very attractive for some applications. A typical Class IV system configuration is shown in Figure 5.

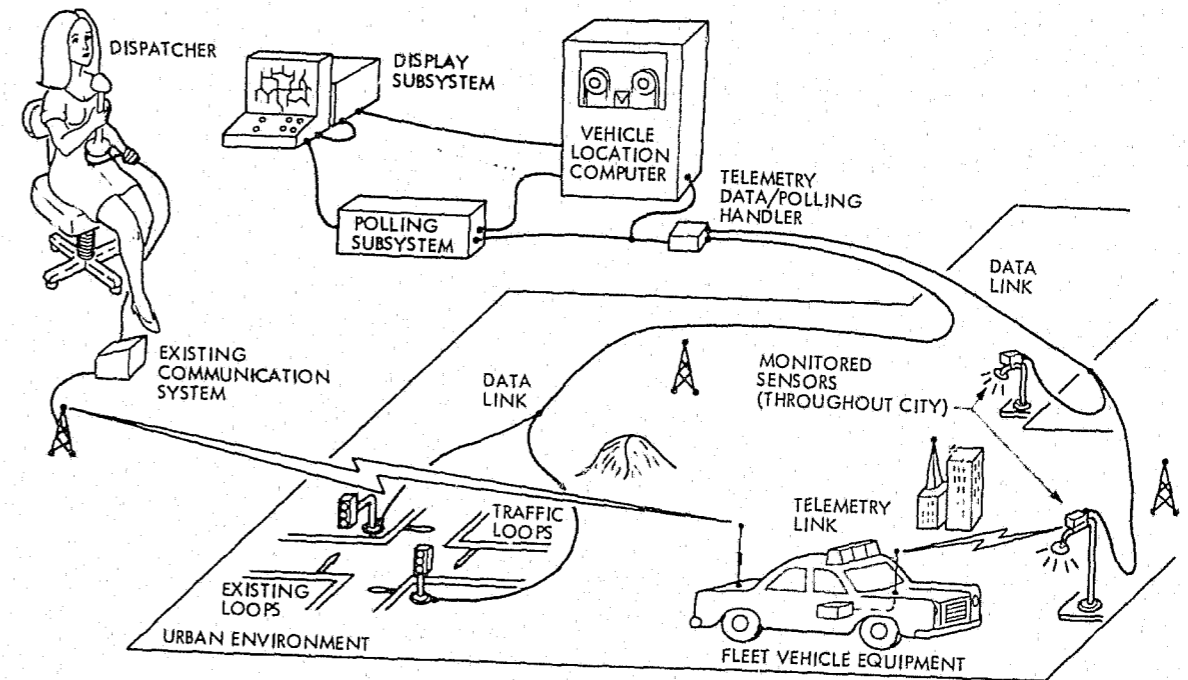


Figure 5. Class IV AVM; Monitored Signposts Throughout Urban Area

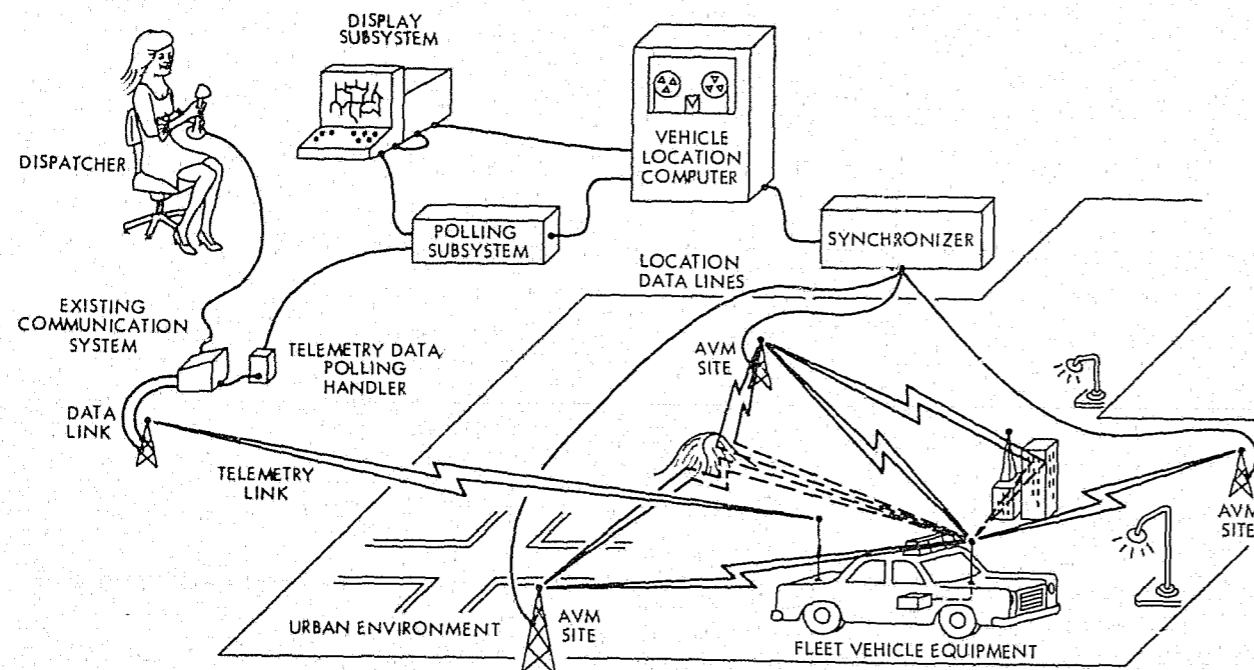


Figure 4. Class III AVM; Sparsely Distributed Special RF Sites

#### IV. VEHICLE LOCATION TECHNOLOGIES AND COSTS

##### A. PROVED AVM TECHNIQUES

This section contains a narrative description and a compilation of the cost and performance parameters of operational or proved techniques used for automatic vehicle monitoring (AVM). Schemes primarily intended for vehicle identification, such as those used in rail freight or extensions of point-of-sale methods are not included. In this report, the vehicle monitoring techniques are categorized into five broad classes, based on system element types and functions: Class 0, Manual Monitoring, no augmentation of location information; Class I AVM, no additions to the urban environment; Class II AVM, densely distributed autonomous signposts; Class III AVM, sparsely distributed special transmitting/receiving fixed RF sites; and Class IV AVM, densely distributed monitored signposts. In Table 1, the proved vehicle location methods are listed by AVM Class along with estimated costs (as of 1974) for unique system-required equipments installed in each vehicle and at each signpost or special fixed site.

1. Functional diagram correlating various AVM techniques. In order to make equipment and cost comparisons, a functional block diagram combining the elements that make up all of the AVM techniques was generated. This block diagram (Figure 6) demonstrates the equipment and functional commonality among the various techniques. In most techniques, the functional elements can also be physically identical, such as the location/vehicle ID/status register. Variations in costing such elements are due to other factors, such as achievable location precision, fleet size, and amount of status telemetry desired which all affect register length but are technique independent.

Figure 6 illustrates the numerous optional methods available for performing the vehicle location function which make AVM system comparisons difficult. For example, the various Class I techniques can either process the location data on the vehicle or transmit the raw data to the base station. In the Class III techniques, the vehicles may be polled either through the normal 2-way radio or through a special telemetry link used for vehicle location purposes.

Table 1. AVM Classes, Systems and Costs of Functional Elements Installed

AVM Class and System	Element Costs, \$		AVM Class and System	Element Costs, \$	
	Vehicle	Fixed Site		Vehicle	Fixed Site
Class 0. Manual Monitoring. No Augmentation of Vehicle Location Information			Class II. Autonomous Signposts Throughout Urban Area		
Class I. No Modifications to Urban Environment (Existing RF Links)			(1) Active signposts		
(1) Officer update systems	—	—	(a) Radio beacons	—	—
(a) Keyboard entry	120	0	Low frequency	145	165
(b) Stylus map	2535	0	Citizen band, VHF	145	145
(2) Dead reckoning systems	—	—	X-band beacon	160	275
(a) Two accelerometers	500	0	(b) Ultrasonic signposts	170	160
(b) Two velocimeters	—	—	(c) Optical, infrared	170	155
Laser, orthogonal	715	0	(d) Buried antennas	135	120
Laser/compass	805	0	(2) Passive signposts	—	—
Ultrasonic	485	0	(a) Buried Magnets	95	110
(c) Odometer/compass	—	—	(b) Reflective patterns	—	—
Magnetic compass	285	0	Coded on signposts	580	85
Gyro compass	—	0	Coded on roadway	135	125
(3) Navigation, existing beacons	—	—	(c) Buried resonant loops	135	95
(a) OMEGA systems	—	—	Class III. Sparsely Distributed Special RF Sites		
Differential	1580	0	(1) Trilateration systems	—	—
Relay OMEGA	455	0	(a) Phase TOA	—	—
(b) LORAN (A, C, or D)	—	—	Narrow-band	100	5,000
Differential	2680	0	Wide-band	2,965	11,000
Relay LORAN	505	0	(b) Pulse TOA	1,435	14,500
(c) DECCA System	1010	0	(c) Interferometer, noise	885	9,000
(d) AM Broadcast stations	365	0	(2) Triangulation systems	—	—
			(a) Rotating beams (HONORE)	—	—
			(b) Direction finding	50	27,500
			Class IV. Monitored Signposts Throughout Urban Area		
			(1) Radio receivers	—	—
			(a) Wayside	135	260
			(b) Buried antennas	145	265
			(2) Ultrasonic receptors	185	280
			(3) Optical, infrared detectors	185	270

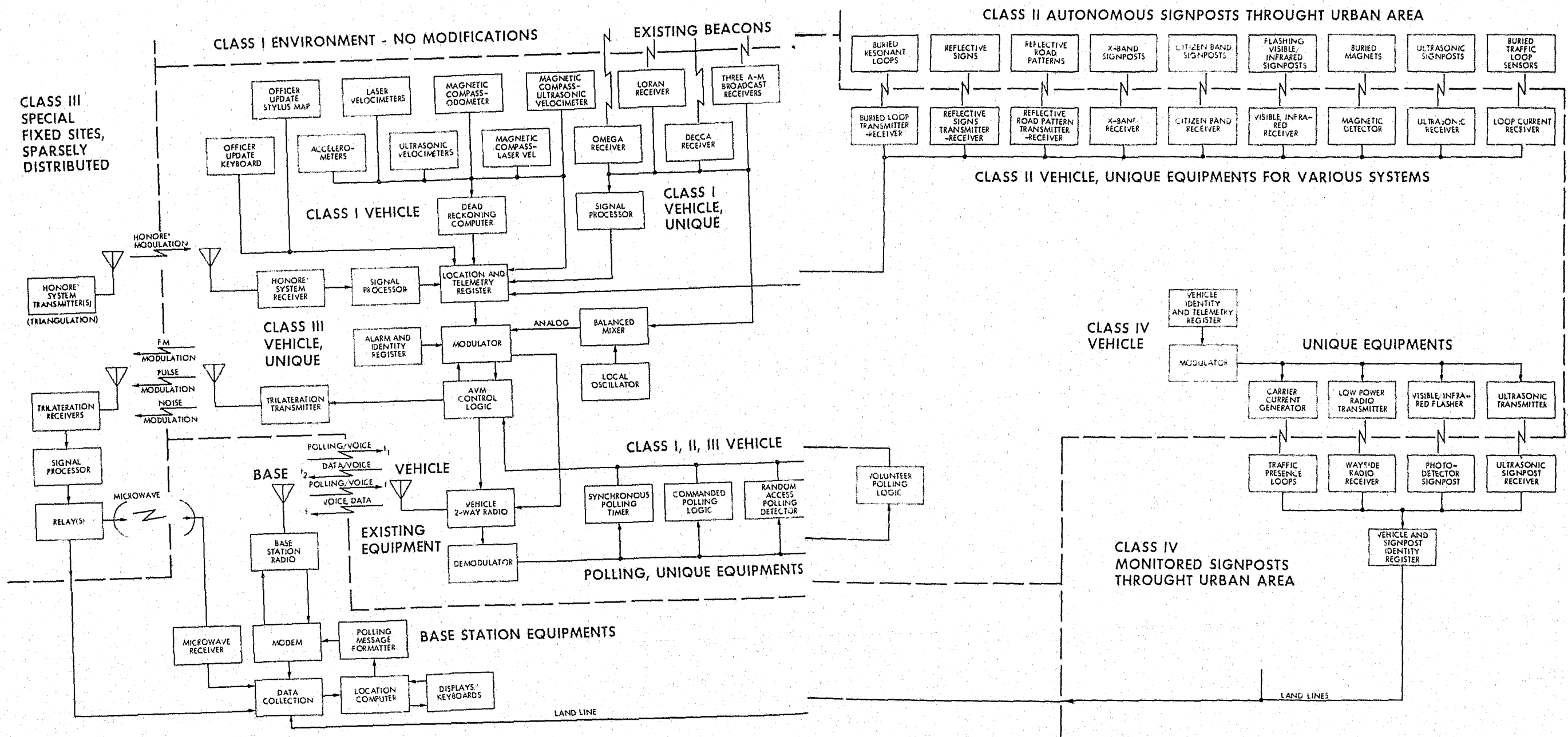


Figure 6. AVM Systems Showing Common and Unique Equipments for Vehicles, Signposts, and Base Stations

Class I, II, and III techniques may use any of the various vehicle polling techniques. Polling does not apply to the Class IV monitored signposts. The consideration of which polling method is to be used may depend heavily on whether or not equipments requiring digital communication have already been installed.

2. Technical and cost parameters. Virtually every technical performance and cost estimate parameter of a particular vehicle location technique is system-dependent. The AVM system accuracy, the numbers of fixed sites, the message lengths, the data rates, the base station computing, the information displays, software, and RF channel requirements are all functions of the particular application. Some functional elements and performance factors can be determined to a limited extent, such as the cost and coverage radius of the various signposts, RF beacons and traffic presence sensors in Classes II, III, and IV; and also the cost and minimum message requirements of the vehicle sensors and data processors in Class I.

In order that cost estimates could be made for the various AVM techniques, extremely simplified block diagrams of the unique functional elements associated primarily with the vehicle location process were developed. That is, only the vehicle sensor and AVM fixed sites associated with the particular technique were considered. These cost figures accompany each of the descriptions and considerations of the method in the following section.

#### B. AVM COST CONSIDERATIONS

In addition to the costs associated with the vehicular and fixed site functional elements required for the basic location process, there are the costs of yearly maintenance and vehicular radio additions or modifications for transmitting and receiving AVM signals. Estimates of the vehicular costs (as of 1974) for each class of AVM are presented in Table 2. In this table, the radio cost and the radio modification columns represent optional choices. That is, the radio modification cost is not applicable where a separate radio for AVM signals is selected.

The costs for fixed sites equipment, installation, operational maintenance, data link, and mileage charges per mile per month are summarized in Table 3 for Classes II, III, and IV.

Table 2. Vehicle Equipment Costs\* for All AVM Classes and Systems

VEHCOST	AVL COSTS PER VEHICLE IN \$						
	TECHNIQUE	SENSOR	PROC.	RADIO	RAD. MOD	INST	O-11
CLASS I							
KEYBOARD	45		40	1200	50	35	15
STYLUS MAP	2465		35	1200	50	35	25
2-ACCELEROMETERS	400		1000	1200	200	100	100
LASER VELOCIMTR	500		1000	1200	200	135	150
ULTRASONIC VELO	270		800	1200	200	100	150
COMPASS/ODOMETER	265		1000	1200	200	20	40
COMPASS-LASER VEL	655		1000	1200	200	150	20
COMPASS/ULTRASONIC VEL	385		1000	1200	200	100	30
OMEGA	2500		0	1200	200	30	75
LORAN	2000		0	1200	200	30	75
DECCA	170		0	1200	200	30	75
AM-STATIONS	200		0	1200	200	30	75
DIFF. OMEGA	2500		0	1200	200	30	75
DIFF. LORAN	2000		0	1200	200	30	75
DIFF. AM-STA.	315		0	1200	200	30	75
RELAY OMEGA	375		0	1200	150	30	60
RELAY LORAN	425		0	1200	150	30	100
CLASS II							
BURIED RES. LOOPS	90		0	1200	50	40	15
REFLECTING SIGNS	430		0	1200	50	100	20
REFLECTING ROAD	75		0	1200	50	30	15
N-BAND POST	120		0	1200	50	30	10
HF, UHF POST	105		0	1200	50	30	10
LF POST	100		0	1200	50	30	10
LIGHT-I-R POST	95		0	1200	50	30	15
BURIED MAGNETS	50		0	1200	50	30	25
ULTRASONIC POST	35		0	1200	50	35	25
TRAFFIC SENSOR	95		0	1200	50	40	10
CLASS III							
NAR-BAND FM PHASE	60		0	1200	165	40	25
WID-BAND FM PHASE	2875		0	0	30	30	25
PULSE T-O-ARRIVAL	2575		0	0	0	150	25
NOISE CORRELATION	785		0	0	0	100	25
DIRECTION FINDER	35		0	0	0	15	0
CLASS IV							
TRAFFIC LOOPS	80		0	0	0	65	10
WAYSIDE RADIO	75		0	0	0	40	10
PHOTO-I-R DETECT	115		0	0	0	70	15
ULTRASONIC DETECT	125		0	0	0	65	15

\* Costs as of 1974.

Table 3. Fixed Site Costs\* for Class II, III, and IV AVM Systems

TECHNIQUE	AVL COST PER SITE (OR UNIT) IN \$				
	EQUIP	INST	O-M	DATA LINK	LINE RENT
CLASS I					
KEYBOARD	0	0	0	0	0
STYLUS MAP	0	0	0	0	0
2-ACCELEROMETERS	0	0	0	0	0
LASER VELOCIMTR	0	0	0	0	0
ULTRASONIC WELD	0	0	0	0	0
COMPASS/ODOMETER	0	0	0	0	0
COMPASS/LASER VEL	0	0	0	0	0
COMPASS/ULTRASONIC VEL	0	0	0	0	0
OMEGA	0	0	0	0	0
LORAN	0	0	0	0	0
DECCA	0	0	0	0	0
RAIL-STATIONS	0	0	0	0	0
DIFF. OMEGA	0	0	0	0	0
DIFF. LORAN	0	0	0	0	0
DIFF. RAIL-STA.	0	0	0	0	0
RELAY OMEGA	0	0	0	0	0
RELAY LORAN	0	0	0	0	0
CLASS II					
BURIED RES. LOOPS	10	17	0	0	0
REFLECTING SIGNS	55	30	0	0	0
REFLECTING ROAD	0	30	25	0	0
V-BAND POST	200	45	15	0	0
HF. VHF POST	100	45	15	0	0
LI POST	125	45	15	0	0
LIGHT I-R POST	100	55	25	0	0
BURIED MAGNETS	2	4	0	0	0
ULTRASONIC POST	85	35	10	0	0
TRAFFIC SENSOR	95	40	0	0	0
CLASS III					
NAR-BAND FM PHASE	4500	500	500	25	5
MID-BAND FM PHASE	9500	1500	500	2070	0
PULSE T-O-ARRIVAL	12000	2500	500	2000	0
NOISE CORRELATION	7500	1500	500	2000	0
DIRECTION FINDER	26000	1500	1200	25	5
CLASS IV					
TRAFFIC LOOPS	165	113	10	13	4
WAYSIDE RADIO	160	113	25	13	4
PHOTO-I-R DETECT	170	113	25	13	4
ULTRASONIC DETECT	180	113	25	13	4

\* Costs as of 1974.

Additional costs associated with each AVM technique when configured as a system are the base station costs and the vehicle polling system costs, given in Table 4. The base station is assumed to include the vehicle location computer, the peripherals, the dispatcher displays, software, and yearly operational maintenance.

1. Vehicle cost parameters. Vehicle costing for an AVM system is a straightforward multiplicative process of determining the total cost to equip all vehicles in the fleet with the appropriate AVM sensor, data processor, vehicle polling equipment, and radio modification; motorcycles are not considered. If a separate radio link is deemed necessary for AVM purposes, then this additional cost must be added.

If the vehicle fleet has already been equipped with digital message entry devices (DiMED), keyboards, hard-copy printers, gas-plasma or cathode-ray displays, then some of the functional elements required for an AVM system have been established. Prior installation of digital message equipment was not considered in the costing of vehicular equipment.

2. Fixed site costs. Site costs unique to AVM systems are considered only in Classes II, III and IV. In determining the system costs, the number of installed units must first be determined. The design algorithms for fixed sites are dependent on the density distributions of intersections, road segments, and lanes, and on the area to be covered.

Most of the Class II AVM techniques that rely on radio ID signals are configured and costed on the basis of one autonomous signpost per intersection. The exception is the HF signpost which is configured on the basis of one unit for each four intersections because of the greater coverage radius. The reflective pattern signs techniques require two installations for each road segment because of the geometry constraints between vehicle and sign, whereas the traffic presence sensors require one installation for each road segment because of the nature of the normal installation. Buried loops and magnets require an installation per lane in each road segment. In addition, each installation is actually a multiple installation; i. e., there must be sufficient loops or magnets to provide adequate coding for each road segment. The cost estimates for fixed sites were based on an average of 2.4 lanes for each road segment, i. e., about 1 four-lane road for each 6 two-lane roads.

Table 4. Base Station Costs\* for All AVM Classes and Systems

TECHNIQUE	AUL BASE STATION COSTS IN THOUSANDS OF \$								
	SML	COMPUTER			O-M	DISP	SOFTWARE		
		MED	LGE	INST			SML	MED	LGE
CLASS I									
KEYBOARD	30	40	60	10	100	3	10	20	30
STYLUS MAP	30	40	60	10	100	3	10	20	30
2-ACCELEROMETERS	40	60	80	10	100	3	25	25	50
LASER VELOCINTP	40	60	80	10	100	3	25	35	50
ULTRASONIC VELO	40	60	80	10	100	3	25	35	50
COMPASS ODOMETER	40	60	80	10	100	3	25	35	50
COMPASS-LASER VEL	40	60	80	10	100	3	25	35	40
COMPASS-U-SONIC VEL	40	60	80	10	100	3	25	35	40
OMEGA	30	50	70	10	100	3	20	30	40
LOPHAN	30	50	70	10	100	3	20	30	40
DECCA	30	50	70	10	100	3	20	30	40
AM-STATIONS	30	50	70	10	100	3	20	30	40
DIFF. OMEGA	30	50	70	10	100	3	20	30	40
DIFF. LOPHAN	30	50	70	10	100	3	20	30	40
DIFF. AM-STA.	30	50	70	10	100	3	20	30	40
RELAY OMEGA	30	50	70	10	100	3	20	30	40
RELAY LOPHAN	30	50	70	10	100	3	20	30	40
CLASS II									
BURIED RES. LOOPS	30	40	60	10	100	3	10	20	30
REFLECTING SIGNS	30	40	60	10	100	3	10	20	30
REFLECTING ROAD	30	40	60	10	100	3	10	20	30
2-BAND POST	30	40	60	10	100	3	10	20	30
AMP. VHF POST	30	40	60	10	100	3	10	20	30
LF POST	30	40	60	10	100	3	10	20	30
LIGHT I-R POST	30	40	60	10	100	3	10	20	30
BURIED MAGNETS	30	40	60	10	100	3	10	20	30
ULTRASONIC POST	30	40	60	10	100	3	10	20	30
TRAFFIC SENSOR	30	40	60	10	100	3	10	20	30
CLASS III									
NAR-BAND FM PHASE	33	80	137	3	100	3	20	40	60
WID-BAND FM PHASE	40	70	70	10	200	3	25	50	100
PULSE T-O-ARRIVAL	100	250	250	10	175	3	35	70	100
NOISE CORRELATION	100	250	250	10	175	3	35	70	100
DIRECTION FINDER	15	30	60	10	150	3	15	30	60
CLASS IV									
TRAFFIC LOOPS	30	40	60	10	100	3	10	20	30
WAYSIDE RADIO	30	40	60	10	100	3	10	20	30
PHOTO-I-R DETECT	30	40	60	10	100	3	10	20	30
ULTRASONIC DETECT	30	40	60	10	100	3	10	20	30

\*Costs as of 1974.

The number of loops at each lane segment was that sufficient to provide a unique base-2 code for each road segment. The number of magnets used is half this value since spaces can be used to provide approximately half the coding bits (magnet for "one", space for "zero").

Since the Class III synchronized RF sites are more sparsely distributed, their numbers are estimated on the basis of urban area for the selected phase and pulse time-of-arrival techniques. The radius of coverage for narrow-band and pulse systems, based on prior tests and experiments, is set at 5 km (3 miles). In addition, the requirement that, wherever possible, four or more antennas should cover the given area is imposed. This procedure provides data for least-squares computation as opposed to the analytic "flat earth" solution of vehicle location. The wide-band antenna coverage radius is set at 11 km (7 miles), based on prior tests. Design algorithms were established from the rectangular model cities data as follows:

$$\text{Number of narrow-band and pulse sites} = 6 + \frac{\text{area in km}^2}{10}$$

$$\text{Number of wide-band sites} = 4 + \frac{\text{area in km}^2}{40}$$

The number of fixed sites in the southern California UGAC cities was determined from geometrical gridlined overlays superposed on outline maps of the cities. The outline and site locations for the cities are depicted in figures that accompany Part 2 of this Report. A minimum number of fixed sites for noise correlation and direction finding was established, recognizing that this number is probably insufficient for all but the smallest cities.

Class IV monitored signposts were configured and costed on the same basis as the equivalent Class II devices. Telephone line rental is, however, included in the site costs where applicable as the line should be considered an equipment cost as opposed to an operation cost.

3. Base station costs. Base station equipment costs were estimated on the basis of both urban area coverage and fleet size. The station's computer costs were estimated on the basis of area, and the software costs were based on fleet size. This separation of cost elements is only partially defensible. It is assumed that a minicomputer is usually used to support the AVM function with varying amounts of bulk storage (disc) to accommodate the city map for output display.



Exceptions are in the Class III time-of-arrival (TOA) methods, where larger machines are assumed. The pulse and noise-correlation techniques also require a larger computer with more speed and versatility than can be provided by a minicomputer because of the inherent capability of servicing many more vehicles per unit time and the need to accommodate a large number of inputs in real time. The software estimate based on fleet size is also difficult to justify totally. Much reliance was placed on prior work estimates and on the judgments of systems analysts.

Three estimates each of base station computer and software costs were made based on model city parameters for small, medium and large cities. For the UGAC cities, the costs were determined based on the urban areas and the total fleet size, excluding motorcycles, using linear interpolation.

Display equipment costs are included in the base station costs on the basis of the actual number of dispatchers in the case of UGAC cities. For the model cities, the costs are estimated on the basis of 1 display console for each 50 vehicles or less.

4. Installation costs. Equipment installation costs were obtained by multiplying the cost per unit vehicle and the cost per fixed site installation by the appropriate number of units. Together with the base station installation cost, they make up the tabulated total cost. A constant cost value is assumed for the base station, which is a rounded average value of prior estimates made in conjunction with AVM demonstration tests.

5. Operation and maintenance costs. The estimates of O - M costs for equipment installed in vehicles, at fixed sites, and the base station are based on experience values for both mobile and fixed equipments. In the base station, the principal cost element is for operation and maintenance personnel. Three persons (one per shift) were assumed in all AVM techniques to provide software support or equipment service. Although this assumption may not be justifiable, it was believed that AVM is a comparatively new technology which will probably interface with computer-aided dispatching and digital message systems and that additional service personnel would be required for a substantial time period after the initial installation.

## V. VEHICLE POLLING AND LOCATION PERFORMANCE

Four classes of vehicle polling are considered for AVM Systems:

(1) Synchronous, (2) Commanded or random access, (3) Synchronous with Command capability, and (4) Volunteer or contention. All four techniques are generally applicable to Class I and II AVM Systems. Synchronous polling and synchronous with command are used mainly in Class III Systems. For the Class IV monitored signpost systems, which use land lines, polling by radio is not applicable in the context used in this description.

All polling techniques are suitable for half-duplex (base station and vehicle on the same frequency), but when the base station relays all vehicle transmissions or when each vehicle monitors all other vehicles, then the Volunteer technique can only be used on full-duplex (base and vehicle on different frequencies).

1. Synchronous polling. In this technique, each vehicle transmits location data at a preselected time within the fleet polling sequence. Equipment on the vehicle keeps track of the start of the sequence and internally determines when its time to respond occurs. The cost of the vehicle polling equipment installed (as of 1974) is about \$270.

2. Synchronous with command capability. This polling technique allows the base station to modify the position of each vehicle in the polling sequence. The cost of the vehicle equipment installed is about \$365.

3. Commanded or random access polling. In this technique, the base station sends a request to each vehicle whenever location data is required. This technique is the most flexible but requires more use of available RF time.

4. Volunteer polling. This contention method requires that each vehicle determine whether the channel is "clear" before transmitting. The cost of vehicle equipment installed is about \$170.

These vehicle polling techniques were evaluated with both a simple one-time radio message transmission and with redundant transmissions where every message is sent twice. The digital message rate is set at 1500 bps. Where equivalent RF channels are assumed, a channel spacing of 25 kHz is used. Message lengths are about 20 bits, or occupy about 15 millisecond transmission time. Delays due to equipment turn-on times reduce the achievable polling rate.

**PART ONE:  
AVM COST BENEFIT  
INFORMATION BASE**

**G.R. Hansen**

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I. PERFORMANCE AND COSTS OF PROVED AVM TECHNIQUES

Costs and performance parameters of 36 operational or proved techniques used for automatic vehicle monitoring (AVM) are described and illustrated in this section. Schemes that are primarily intended for vehicle identification, such as those used in rail freight or extensions of point-of-sale methods are not included. In this Report, the vehicle monitoring techniques are categorized into five broad classes, based on system element types and functions: Class O Manual Monitoring, with no augmentation of location information; Class I AVM, with no additions to the urban environment; Class II AVM, using densely distributed autonomous signposts; Class III AVM, using sparsely distributed special transmitting/receiving fixed RF sites; and Class IV AVM, using densely distributed monitored signposts. Estimated special equipment and installation costs are as of 1974.

A. Class 0 Manual Monitoring. No AVM

This is the baseline vehicle location technique against which other systems should be compared. A manual monitoring system consists of a dispatcher, an existing real-time communication system, and a fleet of vehicles. The dispatcher's knowledge of vehicle locations depends upon voice communications with the officers in the vehicles. Even in the manual vehicle monitoring class, there are several options that affect both performance and costs. The dispatcher can, for example, rely strictly upon his knowledge of each vehicle's designated location or patrol area and its subsequent assignments. Alternatively, he can use some of his RF resources (channels and air time) to interrogate and obtain actual vehicle locations vocally.

A relatively wide range of options is available to the dispatcher for use with Class 0 non-automated vehicle monitoring. The simplest visual location aid is just a map on which the assigned beat areas are permanently marked, the dispatcher relying on his memory to locate the vehicles on the map. Numbered magnets or lights may be used which may be updated manually to augment his memory. Elaborate electro-optical display devices are available, which indicate each vehicle's last known location, status, and anticipated destination, all driven by manual input.

The dollar cost of a purely manual vehicle management system is almost bound to be competitive, but the use of RF resources could be prohibitive, and the attainable dispatching performance is also an open question. With an AVM system, the closest available vehicle can quickly be dispatched in response to a service request. Analyses indicate that response times are reduced and fleet efficiency is increased by up to 7%, permitting a reduction in fleet size and in operating costs.

B. Class I AVM. No Modification to Urban Environment

1. Officer update. Vehicle location data may be encoded automatically by means of manually operated devices installed in the vehicle, such as keyboards or stylus maps.

a. Keyboard entry. This manual data input technique for providing automatic vehicle location data at the base requires the officer to enter some code or identifying numerical sequence on a digital keyboard (Fig. 1-1). The keyboard can be either the device being used for sending digital messages or a separate unit. The location code can relate to a particular street segment and/or intersection and would probably be four or five digits in length. The vehicle location code is transmitted to the base station either by "Touch-Tone" or some other digital modulation techniques. Volunteer or random-access vehicle polling is most suitable for this technique. The AVM system accuracy is dependent on the code used; that is, either (1) the nearest intersection if only streets or intersections have codes, (2) a particular block on a street if each segment is coded, or (3) the location in a block if street segment is followed by address digits of closest property parcel. The automatic computational requirement is a table look-up function to translate the code to a geographical location. While this AVM technique is low in cost, particularly if a digital message entry device (DiMED) is already installed, it is extremely slow and requires much memorization on the part of the patrolling officers. If the car is out of the normal beat, either a map or street guide would have to be used by the officer for reference to determine the code.

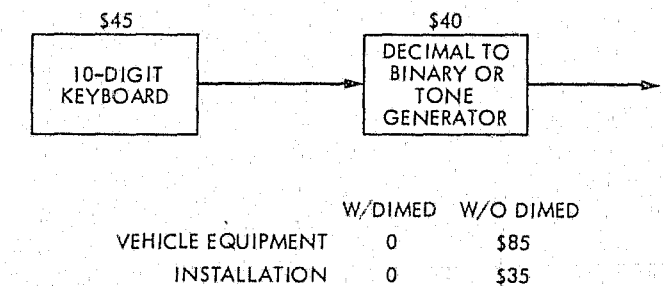


Fig. 1-1. Class I AVM Officer Update Option, Using Keyboard Entry

b. Stylus map. This officer update technique is a manual method whereby the patrolling officer indicates his vehicle's location by pressing the appropriate spot on a special map (Fig. 1-2) with a stylus. The map-and-holder combination encodes the spot where the pressure is applied, and the digital code is sent to the base station. The location polling process can be either in response to a request or volunteered

as part of a transmission from the vehicle. Location accuracy is dependent on the scale of the map and on the holder encoding technique. For example, a 20 x 25 cm (8 x 10 in.) portion of a 7.5-minute U. S. Geological Survey topographic map (scale 1:24000) would cover an area of 6 x 4.8 km (3.6 x 3 mi). If this information were encoded by 5 binary bits (1 in 32) on each axis for a 10-bit location code, then the location could be achieved within a rectangle of about 190 x 150 meters (600 x 500 ft). By increasing the encoding to 12 bits or using a map with half the scale, the size of the vehicle's location rectangle could be decreased by one-half in each dimension. Maps of other beats would probably be required by each officer together with some means of identifying when these maps were in use. The base station computation requirement is a table look-up function to translate the code to a geographical location.

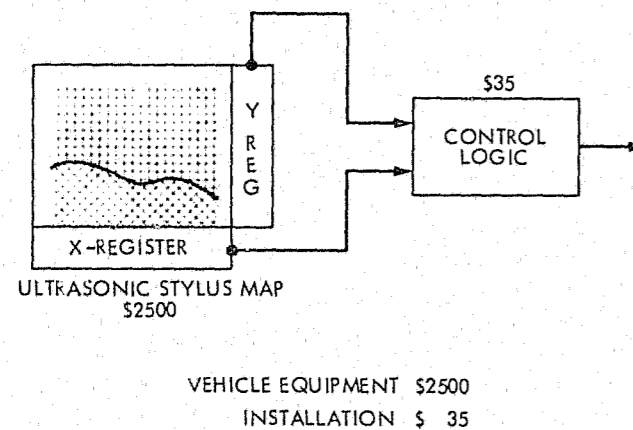


Fig. 1-2. Class I AVM Officer Update Option, Using Stylus Map

2. Kinematic sensors. Changes in vehicle location may be sensed either by accelerometers, velocimeters, or odometers.

a. Two accelerometers. Dead reckoning, which can measure the change in location of a vehicle, can be mechanized with two accelerometers (Fig. 1-3). These devices would measure the rate of change of velocity of the vehicle in the horizontal plane of the vehicle in both the fore-and-aft and sideways directions. The outputs of the two accelerometers can be used to compute velocities attained as well as changes in direction and distance during a selected time interval. The computations can be performed on-board the vehicle and the results transmitted to the base station, or the outputs of the accelerometers can be encoded and transmitted directly to the base station.

A U-turn made at a speed of 10 m/sec (23 mph) in a 4-lane street about 18 m (60 feet) wide is about the limit of vehicle turning performance. This turn would result in about a 0.8-g indication of lateral motion for just over 3 seconds. If the accelerations are sampled and transmitted every 0.03 second, then the 16 data bits each time would lead to a data rate of 4800 bits/sec. Based on personal rapid transit studies, the "comfort"

zone of vehicle operation is in the less than 0.2-g range. If most accelerations experienced by the vehicle are maintained in this 0.2-g region, then a 1% full-scale error during a low-g maneuver causes these normal measurements to be in error by 4% or more.

b. Orthogonal laser velocimeters. This kinematic sensor technique is based on prior work by G. Stavis (Ref. 1), which used a laser velocimeter (Fig. 1-4) and compass (Fig. 1-5). In this scheme, the laser would be used to measure not only the forward velocity of the vehicle, but also that velocity component which occurs during turns and is at a right angle to the fore-and-aft motion. All portions of the vehicle which are not located on the turning axis experience some side velocity during a turn. The sign and magnitude of this velocity component is a function of the distance from and location with respect to the turning axis. If both forward and side velocities are measured at the same point remote from the turning radius, then the velocities at this point provide a means to keep track of the vehicle motion. The operation of the laser velocimeter is based on the speckle pattern observed in the reflection of coherent laser light from a surface that moves relative to the source. The speckles tend to move in the opposite direction to the relative motion between the laser source and the reflecting surface. By passing the reflected laser light through a diffraction grating and then to a photodetector, a signal can be derived with a frequency that is a direct measure of the velocity of the reflecting surface. The velocity measured is that at right angles to the rulings on the grating. Two photo detectors and two gratings with the rulings at right angles provide the means to measure the two components of motion of a single laser spot. Investigators in the cited work (Ref. 1) indicate that a laser velocimeter's dynamic range is of the order of 2500 to 1 and that the maximum and minimum measurable velocities are primarily a function of the rulings on the grating. For example, a vehicle velocity range of 50 m/sec to 2 cm/sec (115 mph to 0.05 mph) could be accommodated, and turning rates of 0.01 radian/sec (0.6 °/s) could be detected. Maximum data bit rates of about 5000/sec for speed and 100/sec for turning may require in-vehicle computation.

c. Ultrasonic velocimeters. The use of ultrasonic waves for intrusion detectors, motion sensors, and distance measuring is well established. The doppler frequency shift of a reflected sound wave from the road surface can form the basis of a velocimeter (Fig. 1-6). An ultrasonic wave directed at an angle at the road surface will reflect a doppler-shifted frequency proportional to the cosine of the angle of incidence times the surface velocity. For example, if a 33-kHz frequency is chosen which has a wave length of about 1 cm directed at a 45-degree angle to the road surface and traveling at 50 m/sec (115 mph) will yield a doppler shift of about 10%. If a dynamic range of 2000:1 can be achieved, a minimum velocity of 2.5 cm/sec (0.05 mph) can be detected. If the velocimeters are mounted on each side of the vehicle and the differential velocities are measured to the same 2.5 cm/sec, then minimal directional changes of 12 mrad (about 0.7 deg) can be detected. This precision is on the order of that achieved with the differential odometer, described later.

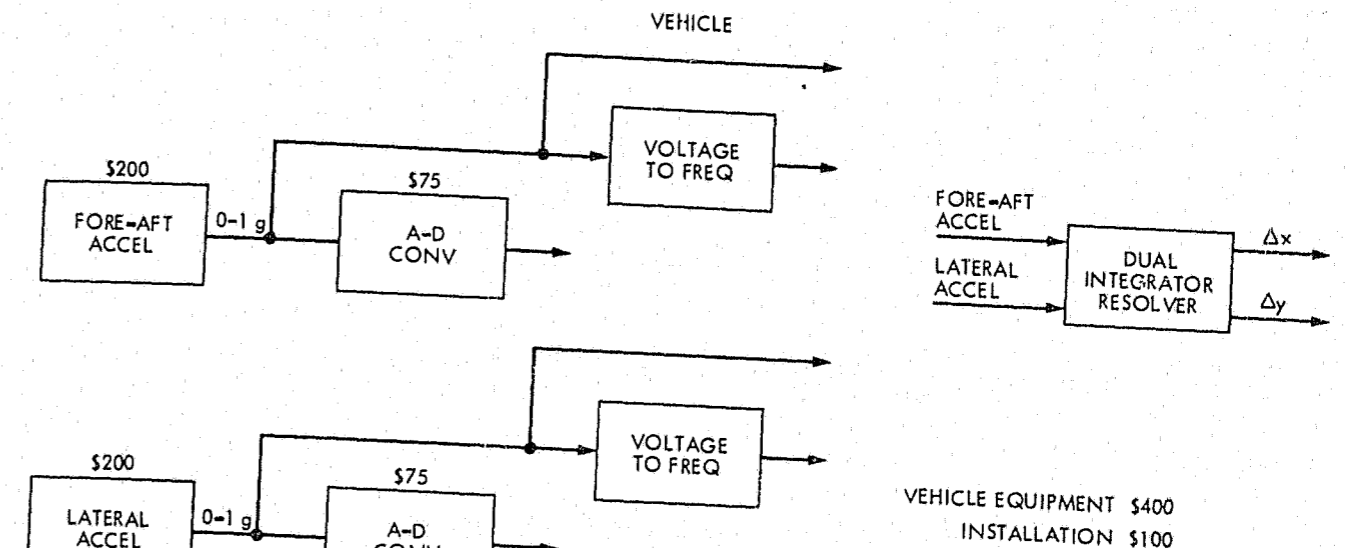


Fig. 1-3. Class I AVM Kinematic Sensor Using Two Accelerometers

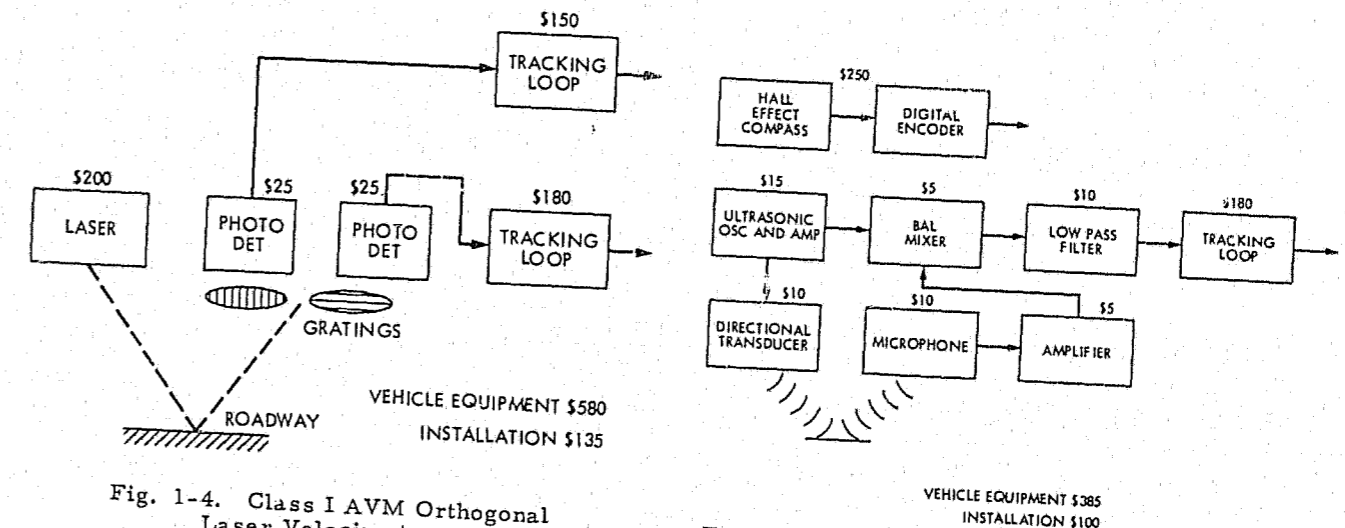


Fig. 1-4. Class I AVM Orthogonal Laser Velocimeter

Fig. 1-6. Class I AVM Magnetic Compass with Ultrasonic Velocimeter

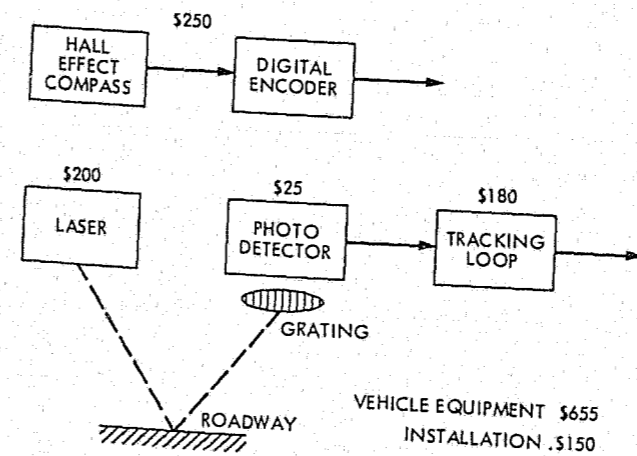
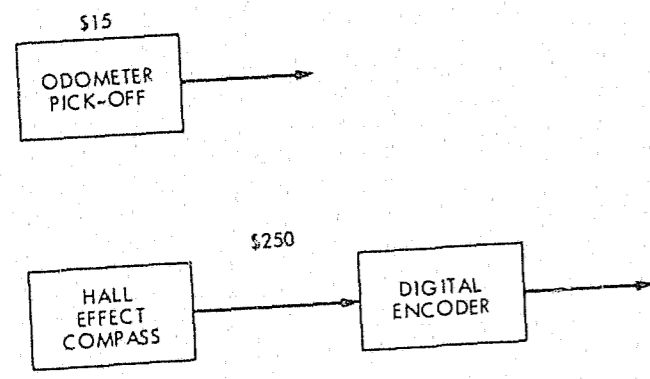


Fig. 1-5. Class I AVM Magnetic Compass with Laser Velocimeter

d. Odometer-Compass. Dead reckoning with compass and odometer (Fig. 1-7) has been tested, built and furnished to several armed forces (U. S., Canada, Britain) as a means of keeping track of military vehicles in off-road situations. The systems have all achieved some measure of success, and all have included on-board computation to indicate position in northings and eastings (Y- and X-coordinates). Accuracies within 0.6 to 2% of the distance travelled have been demonstrated. Error sources are the inaccuracies in the odometer measurement and compass heading. The odometer is affected by tread wear and wheel slip maneuvering. Compass heading is influenced by local anomalies, and proposed filtering techniques have included measuring the steering gear angle, vertical component of the field, and limiting direction change as a function of vehicle speed. At present, gyro compasses are not suited for vehicular applications.

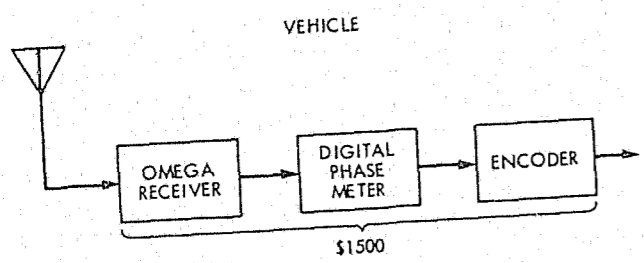


VEHICLE EQUIPMENT \$265  
INSTALLATION \$ 20

Fig. 1-7. Class I AVM Magnetic Compass with Odometer

3. Wide-area navigation. The three principal wide-area navigation schemes use synchronized radiolocation beacons. They are hyperbolic techniques which operate in three different modes: OMEGA, LORAN, and DECCA.

a. OMEGA. This navigation scheme (Fig. 1-8) uses very low frequency (10-13 kHz) time-multiplexed RF signals. The relative phase of the

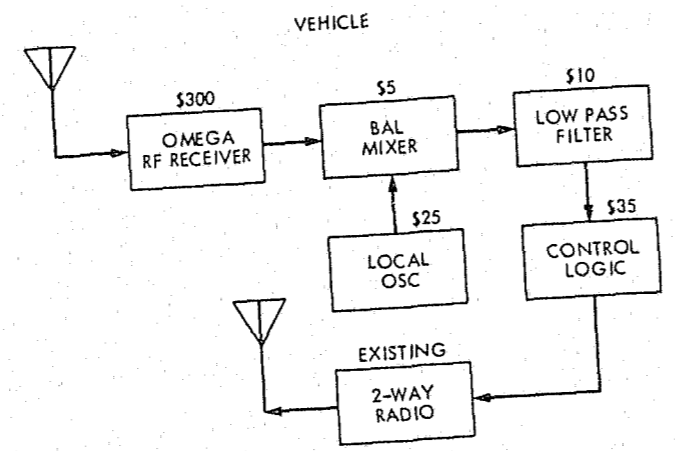


VEHICLE EQUIPMENT \$1500  
INSTALLATION \$ 80

Fig. 1-8. Class I AVM Normal and Differential OMEGA Navigation

signals, transmitted on the same frequency in sequence from several sites, defines a set of lines of position (LOP). At the intersection point of the LOPs is the receive location. There are ambiguities in position since the phase patterns repeat every 15 km or so. Differential OMEGA is a technique for reducing the effects of local anomalies. A fixed receiver at a precisely known location is used to remove these anomalies over a 15 to 30 km radius through continuous monitoring of the received signals.

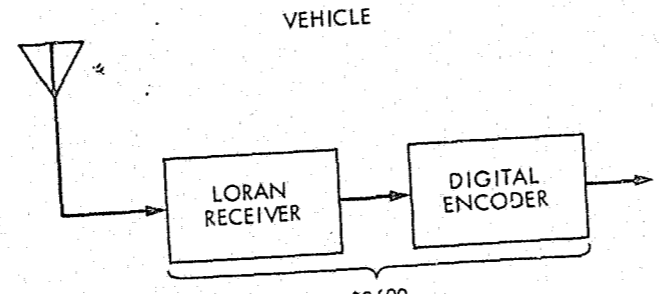
b. Relay OMEGA. In this technique (Fig. 1-9), the vehicle rebroadcasts the raw OMEGA signals on another frequency to the base station. The base station then measures the phase differences and computes the LOPs. This is a time-consuming operation as each vehicle would have to transmit the entire OMEGA sequence lasting several seconds.



VEHICLE EQUIPMENT \$375  
INSTALLATION \$ 80

Fig. 1-9. Class I AVM Relay OMEGA Navigation System

c. LORAN. This technique (Fig. 1-10) uses combined pulse and phase time-multiplexed RF signals for determining LOPs. Pulsed signals from three or more stations are transmitted 10 to

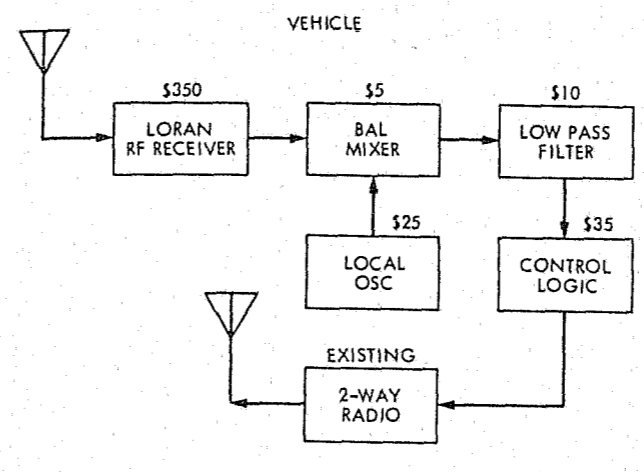


VEHICLE EQUIPMENT \$2600  
INSTALLATION \$ 80

Fig. 1-10. Class I AVM Normal and Differential LORAN Navigation

33 times a second in coded groups. The receiver measures the time of arrival difference from given pairs of signals to determine the LOP. No ambiguity exists, and each LOP is unique geographically. Differential LORAN also uses fixed site receivers to remove local propagation anomalies.

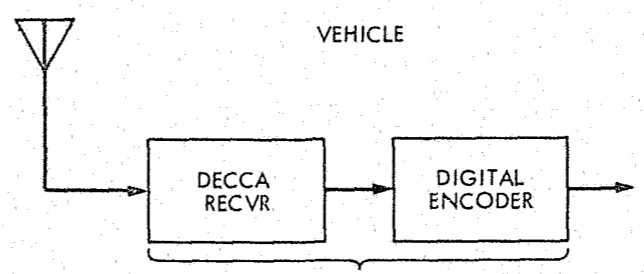
d. Relay LORAN. In this system (Fig. 1-11), the received signals are retransmitted to a base station for time differencing. Some bandwidth compression is required and is used in a technique called LOCATES in order to retransmit the 90 to 110 kHz LORAN over voice communication channels. The 20-kHz bandwidth signals are reduced to 3 to 7 kHz for retransmission. The higher repetition rates of LORAN make relaying more feasible than in OMEGA.



VEHICLE EQUIPMENT \$425  
INSTALLATION \$ 80

Fig. 1-11. Class I AVM Relay LORAN Navigation System

e. DECCA. The DECCA system (Fig. 1-12) is a continuous-wave phase-difference technique in which each transmitter operates on a different, but harmonically related, signal to other transmitters. The location is determined by simultaneous reception and comparison of the phase of the signals. Since the LOPs determined by the phase measurements are not unique, special signals are transmitted frequently to enable the determination of the correct one.

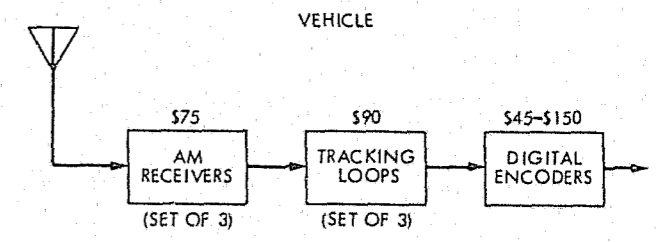


VEHICLE EQUIPMENT \$950  
INSTALLATION \$ 60

Fig. 1-12. Class I AVM DECCA Navigation System

f. AM Broadcasting stations as radiolocation beacons. Carrier signal frequencies, being transmitted from three commercial broadcasting stations located around a city's perimeter, can each be separately received and multiplied by relatively low-cost in-vehicle equipment to synthesize a new common frequency. These three identical frequencies can be made relatively phase coherent. Virtual hyperbolic patterns of navigational LOPs are generated by the signals received

from each pair of AM stations. These LOPs can serve as the basis for a reliable AVM system (Fig. 1-13). A vehicle's starting position is first noted and recorded at the central command base. When the vehicle moves, the phase differences produced in the three signal frequencies are measured on-board, and the number of times that the phase pattern is repeated can be counted on-board. This digital information is then sent to the base where a minicomputer converts it to the vehicle's new geographical location. In Part Four of this report, this AVM system is described in detail.



	NORMAL	DIFFERENTIAL
VEHICLE EQUIPMENT	\$200	\$315
INSTALLATION	\$ 50	

Fig. 1-13. Class I AVM AM Broadcasting Station Navigation Systems

C. Class II AVM: Autonomous Signposts Throughout Urban Area

All autonomous signpost location techniques rely on the vehicle coming near or passing over an instrumented geographical location. The instrument, located at an intersection or road segment, is usually a continuously radiating device sending out a uniquely coded message, either radio, light, IR, ultrasound, or magnetic. The vehicle is equipped with a suitable receptor to receive and store the message for subsequent retransmission to the base station and in this way inform the base as to the last instrumented location passed.

1. Radio frequency signposts. Most of the techniques use RF signals as the medium for the short-range link from wayside or roadway signpost to vehicle. These signals, which may range from low frequencies (190 kHz) through VHF to X-band (10 GHz), require the equipment shown in Figs. 1-14, 1-15, 1-16. Elevated locations for the signposts are usually selected to achieve a larger coverage area, freedom from blocking by large vehicles, and to lessen the probability of vandalism. Vehicle location accuracies of the Class II AVM systems are a function of the radius of influence and density of the signposts, and similarly the message repetition rate from the post must increase as the radius of influence decreases to ensure complete message reception by a fast moving vehicle.

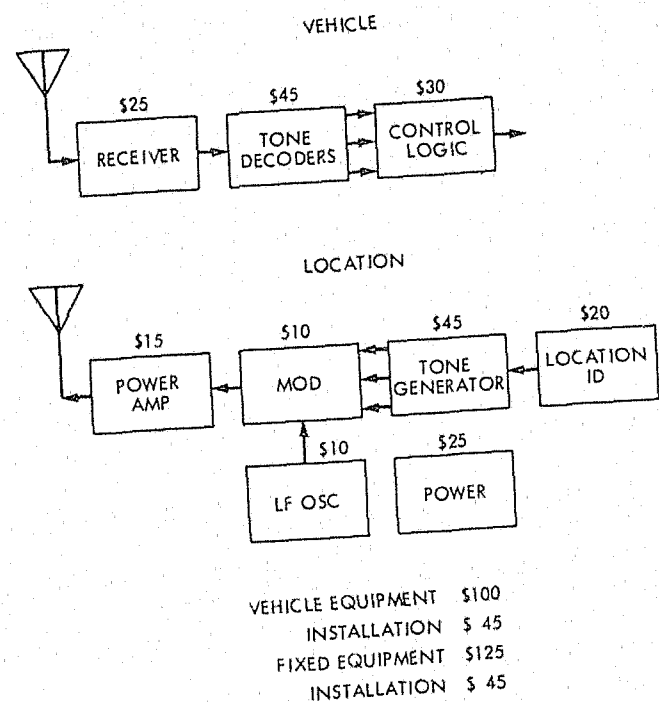


Fig. 1-14. Class II AVM Low-Frequency Wayside Radio Signposts

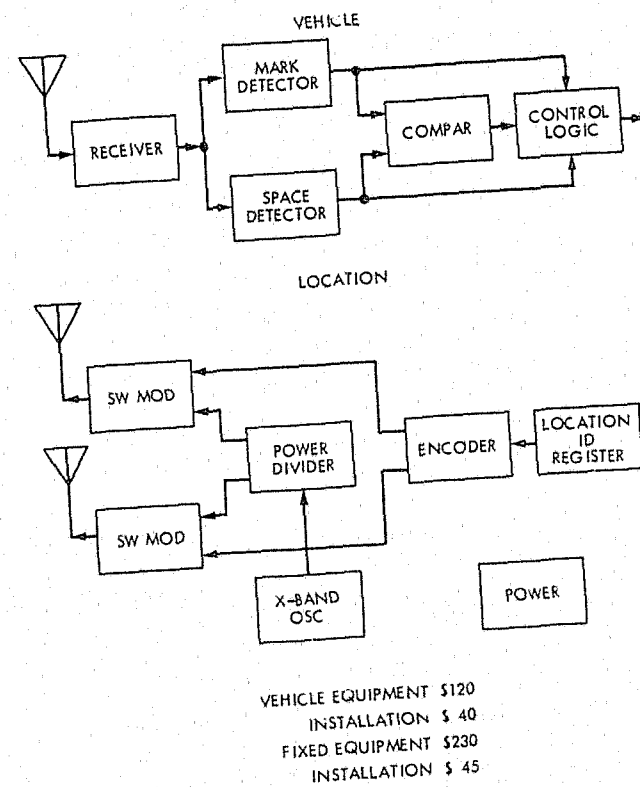


Fig. 1-16. Class II AVM X-Band Wayside Radio Signposts

Since active electronic signposts require some primary power source, difficulties may be encountered in general applications if reliance is placed on either street lighting circuits or traffic signals. In some applications, alternate power sources will be necessary. Options other than utility power are long-lived batteries, solar, and radioisotope sources.

2. Ultrasonic and photo or IR signposts. Ultrasonic and light radiation are possible practical approaches to the message link to avoid further RF congestion and interference to other services. The ultrasonic waves (Fig. 1-17) are similar in length to X-Band RF (less than 1 cm), and "horn" antennas can be designed for focusing sound to a desired coverage area. The flashing light approach (Fig. 1-18), either visible or infrared, is also a practical short-range information transfer method. Both of these techniques are, however, somewhat hindered by weather conditions, particularly fog, rain, and wind.

3. Buried active antennas. The buried antenna approach using existing traffic-presence sensor loops as electronic signposts (Fig. 1-19) is currently being tested in San Francisco and New York as a toll authority billing technique for equipped buses. In these systems, the antenna (buried loop) interrogates continually and receives responses from instrumented buses so that the buses may be billed for toll fees without having to stop. The use of traffic sensor loops as antennas is a practical implementation for electronic signposts and has an added advantage in that weather-proof enclosures and power are available in the traffic signal controller.

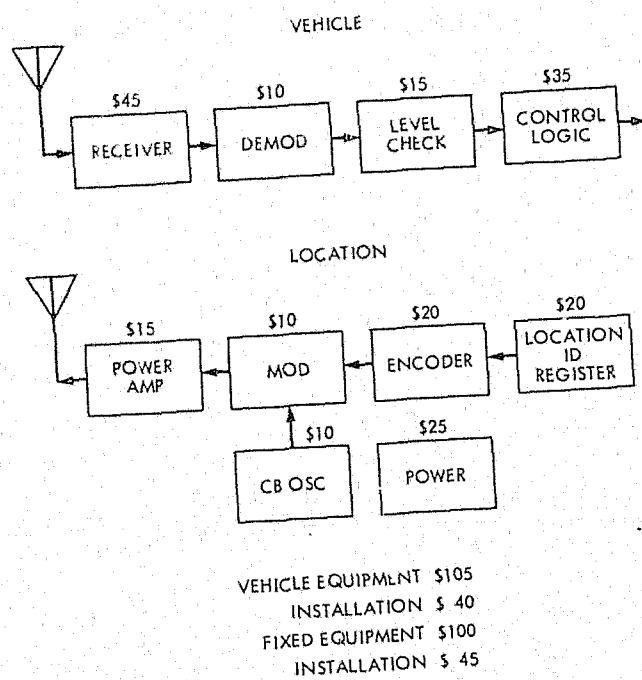


Fig. 1-15. Class II AVM Citizen Band or VHF Wayside Radio Signposts

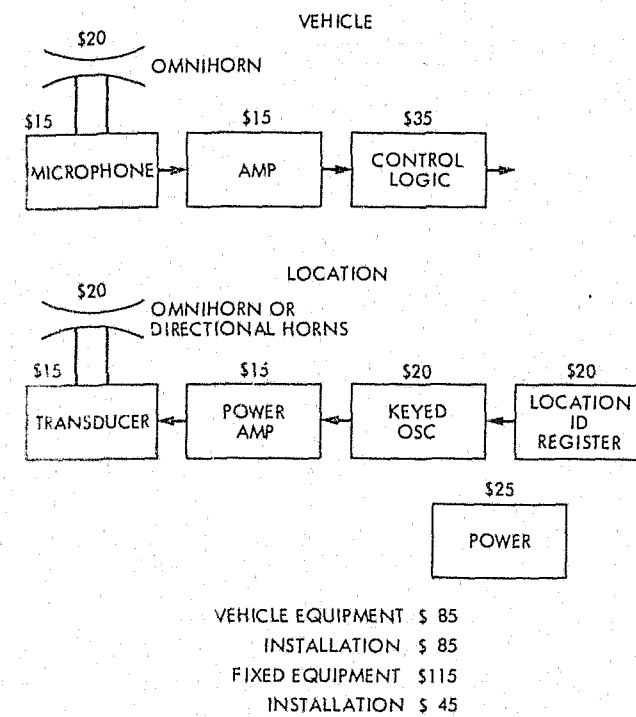


Fig. 1-17. Class II AVM Autonomous Ultrasonic Signposts

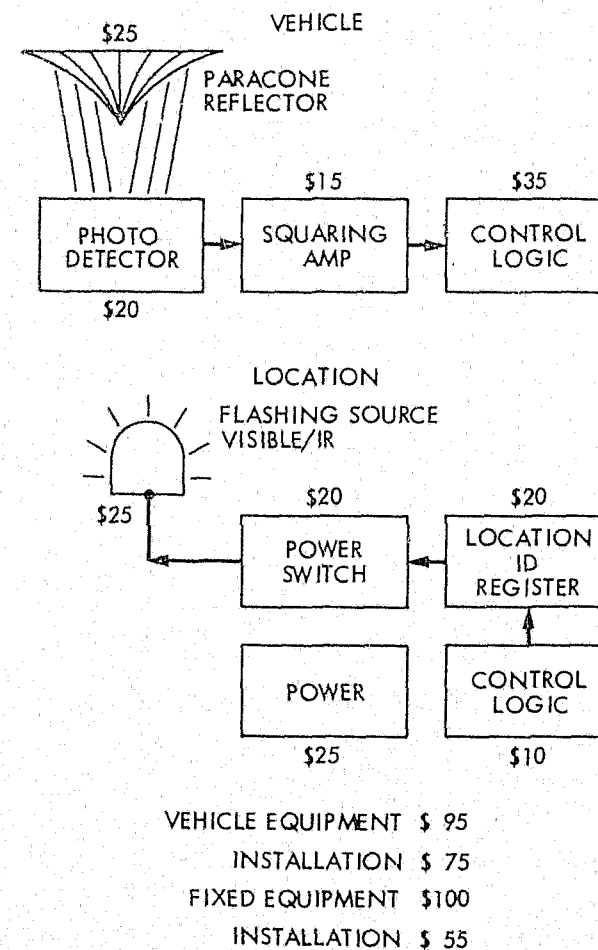


Fig. 1-18. Class II AVM Flashing Visible or IR Light Signposts

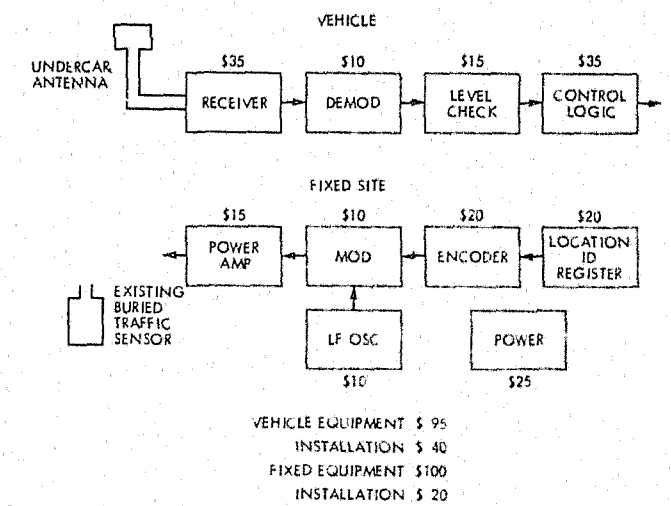


Fig. 1-19. Class II AVM Active Buried Antenna Traffic Sensors

4. Buried magnet autonomous location identifiers. Buried permanent magnets are used to provide a means of passive proximity location identification (Fig. 1-20). In this concept, rows of permanent magnets are installed along vehicle lanes to provide a means of inducing a voltage in a sensing coil mounted on the vehicle. The magnets could be either placed in drilled holes in the pavement or propelled into the surface by using an explosive-actuated concrete fastener tool. Magnets in the rows have either N or S poles up to provide binary identification of the location. The sense coil in a forward moving vehicle would detect signals of different polarities depending on the vehicle direction across the magnetic field. Reasonably strong magnets must be used, both to be detected in the presence of the earth's field, which is about 0.5 gauss, and to withstand added spacing that could be created by street resurfacing.

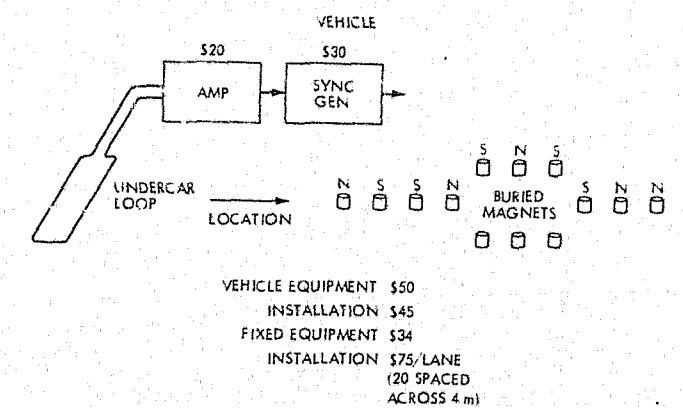


Fig. 1-20. Class II AVM Buried Magnets as Location Identifiers

5. Reflective paint patterns on signposts and roadways. Other passive techniques require that the vehicle continually interrogate the area travelled either by low-frequency RF or light radiation. In the case of the reflective wayside sign (Fig. 1-21) or pattern on the road (Fig. 1-22), the vehicle must be in a fairly precise position to

receive a response — less in the case of the road pattern than the wayside sign.

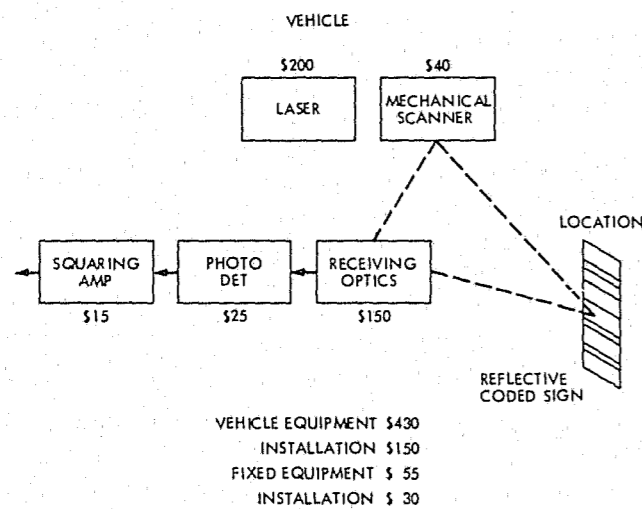


Fig. 1-21. Class II AVM Sensor of Reflective Patterns on Signposts

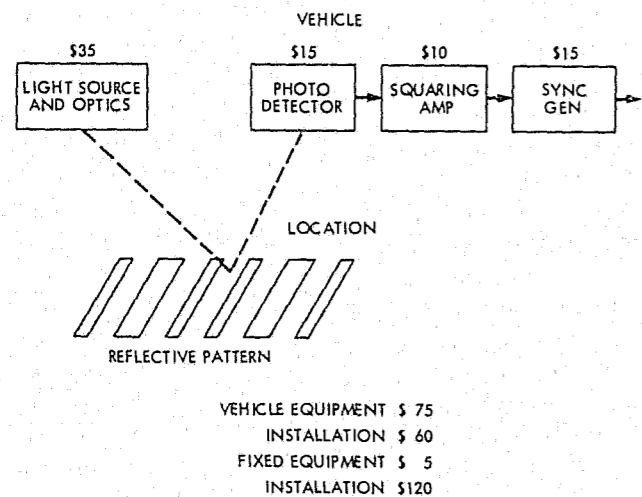


Fig. 1-22. Class II AVM Sensor of Reflective Patterns on Roadway

6. Passive buried loops. The passive buried loop (Fig. 1-23) requires that the vehicle, equipped with under-car antennas, pass over and excite the loops to obtain a response. Results of a detailed analysis of the buried loop coupling are included in Part Four of this report.

D. Class III AVM. Sparsely Distributed Special RF Sites

This class of AVM systems encompasses those vehicle location techniques of the trilateration rho-rho (range-range) and triangulation theta-theta (angle-angle) types with sparsely distributed RF sites primarily intended for medium or small urban area coverage, 7 km (4 mi) to 11 km (7 mi) radius.

1. Trilateration Systems. Included in the rho-rho systems are trilateration techniques which measure the time-of-arrival (TOA) of a signal emanating from a vehicle at several fixed receiving sites. Each pair of time differences

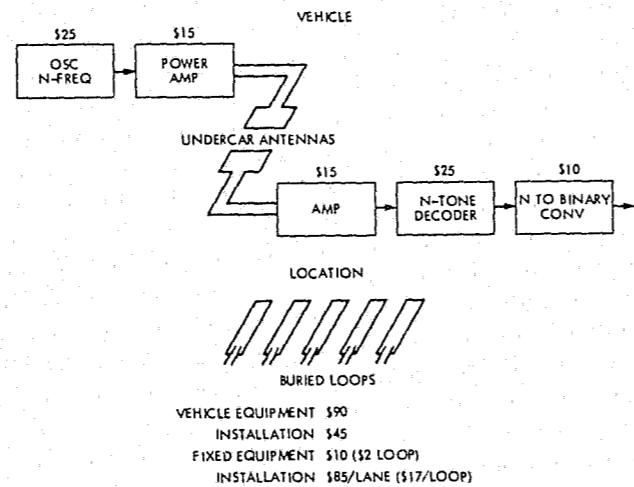


Fig. 1-23. Class II AVM Sensor of Passive Buried Resonant Loops

forms a hyperbolic line-of-position (LOP). The intersection of these LOPs establishes the position of the vehicle. This information may be sent to the base station from the site by leased telephone lines or by microwave transmissions.

Hyperbolic trilateration methods tested have used either a pulsed (or keyed) carrier from the vehicle or an audio-tone frequency modulating a carrier. The pulse systems measure the TOA of the signal and establish the range differences directly. The tone trilateration systems measure the relative phase of the audio tone at the receiving sites, and the phase difference measurement then determines the range difference.

The tested tone phase TOA trilateration methods used 2.7 kHz and approximately 18 kHz frequencies whose phase patterns repeat at 111 km and 16 km, respectively. These AVM systems have been termed narrow-band (Fig. 1-24) and wide-band (Fig. 1-25) since the first can be accommodated in a narrow-band FM voice channel (25 kHz) while the second requires eight times the bandwidth or four adjacent channels (100 kHz). In comparison, the pulse TOA method (Fig. 1-26) utilizes up to 10 MHz of bandwidth to preserve the leading edge of the pulse.

Another wide-band trilateration method is based on interferometer techniques. As currently envisaged, each vehicle would transmit a carrier signal modulated with either white or P-N sequence noise (Fig. 1-27). These signals would again be received at the several sites, and by correlation computation the time differences of arrival would be established. Since only the signals from one vehicle would show substantial correlation, it would be possible but not necessary to have all vehicles broadcasting the noise modulated signals simultaneously. The effects of multipath on trilateration techniques have been analyzed and modeled by George Turin (Ref. 5).

2. Triangulation Systems. The direction finding methods proposed would measure the azimuth angle of the vehicle signal at several fixed sites (Fig. 1-28). The intersection of the extension of these bearing angles would be the position of the vehicle. Multipath in this method would probably cause uncertainty in the angle of arrival of the vehicle signal leading to

approximately the same accuracy limitations as those for trilateration. Of the Class III AVM systems delineated, the direction finding and narrow-band phase TOA would allow the use of the normal vehicle transceiver. The pulse, wide-band phase, and noise modulation TOA methods would require an additional AVM transmitter.

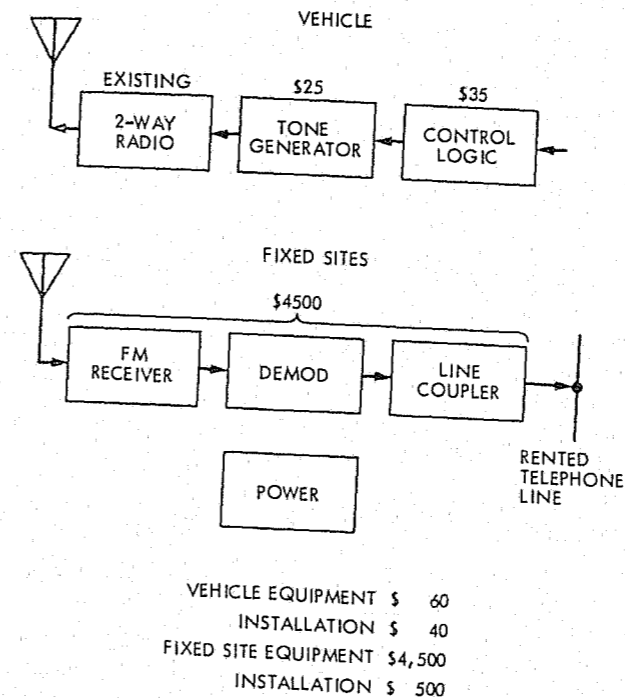


Fig. 1-24. Class III AVM Narrow-Band FM Phase TOA Trilateration

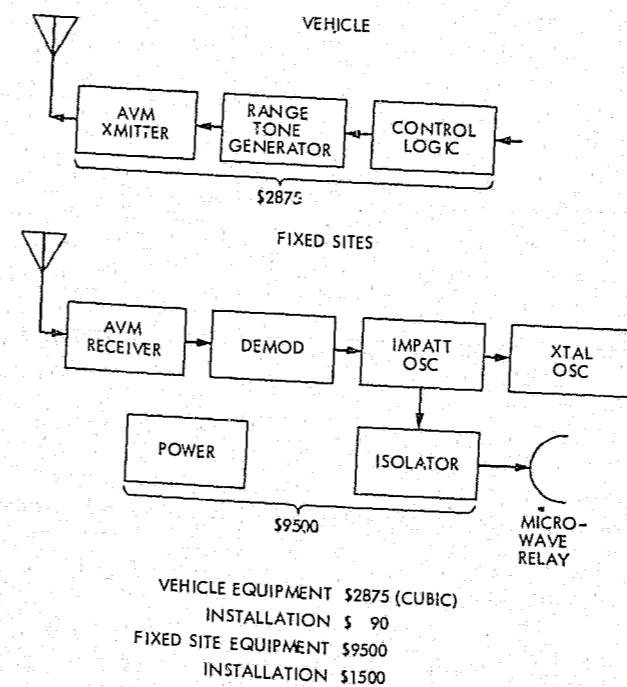


Fig. 1-25. Class III AVM Wide-Band FM Phase TOA Trilateration

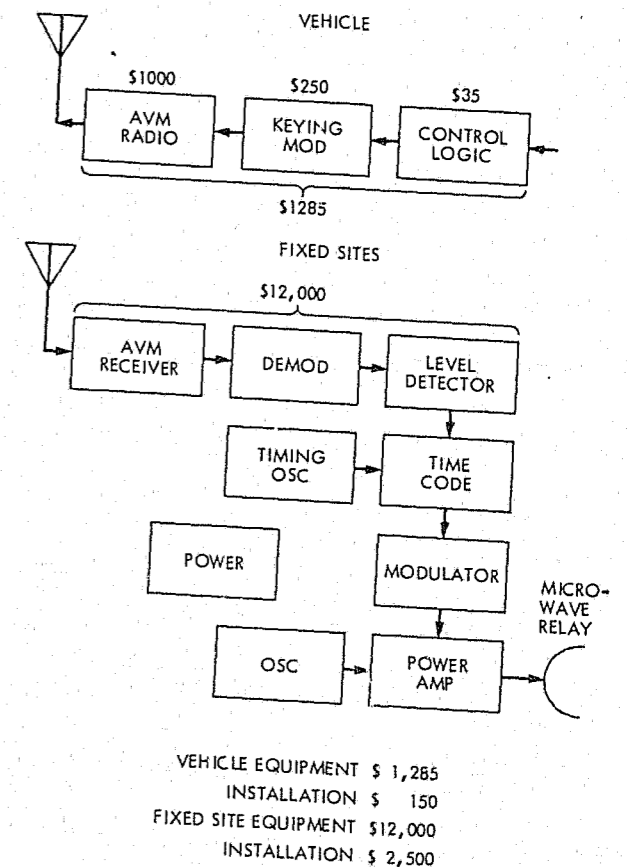


Fig. 1-26. Class III AVM Pulse TOA Fixed Site Trilateration

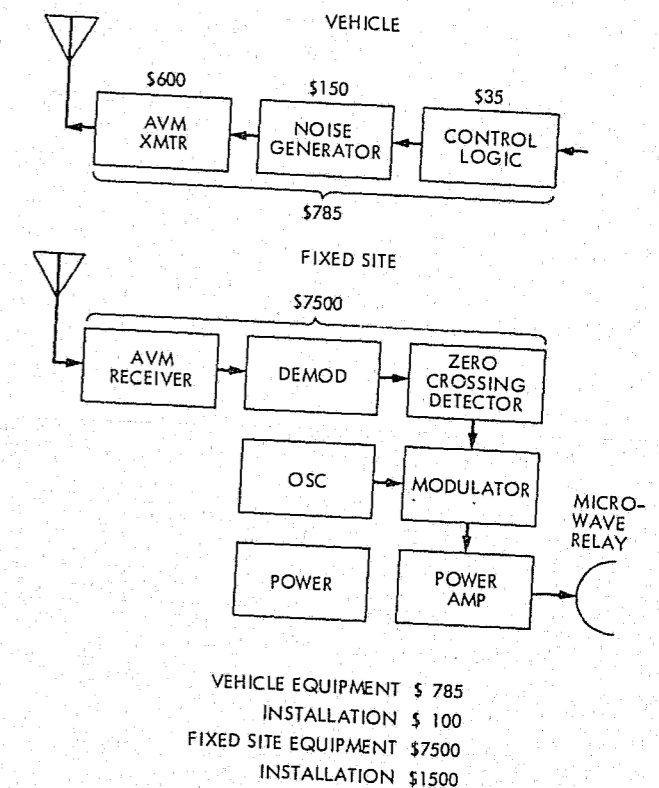


Fig. 1-27. Class III AVM Noise Correlation TOA Trilateration



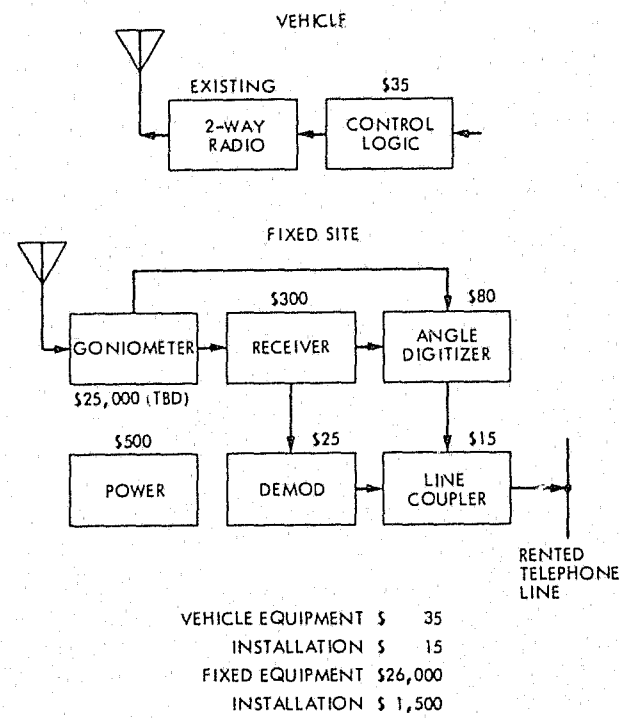


Fig. 1-28. Class III AVM Direction Finding from Special RF Sites

E. Class IV AVM, Monitored Signposts Throughout Urban Area

This class of AVM techniques is an inversion of the Class II autonomous wayside or buried signposts and removes the data collection link responsibility from the vehicle. In Class IV AVM, a vehicle-to-signpost link (Fig. 1-29) is maintained, but the information flow is the vehicle's identity to the monitored signpost. The data link to the base station or central collection point is based either on telephone lines rented from the local utility or on call-box lines for police and fire use. Since individual lines from each signpost are usually not considered economically practical, it is usually proposed to group the signposts on "party lines". The "party line" approach requires that each signpost not only transmit the vehicle ID data received but also identify itself to the central collection point at the base station. The telephone line is an additional complication to the Class IV installation, and a prime power connection is still required.

A technique of using the buried loop-sensors, which actuate traffic signals, as receiving antennas (Fig. 1-30) can be used in the monitored Class IV as in the autonomous Class II signpost method. This is an especially attractive approach if the signals are centrally controlled because dedicated communication lines are usually already installed. Ultrasonic as well as photo/IR detectors could also be used on monitored signposts (Figs. 1-31, 1-32).

In Class IV, the vehicle polling function is replaced either by line-finding, as is used in normal telephone service, or by a continual scanning of the lines to find an "off hook" indication that a signpost on one of the party lines has information to forward.

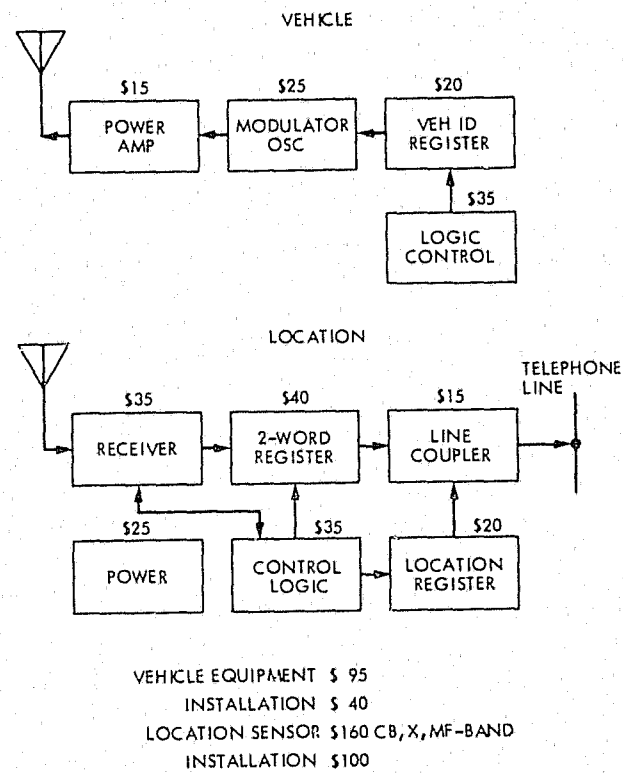


Fig. 1-29. Class IV AVM Monitored Wayside Radio Receivers

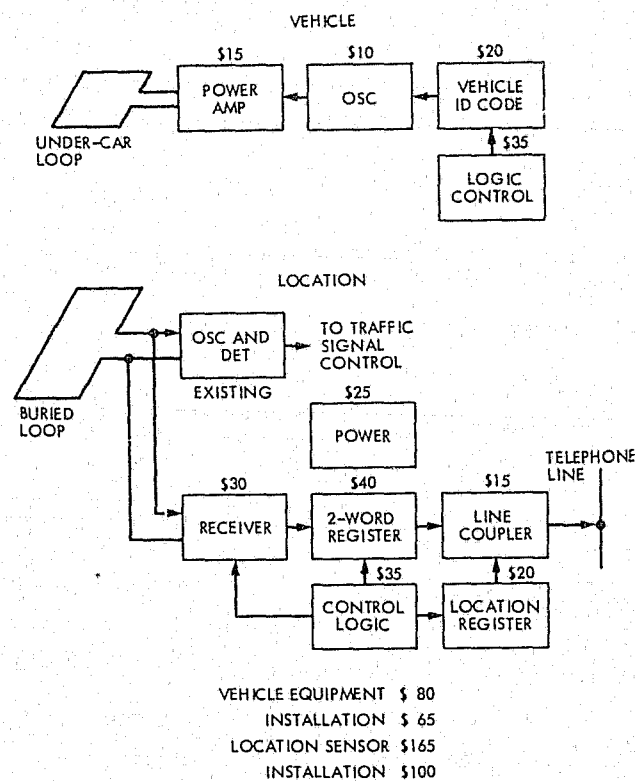


Fig. 1-30. Class IV AVM Monitored Traffic Presence Sensors

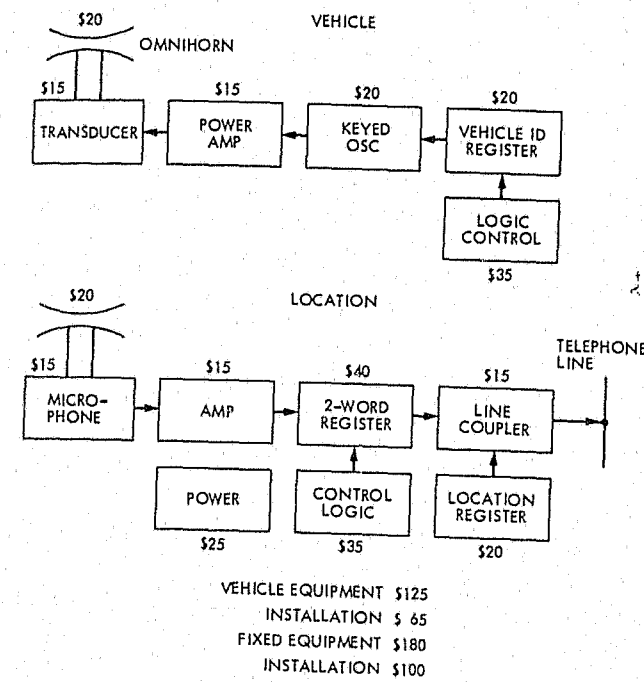


Fig. 1-31. Class IV AVM Monitored Ultrasonic Wave Receptors

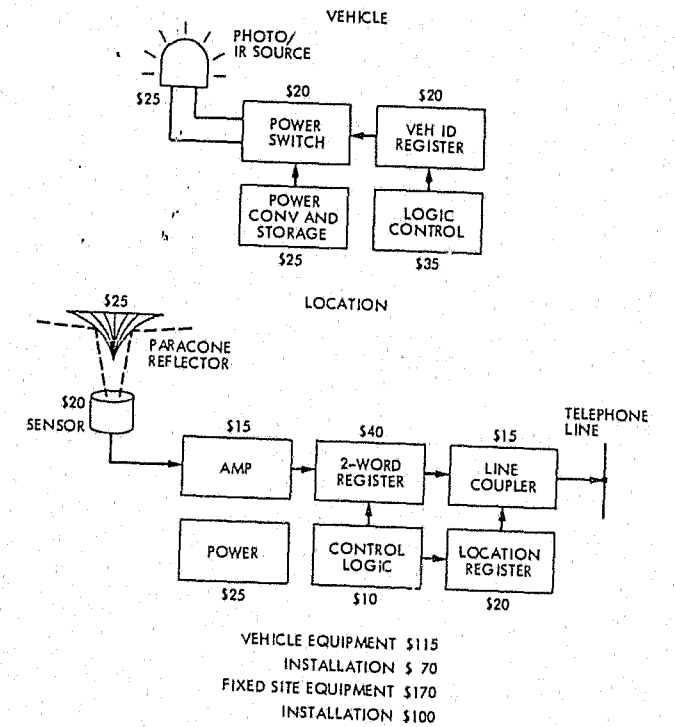


Fig. 1-32. Class IV AVM Monitored Photo or IR Detectors





Table 1-6. Location Performance Parameters for All AVM Classes and Systems

Technique	Accuracy or Radius	Value used, (m)	Location Data, bits or BW	Fix Time, sec
<b>CLASS I AVM</b>				
	Accuracy			
Keyboard update	10-100 m	(33)	6-20 bits	2-5 s
Stylus map update	30 m	(30)	14-20	3
2-Accelerometers	2% dist	(34)	14	0.3
Laser velocimtr	0.5% dist	(13)	16	0.3
Ultrasonic velo	3% dist	(40)	14	0.3
Compass/odometer	1% dist	(20)	14	0.3
Compass/laser vel	0.6% dist	(15)	14	0.3
Cmpss/u-sonic vel	0.8% dist	(17)	14	0.3
OMEGA navigation	1600 m	(1600)	27	3-10
LORAN navigation	0.4 m/km	(160)	32	0.06-.2
DECCA navigation	0.5 m/km	(200)	30	0
AM-Stations nav	150-250 m	(200)	12	0-3
Diff OMEGA nav	160 m	(160)	27	3-10
Diff LORAN nav	120-400 m	(400)	32	0.06-.2
Diff AM-Stations	150-250 m	(250)	21-32	0-3
Relay OMEGA nav	200-600 m	(500)	3 kHz BW	3-10
Relay LORAN nav	800 m	(800)	10 kHz BW	0.06-.2
<b>CLASS II AVM</b>				
	Radius m			
Buried res loops	10	---	10-18 bits	1-2 s
Reflecting signs	10	---	10-18	1-2
Reflecting road	3	---	10-18	1-2
X-Band signposts	12-100	---	9-17	1-2
HF, VHF signpost	15-100	---	7-15	2-5
LF Signposts	100	---	9-17	1-2
Light/IR post	30	---	9-17	1-2
Buried magnets	10	---	10-18	1-2
Ultrasonic post	20	---	9-17	1-2
Traffic sensor	10	---	10-18	1-2
<b>CLASS III AVM</b>				
	Accuracy			
Nar-band FM phase	800-1300 m	(1000)	3 kHz BW	0.015 s
Wid-band FM phase	1000-1500	(1200)	15-40 kHz	0.01
Pulse T-O-Arrival	100 m	(100)	10 MHz	0.0001
Noise correlation	100 m	(100)	5-10 MHz	0.001
Direction finder	3% dist	(700)	3 kHz	0.2-1
<b>CLASS IV AVM</b>				
	Radius, m			
Traffic loops	10	---	N/A	1-2 s
Wayside radio	100	---	N/A	1-2
Photo/IR detect	30	---	N/A	1-2
Ultrasonic detect	20	---	N/A	1-2

Table 1-7. Model City Parameters That Affect AVM Costs

Parameter	Small	Medium	Large
Area, km <sup>2</sup>	10	100	1000
Dimensions, km	2.2 x 4.5	7.1 x 14.2	22.3 x 44.7
Vehicles, patrol/total	5/10	50/100	500/1000
Intersections*	350	3500	35000
Road segments x lanes	1600	16800	168000
Road distance, km	125	1245	12450
Telephone lines, km	83	828	8275
Population	30,000	300,000	3,000,000

\*Based on 25/75% ratio of 50/30 blocks/km<sup>2</sup> in the urban area.

5. Intersections. The number of intersections in each city is based on two business area street densities. They are based on actual measurements of randomly selected areas of the UGAC cities, and the values assumed are 30/km<sup>2</sup> for 75% of the area and 50/km<sup>2</sup> for 25% of the area.

6. Road distance. For the purposes of the models, the blocks are assumed to have the same aspect ratio as the city, namely 2:1, and to be in a regular array. An average of 2.4 lanes for each road segment was assumed, based on UGAC city averages.

7. Telephone line distance. Class IV AVM systems require land line monitoring; and for the purposes of comparison, an equal division of sensors is assumed of up to a maximum of 100 sensors for each phone "party" line. These party lines are assumed to parallel the long street, so that the total mileage of lines is about two-thirds of the total road distance.

8. Building distribution and topography. A uniform low-rise building distribution is assumed for location accuracy comparison purposes. The topography of the model cities is assumed to be essentially flat without "blind" radio areas or special areas that might unduly affect any particular technique.

9. Radio. The only information sent from the vehicle in this comparison is that required for location, either as a binary message or equivalent RF bandwidth for the Class I, II, and III systems. Radio modifications are also assumed to enable automatic message transmission. Additionally, transmitter turn-on stabilization time, squelch delay, and antenna transfer are assumed constant at several values.

10. Model city AVM cost and performance summaries. Tables 1-8 through 1-16 summarize the AVM system costs in each of three model cities, small, medium, and large, for each of thirty six location techniques and for three polling methods.

a. Small city summary. The costs of all AVM techniques in the small city model are dominated by the operation-and-maintenance (O-M) cost with the result that there is a great similarity in total costs regardless of the vehicle location technique. The Class II and IV system costs are higher because the signposts and the associated costs are relatively greater than the vehicle costs (see Tables 1-8, 1-9, 1-10).

b. Medium city summary. The costs of AVM Class I in the medium city model show an increase which is almost all due to vehicular equipment. The Class II costs increase by a greater factor due again to signposts. The site costs of the buried resonant loops are substantially higher than those of any other Class II technique because of installation costs. The more sparsely distributed RF posts, either HF or VHF, do not impact the total cost to the extent of the techniques which use a post at each intersection. In the Class III techniques that require pulse or wideband equipment, the vehicular equipment accounts for about one-third the total cost.

In Class IV techniques, the telephone line rental which is included in the site cost is the primary cost factor (see Tables 1-11, 1-12, 1-13).

c. Large city summary. The AVM costs in the large model city show the same trend with Class II techniques (save for two exceptions) costing some 2 to 4 times the Class I techniques and about twice the cost of Class III systems. The Class II techniques systems costs are reducible by less dense placement of posts (see Tables 1-14, 1-15, 1-16).

The method of vehicle polling has only a slight impact on AVM system costs in any of the techniques in any of the model cities. Applications of the AVM cost analysis to actual cities in Southern California are presented in Part Two of this Report (p. 2-1).

B. Small Model City AVM Cost Summary Tables

Table 1-8. Small Model City Parameters Used in AVM Cost Analysis

- AREA IS 4 SQUARE MILES.
- EAST WEST DISTANCE IS 1.4 MILES.
- NORTH SOUTH DISTANCE IS 2.8 MILES.
- TOTAL ROAD MILEAGE IS 77 MILES.
- THE NUMBER OF INTERSECTIONS IS 3500.
- THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 700.
- THERE ARE 10 CARS IN THE FLEET
- AND THERE ARE 0 MOTORCYCLES.
- THE NUMBER OF VEHICLES ON EACH SHIFT IS:

  - FIRST SHIFT MAX. 5
  - FIRST SHIFT MIN. 5
  - SECOND SHIFT MAX. 5
  - SECOND SHIFT MIN. 5
  - THIRD SHIFT MAX. 5
  - THIRD SHIFT MIN. 5

- THE CITY WOULD REQUIRE 4 WIDE-BAND OR PULSE T-O-A ANTENNA SITES AND 6 NARROW BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADII.

Table 1-9. Small Model City AVM Cost Summary

Table with columns: TECHNIQUE, CARS, THOUSANDS OF \$, and TOTAL. Rows include: KEYBOARD, STATUS MAP, SMOKELEPHONETER, LASER HELIOLITH, ULTRASONIC DETECT, COMPASS GONIOMETER, COMPASS LASER MEL, COMPASS U-SONIC MEL, OREGON, LORAN, DIFF. OREGON, DIFF. LORAN, DIFF. HI-STRA, RELAY OREGON, RELAY LORAN, CLASS II, BURIED PEG. LOOPS, REFLECTING SIGNS, REFLECTING ROAD, ROAD POST, HI-WAY POST, LIGHT I-R POST, BURIED MAGNETS, ULTRASONIC FOOT, TRAFFIC SENSOR, CLASS III, WID-BAND FM PHASE, MID-BAND FM PHASE, PULSE T-O-RAPPROX, NOISE CORRELATION, DIRECTION FINDER, CLASS IV, TRAFFIC LOOPS, MIDSIDE RADIO, PHOTO I-P DETECT, ULTRASONIC DETECT.

Table 1-10. Small City Vehicle Polling

C. Medium Model City AVM Cost Summary Tables

Table 1-11. Medium Model City Parameters Used in AVM Cost Analysis

- AREA IS 40 SQUARE MILES.
EAST WEST DISTANCE IS 4.41 MILES.
NORTH SOUTH DISTANCE IS 8.2 MILES.
TOTAL ROAD MILEAGE IS 774 MILES.
THE NUMBER OF INTERSECTIONS IS 3500.
THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 7000.
THERE ARE 100 CARS IN THE FLEET.
AND THERE ARE 0 MOTORCYCLES.
THE NUMBER OF VEHICLES ON EACH SHIFT IS:
FIRST SHIFT MAX. 50
FIRST SHIFT MIN. 50
SECOND SHIFT MAX. 50
SECOND SHIFT MIN. 50
THIRD SHIFT MAX. 50
THIRD SHIFT MIN. 50

- THE CITY WOULD REQUIRE 5 WIDE-BAND OR PULSE T-O-R ANTENNA SITES AND 10 NARROW BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADII.

Table 1-12. Medium Model City AVM Cost Summary

Table with columns: TECHNIQUE, CARS, THOUSANDS OF \$, and TOTAL. Rows include: KEYBOARD, STATUS MAP, SMOKELEPHONETER, LASER HELIOLITH, ULTRASONIC DETECT, COMPASS GONIOMETER, COMPASS LASER MEL, COMPASS U-SONIC MEL, OREGON, LORAN, DIFF. OREGON, DIFF. LORAN, DIFF. HI-STRA, RELAY OREGON, RELAY LORAN, CLASS II, BURIED PEG. LOOPS, REFLECTING SIGNS, REFLECTING ROAD, ROAD POST, HI-WAY POST, LIGHT I-R POST, BURIED MAGNETS, ULTRASONIC FOOT, TRAFFIC SENSOR, CLASS III, WID-BAND FM PHASE, MID-BAND FM PHASE, PULSE T-O-RAPPROX, NOISE CORRELATION, DIRECTION FINDER, CLASS IV, TRAFFIC LOOPS, MIDSIDE RADIO, PHOTO I-P DETECT, ULTRASONIC DETECT.

Table 1-13. Medium City Vehicle Polling

Table with columns: TECHNIQUE, CARS, THOUSANDS OF \$, and TOTAL. Rows include: KEYBOARD, STATUS MAP, SMOKELEPHONETER, LASER HELIOLITH, ULTRASONIC DETECT, COMPASS GONIOMETER, COMPASS LASER MEL, COMPASS U-SONIC MEL, OREGON, LORAN, DIFF. OREGON, DIFF. LORAN, DIFF. HI-STRA, RELAY OREGON, RELAY LORAN, CLASS II, BURIED PEG. LOOPS, REFLECTING SIGNS, REFLECTING ROAD, ROAD POST, HI-WAY POST, LIGHT I-R POST, BURIED MAGNETS, ULTRASONIC FOOT, TRAFFIC SENSOR, CLASS III, WID-BAND FM PHASE, MID-BAND FM PHASE, PULSE T-O-RAPPROX, NOISE CORRELATION, DIRECTION FINDER, CLASS IV, TRAFFIC LOOPS, MIDSIDE RADIO, PHOTO I-P DETECT, ULTRASONIC DETECT.

D. Large Model City AVM Cost Summary Tables

Table 1-14. Large Model City Parameters Used in AVM Cost Analysis

- AREA IS 600 SQUARE MILES.
EAST WEST DISTANCE IS 13.9 MILES.
NORTH SOUTH DISTANCE IS 27.8 MILES.
TOTAL ROAD MILEAGE IS 7736 MILES.
THE NUMBER OF INTERSECTIONS IS 35000.
THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 70000.
THERE ARE 1000 CARS IN THE FLEET.
AND THERE ARE 0 MOTORCYCLES.
THE NUMBER OF VEHICLES ON EACH SHIFT IS:
FIRST SHIFT MAX. 500
FIRST SHIFT MIN. 500
SECOND SHIFT MAX. 500
SECOND SHIFT MIN. 500
THIRD SHIFT MAX. 500
THIRD SHIFT MIN. 500

Table 1-14. Large Model City Parameters Used in AVM Cost Analysis (Cont'd)

- THE CITY WOULD REQUIRE 29 WIDE-BAND OR PULSE T-O-R ANTENNA SITES AND 106 NARROW BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADII.

Table 1-15. Large Model City AVM Cost Summary

Table with columns: TECHNIQUE, CARS, THOUSANDS OF \$, and TOTAL. Rows include: KEYBOARD, STATUS MAP, SMOKELEPHONETER, LASER HELIOLITH, ULTRASONIC DETECT, COMPASS GONIOMETER, COMPASS LASER MEL, COMPASS U-SONIC MEL, OREGON, LORAN, DIFF. OREGON, DIFF. LORAN, DIFF. HI-STRA, RELAY OREGON, RELAY LORAN, CLASS II, BURIED PEG. LOOPS, REFLECTING SIGNS, REFLECTING ROAD, ROAD POST, HI-WAY POST, LIGHT I-R POST, BURIED MAGNETS, ULTRASONIC FOOT, TRAFFIC SENSOR, CLASS III, WID-BAND FM PHASE, MID-BAND FM PHASE, PULSE T-O-RAPPROX, NOISE CORRELATION, DIRECTION FINDER, CLASS IV, TRAFFIC LOOPS, MIDSIDE RADIO, PHOTO I-P DETECT, ULTRASONIC DETECT.

Table 1-16. Large City Vehicle Polling

Table with columns: TECHNIQUE, CARS, THOUSANDS OF \$, and TOTAL. Rows include: KEYBOARD, STATUS MAP, SMOKELEPHONETER, LASER HELIOLITH, ULTRASONIC DETECT, COMPASS GONIOMETER, COMPASS LASER MEL, COMPASS U-SONIC MEL, OREGON, LORAN, DIFF. OREGON, DIFF. LORAN, DIFF. HI-STRA, RELAY OREGON, RELAY LORAN, CLASS II, BURIED PEG. LOOPS, REFLECTING SIGNS, REFLECTING ROAD, ROAD POST, HI-WAY POST, LIGHT I-R POST, BURIED MAGNETS, ULTRASONIC FOOT, TRAFFIC SENSOR, CLASS III, WID-BAND FM PHASE, MID-BAND FM PHASE, PULSE T-O-RAPPROX, NOISE CORRELATION, DIRECTION FINDER, CLASS IV, TRAFFIC LOOPS, MIDSIDE RADIO, PHOTO I-P DETECT, ULTRASONIC DETECT.

#### IV. AVM SYSTEM ACCURACIES AND COST BENEFITS

##### A. System Parameters That Affect AVM Costs

The prediction of the expected accuracies of AVM systems is essentially a probabilistic problem. Actually there are two distinct problems, one a precursor to the other, depending on the class of AVM system. Classes I and III are loosely referred to as "random route" systems because the techniques have the capability of vehicle location anywhere within their surveillance areas. Classes II and IV are called "fixed route" systems because the location capability exists only in the vicinities of signposts that are distributed along the wayside or on the roadway at intersections within the covered area. Besides the inherent range of uncertainty in the location measurements provided by individual AVM techniques, Classes I and III are subject to another location error, which is the shift in the moving vehicle's position during the interval between the instant of polling and the display of location data at the base. On the other hand, Class II and IV techniques provide location information only at the time when the vehicle passes within the sensing radius of a wayside or buoied signpost. This information is the best available until the time that the vehicle enters the sensing radius of another signpost. A measure of this uncertainty in location is required to determine the "inherent" accuracy of the signpost AVM techniques. This is particularly true when the signposts are less than maximally dense; that is, when the signposts are placed two or more intersections apart.

It is intuitively reasoned that if the signpost sensors in Classes II and IV are placed at each intersection, then the location of any vehicle can be found to plus-or-minus one block. It also follows that if the sensors are placed in a diamond pattern at every other block in each direction, then the accuracy is plus-or-minus two blocks. This reasoning is valid only if every passage through instrumented intersections by all vehicles is known. If the polling technique or RF channel loading is such that this data frequency cannot be assured, then the achievable accuracy is not as well known. A tutorial treatment of the less dense signpost placement by Markov, or random-walk, processes is included in Part Three of this Report. The analysis technique leads to a prediction of the mean and variance of the distance traveled by a vehicle starting at an unsensed intersection before it passes a sensed intersection. The results of this technique for various signpost densities are as follows:

Ratio (Sensed/Unsensed)	Mean	Variance
1/1	1	1
3/8	1.778	1.778
3/9	2	2

The second approach to the system accuracy prediction considers not only the inherent error in the vehicle location technique but also the additional inaccuracies introduced by the delays in

successive pollings of the vehicles and by the computation of location when the vehicles in the fleet are moving at various speeds. In Part Three of this Report, the analysis, the method of solution, and the tabular results are presented.

The technique for predicting the location accuracy was used to generate the family of curves in Fig. 1-36. These contours of system accuracy correlate the independent variables of the polling interval and the standard deviation of the inherent error. The accuracy contour yields the 95% confidence interval for vehicle fleets that move with an exponential velocity distribution such that more than half the vehicles are moving at speeds less than 15 mph (6.67 m/s). It can be seen from the curves that either the polling interval or the inherent error can quickly dominate the achievable system accuracy if either is very large. The curves are shown for the system accuracy interval of 100 to 1000 meters (0.1 to 0.6 mile). The curves for less than 100 and greater than 1000 meters are repetitions of those shown and can be derived with subtraction or addition of a unit constant on both axes (equivalent to division or multiplication of the interval or deviation by a factor of 10).

##### B. Estimated Cost Savings Based on Urban Parameters

1. System accuracy estimation. The accuracy to be expected from any given AVM system in a locality is estimated by a step-by-step process. First, from the data provided for the particular city, the maximum and minimum number of vehicles deployed is obtained. Next, the number of bits in the location message required from each vehicle for each technique is determined. The time required to poll the deployed vehicles with a 0.1-sec radio turn-on time is then computed for the redundant mode of the random polling process. This value yields very conservative (or pessimistic) polling intervals for the two values of vehicles deployed. These intervals together with the value obtained from the table of technique accuracies provide the entries to the graph of system accuracies. These curves are prestored in the computer program. A rather simple linear interpolation program yields a maximum and minimum estimation of the 95% confidence level of system accuracy for the maximum and minimum vehicle deployments. The location accuracies used are usually greater than the standard deviation value.

2. Vehicles saved estimation. Based on the prior work of Larson (Ref. 2), Knickel (Ref. 3), and Doering (Ref. 4), a quantitative measure of efficiency increase in responding to calls for service should be determinable from the accuracy of the AVM system. One of the approaches to this problem is to compare a situation where, in response to a call for service, the dispatcher always sends the vehicle responsible for a beat to that where the location of the vehicles is known and the "closest" vehicle is dispatched to the scene.

The efficiency comparison is made either in the excess time required or the excess distance travelled by the beat vehicles relative to the closest located vehicles. The conclusions of this approach are generally that a vehicle location accuracy of about 1/5 the beat-side dimension is

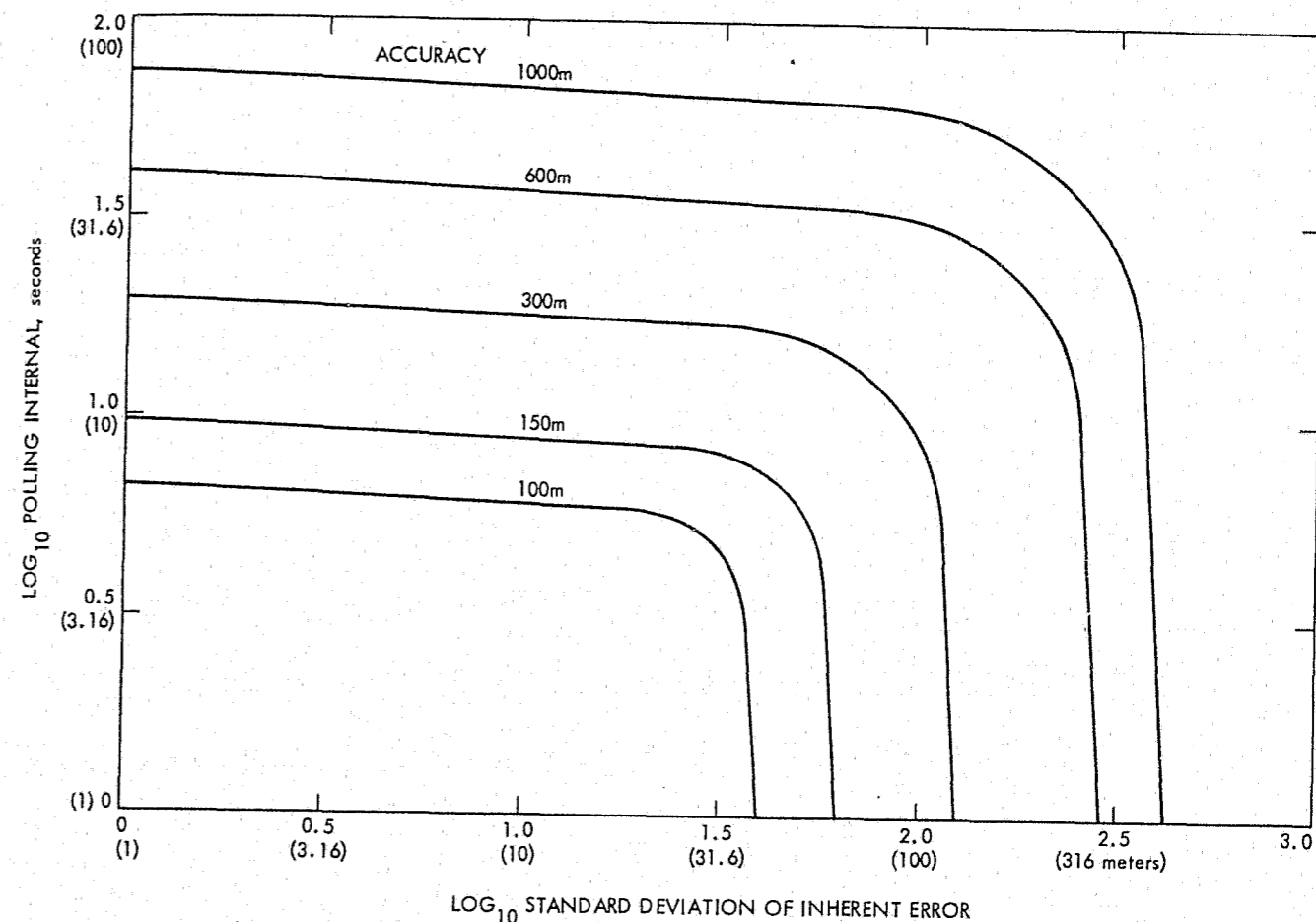


Fig. 1-36. Vehicle Polling Intervals vs 95% AVM System Accuracy

sufficient. Additionally the service improvement is found to be about 7% for the locator system dispatches versus the "center of mass" or beat vehicle dispatches.

The more recent study of Doering (Ref. 4), however, compares response time performance in a situation with differing absolute accuracy values of the AVM system and a given fleet size with the number of vehicles required to provide the same response time with no AVM. Doering's study indicated that, in the area studied (the city of Orlando, Florida), 34 vehicles in the AVM fleet where the accuracy is 240 meters (800 ft) would provide a response time which would require 35.8 vehicles in a non-AVM fleet. Extrapolation of the curves presented by Doering indicates that 8 to 10% fewer vehicles in an AVM system fleet with perfect (0 feet) accuracy can provide the same response performance as the larger number of vehicles in a non-AVM fleet. Extrapolation in the direction of less accurately known location, indicates that there is little improvement in response time with location accuracies of 450 meters (1500 ft) or more. It may be coincidental that this value is about 0.3 km (0.2 mile), which is 1/5 the average beat side dimension in the Orlando simulation studies. A plot of the increase required in a non-AVM vehicle fleet to equal AVM vehicles response time performance versus accuracy shows a linearly decreasing value as the AVM accuracy decreases.

For the purposes of this study, a 7% increase in efficiency is assumed for a perfect AVM system, with the percentage decreasing linearly to zero at an AVM accuracy of 0.2 times the average beat side length. The average beat is calculated by dividing the area by the number of vehicles deployed.

For maximum and minimum deployments, the efficiency increase assumption yields different values for the same AVM technique accuracy. In cases where the minimum deployment is substantially lower than the maximum, the apparent beat size may be increased to the point where an AVM technique which yields no efficiency increase with maximum deployment may display a marked improvement in response. Additionally, the minimum deployment decreases the polling time interval which provides an additional improvement in system accuracy.

The calculation of cars saved is based on a reasonable reciprocity assumption that fewer cars with AVM can yield the same performance as that obtained now with a given fleet size. The number of cars saved is determined by multiplying the percentage efficiency value, obtained from the beat dimension and system accuracy, by the number of vehicles deployed. Savings of less than one vehicle are allowed by the calculation. As stated before, the factors tending to increase efficiency are such that, in some cases, the number of cars

served with minimum deployment exceeds that for maximum deployment with a given technique.

3. Estimated 5-year cost saving. The 5-year saving calculation, presented in Tables 1-17 through 1-20 is an attempt to place a dollar value on the efficiency increase which might in turn indicate possible choices of candidate AVM systems. The calculation assumes that each car saved is worth \$150,000 annually, which is primarily salaries and overhead (as of 1974). This is an average value for a 1-man car based on 5 salaries and 100% overhead. The saving for small, medium, and large cities is a straightforward multiplication of the maximum of the cars saved times the annual value of the car minus the O-M costs of the AVM technique. The value

Table 1-17. Small Model City Cost Benefits from AVM System Usage

AVM TECHNIQUE	VEHICLES SAVED PER YEAR	ESTIMATED ANNUAL SAVINGS (\$)	AVM COST PER YEAR (\$)	NET ANNUAL SAVINGS (\$)
TECHNIQUE I	1000	150000	10000	140000
TECHNIQUE II	1000	150000	15000	135000
TECHNIQUE III	1000	150000	20000	130000
TECHNIQUE IV	1000	150000	25000	125000
TECHNIQUE V	1000	150000	30000	120000
TECHNIQUE VI	1000	150000	35000	115000
TECHNIQUE VII	1000	150000	40000	110000
TECHNIQUE VIII	1000	150000	45000	105000
TECHNIQUE IX	1000	150000	50000	100000
TECHNIQUE X	1000	150000	55000	95000
TECHNIQUE XI	1000	150000	60000	90000
TECHNIQUE XII	1000	150000	65000	85000
TECHNIQUE XIII	1000	150000	70000	80000
TECHNIQUE XIV	1000	150000	75000	75000
TECHNIQUE XV	1000	150000	80000	70000
TECHNIQUE XVI	1000	150000	85000	65000
TECHNIQUE XVII	1000	150000	90000	60000
TECHNIQUE XVIII	1000	150000	95000	55000
TECHNIQUE XIX	1000	150000	100000	50000
TECHNIQUE XX	1000	150000	105000	45000

Table 1-18. Medium Model City Cost Benefits from AVM System Usage

AVM TECHNIQUE	VEHICLES SAVED PER YEAR	ESTIMATED ANNUAL SAVINGS (\$)	AVM COST PER YEAR (\$)	NET ANNUAL SAVINGS (\$)
TECHNIQUE I	2000	300000	20000	280000
TECHNIQUE II	2000	300000	30000	270000
TECHNIQUE III	2000	300000	40000	260000
TECHNIQUE IV	2000	300000	50000	250000
TECHNIQUE V	2000	300000	60000	240000
TECHNIQUE VI	2000	300000	70000	230000
TECHNIQUE VII	2000	300000	80000	220000
TECHNIQUE VIII	2000	300000	90000	210000
TECHNIQUE IX	2000	300000	100000	200000
TECHNIQUE X	2000	300000	110000	190000
TECHNIQUE XI	2000	300000	120000	180000
TECHNIQUE XII	2000	300000	130000	170000
TECHNIQUE XIII	2000	300000	140000	160000
TECHNIQUE XIV	2000	300000	150000	150000
TECHNIQUE XV	2000	300000	160000	140000
TECHNIQUE XVI	2000	300000	170000	130000
TECHNIQUE XVII	2000	300000	180000	120000
TECHNIQUE XVIII	2000	300000	190000	110000
TECHNIQUE XIX	2000	300000	200000	100000
TECHNIQUE XX	2000	300000	210000	90000

obtained is then multiplied by 5 years for the total saving.

The 5-year saving is positive only if the value of the car saving exceeds the annual O-M cost. The calculation is performed for a given technique only if a car saving is indicated, and the result is presented regardless of sign. No calculation is performed if no car saving is indicated.

A simple summation of savings rather than a present worth of an annuity calculation is justified on the basis that it is less speculative and might be more nearly correct if salaries rise at a percentage rate which exceeds the rate of return that can be realized on 5-year municipal investments. The 5-year saving estimation is presented solely for AVM system comparison purposes.

Table 1-19. Large Model City Cost Benefits from AVM Systems Using One RF Channel

AVM TECHNIQUE	VEHICLES SAVED PER YEAR	ESTIMATED ANNUAL SAVINGS (\$)	AVM COST PER YEAR (\$)	NET ANNUAL SAVINGS (\$)
TECHNIQUE I	5000	750000	30000	720000
TECHNIQUE II	5000	750000	45000	690000
TECHNIQUE III	5000	750000	60000	660000
TECHNIQUE IV	5000	750000	75000	630000
TECHNIQUE V	5000	750000	90000	600000
TECHNIQUE VI	5000	750000	105000	570000
TECHNIQUE VII	5000	750000	120000	540000
TECHNIQUE VIII	5000	750000	135000	510000
TECHNIQUE IX	5000	750000	150000	480000
TECHNIQUE X	5000	750000	165000	450000
TECHNIQUE XI	5000	750000	180000	420000
TECHNIQUE XII	5000	750000	195000	390000
TECHNIQUE XIII	5000	750000	210000	360000
TECHNIQUE XIV	5000	750000	225000	330000
TECHNIQUE XV	5000	750000	240000	300000
TECHNIQUE XVI	5000	750000	255000	270000
TECHNIQUE XVII	5000	750000	270000	240000
TECHNIQUE XVIII	5000	750000	285000	210000
TECHNIQUE XIX	5000	750000	300000	180000
TECHNIQUE XX	5000	750000	315000	150000

Table 1-20. Large Model City Cost Benefits from AVM Systems Using Two RF Channels

AVM TECHNIQUE	VEHICLES SAVED PER YEAR	ESTIMATED ANNUAL SAVINGS (\$)	AVM COST PER YEAR (\$)	NET ANNUAL SAVINGS (\$)
TECHNIQUE I	10000	1500000	60000	1440000
TECHNIQUE II	10000	1500000	90000	1410000
TECHNIQUE III	10000	1500000	120000	1380000
TECHNIQUE IV	10000	1500000	150000	1350000
TECHNIQUE V	10000	1500000	180000	1320000
TECHNIQUE VI	10000	1500000	210000	1290000
TECHNIQUE VII	10000	1500000	240000	1260000
TECHNIQUE VIII	10000	1500000	270000	1230000
TECHNIQUE IX	10000	1500000	300000	1200000
TECHNIQUE X	10000	1500000	330000	1170000
TECHNIQUE XI	10000	1500000	360000	1140000
TECHNIQUE XII	10000	1500000	390000	1110000
TECHNIQUE XIII	10000	1500000	420000	1080000
TECHNIQUE XIV	10000	1500000	450000	1050000
TECHNIQUE XV	10000	1500000	480000	1020000
TECHNIQUE XVI	10000	1500000	510000	990000
TECHNIQUE XVII	10000	1500000	540000	960000
TECHNIQUE XVIII	10000	1500000	570000	930000
TECHNIQUE XIX	10000	1500000	600000	900000
TECHNIQUE XX	10000	1500000	630000	870000

### V. COMPUTER PROGRAMS FOR ANALYSES OF AVM NEEDS

The cost estimates for the AVM techniques are in almost all cases precisely that - estimates as of 1974. They have the additional shortcoming that large-scale production is assumed, which accounts for the generally low system cost amounts. Therefore, additional studies are necessary to refine these estimates in view of the rapidly changing technology and costs.

Although the cost estimation procedure for AVM systems in model cities is a valid technique, it does not take into account the individual differences of real cities. That is, the system engineering aspect where the vagaries of a particular city and operational methodology are considered has not been included. The AVM system cost estimation and particularly the performance estimation and resultant estimated savings are essentially averaging processes. Since each city differs in details from each other city, and the AVM system cost, performance, and impact depend on these differences, final selection of an AVM system will require an individual analysis such as those presented in Part Two.

An individualized analysis for a particular city requires the two following steps: (1) Synthesis of AVM systems corresponding to each of the desired concepts as they would be configured for the physical, political, and cost environment of that city, and (2) evaluation of the effects of each of those systems. The process of synthesizing a particular AVM system is a straightforward but tedious task, requiring detailed technical knowledge that may not be readily available in real cities. It can be made easily available, however, by the development of an AVM system synthesis computer program, as is described later. The expected effects can then be assessed by using the resultant systems in a system simulation computer program, which is described in more detail in Section B. Since these two programs were planned to be developed in Phase One of this AVM Systems Study project, they do not yet exist.

#### A. AVM System Synthesis Computer Program

The synthesis program will be based on design algorithms, equations, cost estimates, and the AVM data base developed in Phase Zero of this Study. These program components include antenna siting algorithms for time-of-arrival systems, message length equations for different location technique and polling combinations, accuracy estimation equations for various reporting intervals or signpost densities, and life-cost equations. A preliminary concept of the basic elements of the AVM system synthesis computer program is shown in Figure 1-37. A concept of the operations sequence in using the synthesis program is presented in Table 1-21. Salient features of the synthesis program are listed in the following subsections.

1. City and fleet data for AVM System Synthesis Program. The synthesis program will first summarize the data provided from the input file. The purpose of this step is to provide the user with an opportunity to review the input before actually running the synthesis program. Table 1-22 lists some of the parameters that will be included in the data input summary.

Table 1-21. Operating Sequence of AVM System Synthesis Computer Program

- Step 1. The user will supply the values of those parameters that describe his particular city. Some of the data may be fairly extensive, for example, geocoding data or DIME file type information which describes the city street/block system in detail. For information of this type a computer-readable data file will be used. An auxiliary program, separate from the AVM system synthesis program, will be developed to facilitate the interactive development of the data file.
- Step 2. The synthesis program will read the data file and determine the AVM system configurations suited to the city. If any data is missing or incomplete, the program will indicate which systems cannot be evaluated and provide an opportunity to modify the data file.
- Step 3. The program will present basic comparison data for each system configuration option.
- Step 4. After selecting the viable configuration options, the program will shift to a "trade-off" or compromise mode in which the user can access further detail and investigate the options available within a particular choice of system concept.

Table 1-22. City and Fleet Input Data for AVM System Synthesis Program

City name: AAAAAAAAAAAAAAAAAAAAAAA  
 Area monitored: XX.X sq. miles  
 Maximum X and Y dimensions: XX.XX mi, by XX.XX miles  
 Street length: XXX.X miles  
 Number of intersections: NNNN  
 Number of road segments: NNNN  
 Number of vehicles instrumented: NNNN  
 Average number of vehicles each shift: NN, NN, NN  
 Number of beats per shift: NN, NN, NN  
 Shift hours: HH-HH, HH-HH, HH-HH  
 Number of dispatcher consoles: N  
 Utilization factor by shift: FF%, FF%, FF%  
 (This is the fraction of time available to respond to calls for service).  
 Average call for service time by shift: HH, HH, HH  
 RF channel utilization factor: P%, P%, P%  
 RF channel assigned: N Planned: N  
 LORAN coverage in area?: Y-N; DECCA?: Y-N  
 AM stations in area: K--, W--, K--, W--

2. AVM Configuration options for AVM System Synthesis. Each of the AVM options identified by the selection process will be described briefly in narrative form. Each will be tagged with an identity code for later use. Then for each of the applicable options, the following gross data will be presented for comparison:

- a. Cost estimates. Total system cost, present value, "\$XX XXX XXX (These figures

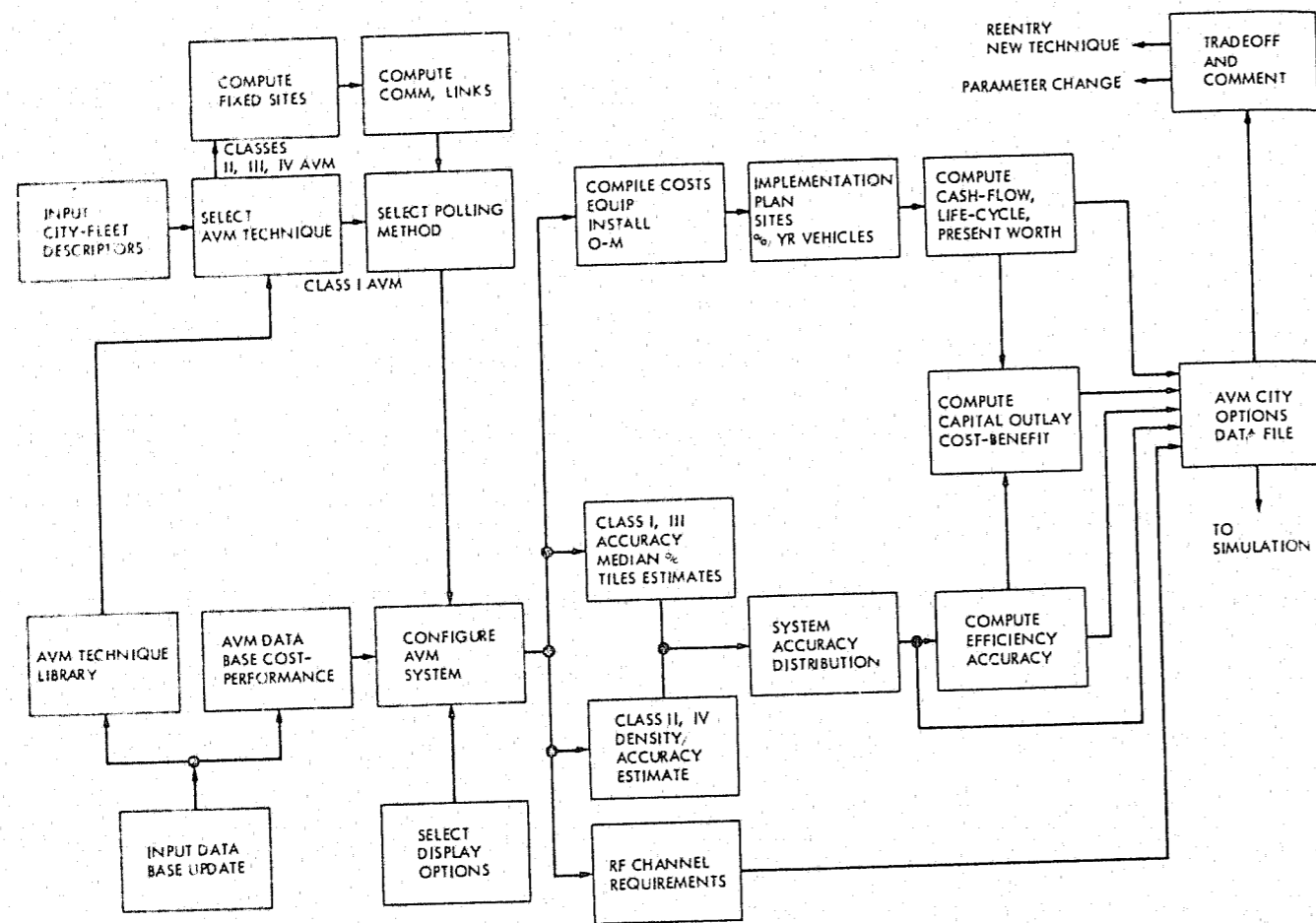


Figure 1-37. Concept for AVM System Synthesis Computer Program

will be for comparison purposes only. A breakdown follows:)

One-time costs	\$XX XXX XXX
(development, conversion, facilities)	
Installation costs	\$XX XXX XXX
Recurring costs	\$XXX XXX per year
(operations, maintenance, training)	
Replacement	\$XXX XXX per year
(equivalent annual payment at 10% year)	
Upgrading costs	
Display consoles	\$XXX XXX plus \$XX XXX per year (each)
Fixed sites	\$XXX XXX plus \$XX XXX per year (each)
Signposts	\$ XXX plus \$ XXX per year (each)
Vehicle equipment	\$ X XXX plus \$ XXX per year (each)
Telephone mileage	\$XXX XXX plus \$XXX XXX per year (each)

b. Resource utilization estimate.

Radio channels required: XX, X  
 Microwave or dedicated telephone lines needed: XXX  
 Computer memory estimate: XXX XXX bytes

c. Performance estimates.

Median location accuracy: XX ft  
 (effective polling rate = XX vehicles/second)

Fraction of fleet with error

less than \_\_\_\_\_ft: XX%  
 less than \_\_\_\_\_ft: XX%  
 less than \_\_\_\_\_ft: XX%

d. Comments. Design features and other relevant considerations will be noted. Typical comments that might apply to specific systems are as follows:

"Vehicle status is monitored".

"Field unit alarm capability is present".

"Polling procedures are inflexible".

"Shared usage by several agencies would be difficult to implement".

"Effect of weather on performance expected to be small".

"Fleet locations easily monitored by public".

"Each 90 vehicles monitored requires an additional radio channel".

"Sensors may require protection from vandalism".

e. Trade-off potential. This portion of the output will identify significant trade-off possibilities and the potential outcome that could result from those trade-offs. The trade-off relationships will be accessible during Step 4 (Table 1-21) of the program. Typical trade-offs that might be possible for all or some of the systems are these:

Location accuracy vs number of radio channels (via the polling option and rate).

Computing at the command center vs computing on-board the vehicles. (This affects the costs and accuracy vs radio spectrum trade-off.)

Display characteristics vs cost. (These trade-offs may be independent of the other descriptors of the system.)

Location accuracy vs cost (via the spatial density of signposts, the number of fixed sites, etc).

f. Cost benefit estimate. A preliminary estimate of efficiency increase with AVM will also be an output. The cost benefit estimate will be derived from the estimated increase in efficiency and data such as that listed below:

Patrolman average salary: \$XX, XXX per year  
 Patrolmen required for each vehicle: N  
 Support personnel for each vehicle: N.N  
 Overhead on salaries: PP%  
 Replacement cost of vehicle: \$X, XXX  
 Maintenance cost of vehicle: \$X, XXX per year

Based on the size of the fleet and these parameters, a cost benefit (deficit) first estimate will be provided such as:

Number of vehicles saved by shift: X, X, X  
 Vehicle cost saving equivalent: \$XXX, XXX  
 AVM capital investment equivalent,  
 10 yr: \$XXX, XXX  
 5 yr: \$XXX, XXX

The information provided by the AVM system synthesis program will not in itself provide sufficient justification for selection but will be a very important first step that eliminates obvious non-competitive techniques and allows for more detailed consideration of the viable techniques.

B. AVM System Simulation Computer Program

Much work has already been done by others in regard to AVM simulation (see Bibliography). The intent of this study effort is to utilize as much of that work as possible.

There is one aspect of the prior work where it is believed that improvement is needed. This is in the area of AVM system accuracy estimation. Prior AVM simulation work has investigated the overall command and control function to determine the effect of AVM system accuracy on "wrong dispatches" and the average distance travelled as a result of these "wrong dispatches." A "wrong dispatch" results when the closest available vehicle is not the one directed to respond to the call for service. This incorrect action results from not knowing precisely the vehicle locations, and thus the entire system performance is degraded owing to unnecessary distance travelled and time consumed in responding to calls for service.

In these prior simulations of the command and control functions, the investigators assigned values such as a 95 percentile value of a radial error of X feet to the AVM system accuracy. It has been assumed that this error distribution is normal and constant with time. The computer simulation programs determine the exact location of each vehicle from a mobility routine or driver scenario. Then, in order to test the system response to a call for service, each of the exact locations is corrupted in some random fashion with either X and Y or with an angle and range to the exact location. The apparent location is then used by the dispatching routine in the search for the vehicle closest to the call for service. The foregoing mode of simulation effectively assumes a constant value for the AVM system accuracy which may be misleading for all but those techniques that use very short intervals between vehicle location determinations. Short interval interrogation of location is not a requisite mode of operation in many AVM techniques and is impractical or inappropriate in others.

A more realistic approach to AVM accuracy simulation is to model the actual vehicle location process, including the expected or appropriate polling technique and taking into consideration the time lapse from the last location determination, the motion of the vehicles, and the resultant effect on closest car determination. In this mode of simulation, the vehicle mobility or driver location routine can be altered by a time-varying location uncertainty, if that is appropriate for the particular AVM system concept. The exact nature of this uncertainty or modification to the exact location may also be a function of other factors in addition to time. These factors may be vehicle speed, physical location at time of interrogation, distance travelled since last location, or distance travelled since last signpost proximity update. These factors will be explicitly considered by the AVM simulation program.

An accurate measure of the reduction in response time requires that a reasonably accurate geocoded definition of the coverage area be a part of the simulation program. Simulations that sum the absolute values of the differences in X- and Y-distances from the vehicle position



to the location of the call for assistance give a correct solution only for idealized rectangular cities. Geocoded descriptions of the coverage area will allow an accurate measure of distance in each instance, since the optimum travel routes can be used in the simulation.

The advantage of using the more accurate AVM simulation models is that a more realistic appraisal of the expected increase in efficiency can be determined. In addition, the possible variations in system configuration that affect performance parameters of the entire system can be investigated with the assurance that the influence of the variation has been considered.

Other technical performance parameters that will be considered in the simulation program include the data links involved in the vehicle location process and the effects of errors in reception; the effects of entry of new vehicles into the coverage area; and the re-establishment of the position of "lost" vehicles in relative location techniques. In addition, the actual location algorithm for each technique can be exercised with the expected input data. The preliminary concept of the main components of the AVM system simulation program are shown in Fig. 1-38. As already indicated, the intent is to develop this program around prior work insofar as possible.

Heretofore, simulation has been used almost exclusively in regard to reducing response time. The proposed simulation program will allow the investigation of other aspects of vehicle location. The utility of post data analysis can be evaluated, and the effects of an officer-needs-assistance incident can be assessed, both for the impact on subsequent calls for service and on the response time improvement to the officer in trouble.

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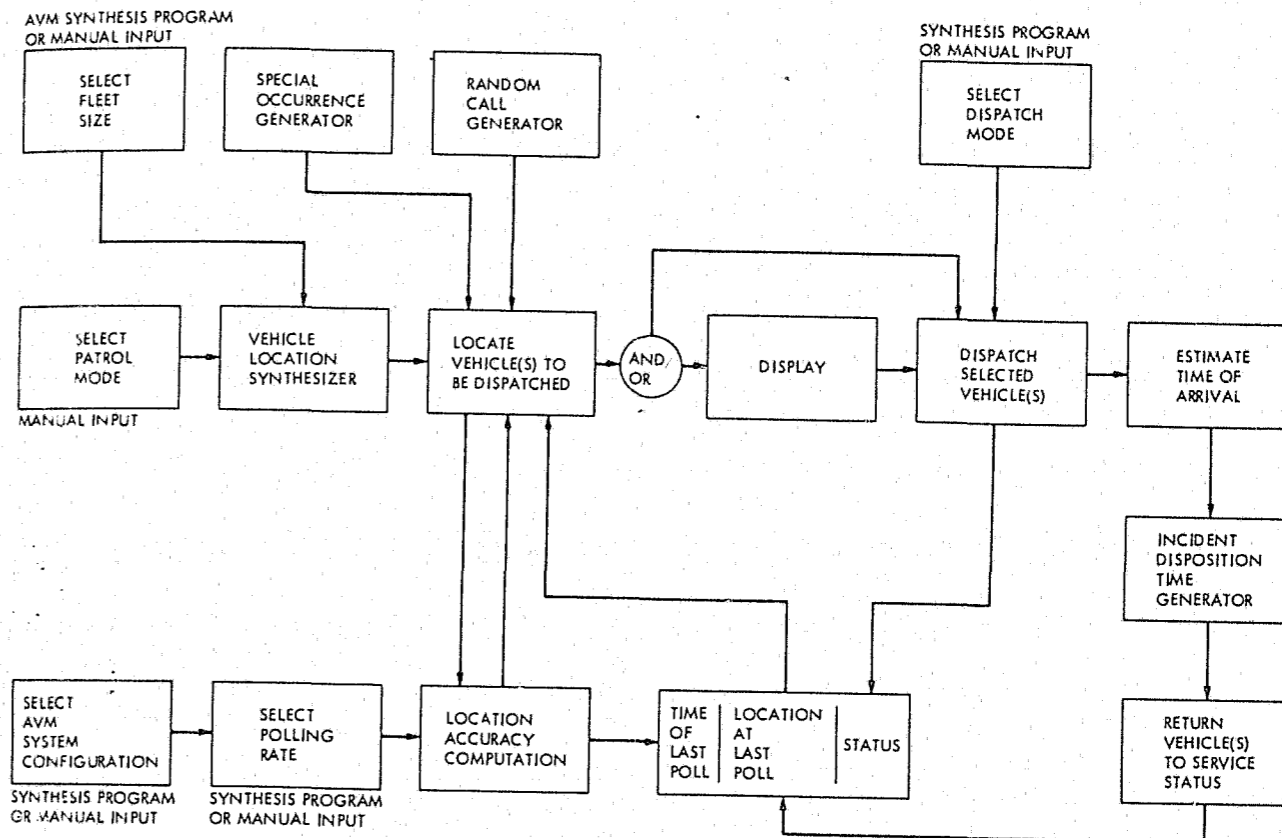


Figure 1-38. Concept for AVM System Simulation Computer Program

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**PART TWO:  
AVM DATA FOR USER  
GROUP ADVISORY  
COMMITTEE CITIES**

G.R. Hansen

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I. COST BENEFITS OF AVM SYSTEMS FOR SEVEN CITIES

A. Rationale for Selection of UGAC Cities

In order that a more realistic appraisal of the costs and expected performance of AVM Systems could be estimated, police department representatives from several cities were invited to participate in a User Group Advisory Committee (UGAC) devoted to studying AVM technologies. A set of nine criteria was established for selecting typical Southern California cities for the UGAC study. Some criteria are obvious and were established for time and economic considerations, while others were arrived at by heuristic processes. In this listing, the future tense is used because the criteria were established before city selection began. A brief rationale is presented with each criterion, to wit:

- (1) City Size. Cities in three categories, (a) less than 20 sq miles, (b) between 20 and 100 sq miles, and (c) greater than 100 sq miles, will be solicited to determine the impact on urban areas to be covered by AVM Systems.
- (2) Geography/Topography. Essentially flat as well as hilly areas in the communities are desirable to ascertain the effects on AVM methods as well as the communication data links.
- (3) Population Density/Land Use. These criteria are closely allied; and agricultural areas, industrial centers, and suburban as well as high-rise residential areas should be a part of the cities. This criterion will eliminate those cities formed to be wholly agricultural or industrial areas for tax purposes.
- (4) Building Sizes. The inclusion of high-rise dense metropolitan, low-rise business (less than 6-10 stories), mixed business and residential, and suburban areas is desirable to match and extend prior AVM work and to include the effects of these structure distributions on the communication links.
- (5) Population. Cities with populations of (a) more than 1,000,000, (b) between 200,000 and 1,000,000, and (c) less than 200,000 will be solicited. These numbers are arbitrary and are not firm, but the population somewhat determines the size of the municipal government. It is felt that this criterion is desirable as differing governing bodies will require AVM information to different degrees. Additionally, the participants in the user group will probably have different authority within their city governments as a function of population. It is believed, that those from smaller cities may be closer to the policy making level than those from major cities.
- (6) Willingness to Cooperate. This is an obvious but important criterion and is

difficult to assess beforehand. It is essential because the participants will be required to furnish data about their city as well as being regular in meeting attendance.

- (7) Pursuing or Contemplating AVM. This criterion is necessary to assure some active interest in the study effort.
- (8) Close to JPL. Economic considerations require this criterion since expense monies are not available in the grant for the participants. Additionally, regular frequent meetings are required and extensive travel time would be an additional expense to the participating city.
- (9) Must Have Public Safety Department. This is an obvious and perhaps trivial requirement, but is necessary to eliminate those cities that contract for police services with another government agency. These cities would probably fail Criterion (7) as well. This criterion is a natural outgrowth of the principal thrust of the proposed work which will focus on public safety vehicle location.

None of the foregoing criteria were intended to preclude participation by governmental bodies other than cities, such as counties. By criterion (8), only Los Angeles and possibly, San Bernardino, Ventura and Riverside counties could have been considered.

Seven cities were selected which met the majority of the criteria. Small cities were Menlo Park and Monterey Park. Medium cities selected were Pasadena, Long Beach, and Anaheim. The large cities were San Diego and Los Angeles.

Senior police officers from each of these cities participated in the UGAC and provided information concerning police operations and plans as well as statistical data for the individual cities.

B. Parameters Used in AVM Cost Analyses

Each UGAC city had different modes of operation and requirements regarding the implementation of AVM systems. For example, some police departments operate on a three-shift basis, while others use the ten-four plan where the officers work four 10-hour days in sequence. In responding to calls for service, some police departments use only patrolling vehicles while others dispatch the plain colored (i. e., pastels) in response to citizen calls. The inclusion of motorcycles, either two- or three-wheelers, in the AVM system was planned by some cities, but not by others. In the main, however, there is sufficient commonality of parameters to allow for automation of the AVM cost and performance estimation procedures.

1. Number of vehicles in the fleet. The total number of vehicles to be instrumented is the basis for the car cost estimates. Motorcycles were not included because a satisfactory digital message capability for motorcycles does not yet

exist. Vehicles, which in general do not respond to calls for service were also not included. The maximum and minimum number of vehicles by shift was determined and normalized to a three-shift operation. This parameter is necessary to determine vehicle polling intervals.

2. City area, street mileage, number of intersections and road segments. This information was provided by the representatives for the UGAC cities. The beat area is an important parameter which is used in the AVM system accuracy estimation, but no standard or common method of determining this parameter could be found. In some cities, the beats are correlated with the crime reporting technique. In others, the beats are periodically readjusted as determined by the average number of vehicles deployed on particular shifts. The beat size parameter is an independent variable in predicting the response-time improvement that should accrue with a given location accuracy value. For the purposes of this study, the beat size was placed at the values resulting from dividing the city area by the number of vehicles deployed. This average value assumption cannot be wholly justified when, for example, beats vary from 6 blocks to 49 square miles in size as they do in San Diego.

3. Number of signposts or fixed sites required. The fixed site enumeration parameter in Class II and IV AVM systems was determined from the data supplied concerning the number of intersections or road segments. Where the technique was dependent on the number of lanes in the segment, the average value of 2.4 lanes per street segment was assumed as in the model cities. For the Class III AVM techniques, the placement and/or the number of widely distributed fixed sites required was determined by an algorithm which was only a function of the area in the model city estimations. The boundaries and shape of the UGAC cities seemed to dictate a more realistic approach. Boundary outline maps of each city were prepared, and the most optimum placement of a grid representing the spacings for narrow-band and wide-band antennas was determined. The minimum number of sites that would be necessary was thereby determined. The assumptions made were that there were no "difficult" RF areas that would require additional coverage, and that a fixed site could be placed where needed regardless of zoning, existing structure, or geographical restrictions.

4. Costing procedure for AVM Systems in UGAC cities. The costing of the various AVM system configurations for the UGAC cities was accomplished through the use of the APL computer programming language (see Part Three). The costs of vehicle equipment, fixed sites, base equipments, and polling elements were stored in the table form by technique and cost category (e.g., equipment, installation, operation and maintenance). This assemblage forms the cost data base. The various parameters for each UGAC city are also stored in a prescribed manner as follows:

- (1) Urban area in square miles.
- (2) East to West extent in miles.
- (3) North to South extent in miles.

- (4) Road mileage.
- (5) Number of intersections.
- (6) Number of road segments.
- (7) Number of vehicles in AVM fleet.
- (8) Number of motorcycles.
- (9) Maximum number vehicles deployed in first shift.
- (10) Minimum number of vehicles deployed in first shift.
- (11) Maximum number of vehicles deployed in second shift.
- (12) Minimum number of vehicles deployed in second shift.
- (13) Maximum number of vehicles deployed in third shift.
- (14) Minimum number of vehicles deployed in third shift.
- (15) Number of dispatcher consoles.
- (16) Number of small coverage (or narrow band) Class III AVM sites.
- (17) Number of wide coverage (wide-band) Class III AVM sites.

The cost estimates (as of 1974) are compiled into the cost categories after multiplying by the appropriate parameter. The program is very simple, being really a programmed desk calculator with automatic input. The rationale for programming was to avoid a repetitious procedure of calculating fine cost categories and obtaining three totals for each of 36 AVM techniques in the seven UGAC and three model cities and to simplify future cost estimations.

#### C. Descriptions and Summary Analyses of UGAC Cities

In Sections II through VIII, outline maps of each UGAC city are presented along with detailed listing of each city's physical parameters, AVM cost summaries, vehicle polling cycle times, and estimates of the AVM system accuracies and 5-year cost savings. The seven selected cities were Anaheim, Long Beach, Montclair, Monterey Park, Pasadena, San Diego, and Los Angeles. Thirty-six techniques in the four AVM classes were investigated for each city. Each of the seven cities was treated as an entity, with the exception of Los Angeles which was evaluated for each of its four geographical bureaus. Additionally, because of the large number of vehicles deployed in the cities of San Diego and the four Los Angeles bureaus, the system accuracies were determined for shorter cycle times or polling intervals. That is, more than one RF channel (half-duplex) was allowed for these areas.

In this Section, the summary analyses for each UGAC city are based solely on a comparison of the estimated 5-year saving and the estimated costs (as of 1974) of particular AVM systems.

The 5-year saving is predicted on only one factor of AVM performance, namely response time improvement. There are many other aspects of AVM systems which should enter into the decision process. Many of the thirty-six listed techniques which appear viable have never been developed or tested in typical urban environments. Therefore, only the developed and/or tested concepts will be discussed in the following summary descriptions. Complete tabulations are given in Sects. II to VIII.

1. Anaheim, CA. This city might be characterized as a break-even city with response time improvement such that cost savings just equal AVM costs, but only for the dead-reckoning techniques in Class I. Anaheim is slightly smaller than the medium model city (see Part One, Sect. III) in both area and fleet size, and the cost summary indicates Class I system costs for the dead-reckoning techniques of about \$280,000. The 5-year saving is about \$300,000 for a magnetic-compass/odometer system with a system accuracy of 50 to 75 meters.

The Class II AVM systems which indicate some car saving are the wide-spaced signposts and buried magnets. The accuracies achievable are roughly 250 meters and 50 to 75 meters, respectively. The cost of the Class II wide-spaced signposts is about twice the saving, while the buried magnets may cost four times the 5-year saving.

The most accurate Class III and all Class IV systems resulted in car saving, but the cost saving was negative. (See Sect. II.)

2. Long Beach, CA. The same AVM techniques as in Anaheim are viable in this city, but because the city is slightly larger in area with a substantially bigger vehicle fleet, the costs are about \$50,000 more for the Class I dead-reckoning techniques. The 5-year savings are lower, about \$160,000, because the maximum deployment considered is less than in Anaheim.

There is a large difference between Anaheim and Long Beach in the Class II AVM systems as Long Beach has almost four times the road mileage and almost twice the number of intersections. Long Beach is unique in having a large number of named dedicated alleys in the central area which results in an intersection density of 144/km<sup>2</sup> (400 per square mile). This factor causes the Class II and Class IV techniques to have a greater number of installations than are really required. Wide-spaced signposts and buried magnets indicate car savings, but the 5-year figure is well below the systems cost. If the high central density were reduced to a more reasonable value, the disparity between cost and saving would lessen to the point where the saving would be half the cost.

The pulse TOA Class III technique and all the Class IV systems indicated car savings, but cost savings were negative. (See Sect. III.)

3. Montclair, CA. In this city, the dead-reckoning techniques of Class I AVM and most of the techniques in the other classes indicate car savings primarily because system accuracies are very high. This is a direct result of a very short polling cycle time. The 5-year savings for all systems that indicate a saving are negative and exceed a "loss" of \$200,000. The car savings are

in the order of 5% of the deployed vehicles (4 to 7), that is, 0.2 to 0.4 cars.

Despite the fact that Montclair has a wide-spaced signpost AVM system installed and operational for over a year, this analysis indicates that the cost is substantially greater than the saving. The reason this analysis is faulty in this case is that Montclair does not have either a computer in the system nor the operation and maintenance (O-M) personnel indicated as required for all systems.

The system accuracy indicated for the wide-spaced Class II signposts is about 250 meters, which is quite close to that achieved in Montclair. The installed system has an accuracy of 0.2 km (1/8 mile) with slightly fewer signposts. The system costs are quite similar for the technique if the O-M category is omitted (\$60K versus \$71K). (See Sect. IV.)

4. Monterey Park, CA. Car savings are indicated for all classes of AVM in this city. Again as in the other small city, or small model, the cost saving is near zero or negative. This city, because of the great difference between maximum and minimum deployment and short polling cycle shows a greater car saving when fewer vehicles are deployed. If the O-M costs were greatly reduced, the 5-year saving would exceed the costs. (See Sect. V.)

5. Pasadena, CA. This city is roughly half-way between the small and medium models. Again a car saving is shown in all AVM classes with negative 5-year cost savings. Again, the short polling cycle causes little degradation of achievable accuracy. The O-M costs are the principal element mitigating against a positive saving, and the value for cars saved is less than a whole car. (See Sect. VI.)

6. San Diego, CA. In this city, virtually every AVM technique indicates a positive 5-year saving. The Class I dead-reckoning techniques system costs are exceeded by the estimated savings, and the Class III costs are close to the savings. This result occurs despite the poor system accuracies caused by relatively long polling cycles. There is a substantial car savings because the averaging of beat areas leads to results in which apparent response time improvements with very inaccurate techniques occur. More than half the area of San Diego is covered by five northern beats which causes the average beat to be 40% larger in side dimension than the average beat that would result if these five beats and the area involved were not considered. The reduction in beat dimension would cause a decrease in apparent response time improvement.

In an attempt to reduce cycle time effects, the system accuracy and cost savings calculation were also performed for three RF channels for AVM. The cost savings under these conditions for Class I systems were doubled. The savings for Class II were uniformly increased by about \$1.8 million to the point where the cost of the buried magnet system was equalled, as were the costs of the Class III pulse TOA system, by the cost saving. (See Sect. VII.)

7. Los Angeles, CA. Los Angeles was analyzed separately for each of the four bureaus

(Central, South, West, Valley), which range in area from 130 to 500 km<sup>2</sup> (50 to 200 square miles). Again as in the medium model city, all of the bureaus show a 5-year saving for most of the AVM techniques. All bureaus operate about the same number of cars, so the effect of beat size on the response time efficiency increase is greater for the larger bureaus. In overall cost savings, the Valley bureau shows the greatest saving, followed in order by the West, Central, and South Bureaus.

The AVM system accuracy and 5-year saving calculations were performed for 2 and 3 RF channels for the AVM systems for each of the bureaus. As expected, the accuracy improved to about one-half and one-third that of the one RF channel case. The 5-year saving with 3 channels showed an increase when changing from 2 to 3 RF channels that was almost twice that obtained in changing from 1 to 2 RF channels. The increase in accuracy leads to increased car savings, thereby reducing the effect of the constant O-M expenses. (See Sect. VIII.)

**II. Anaheim, CA, City AVM Cost Benefit Analysis Tables**

Table 2-1. Anaheim, CA, City AVM Physical Parameters

AREA IS 98.5 SQUARE MILES.  
 EAST WEST DISTANCE IS 15.3 MILES.  
 NORTH SOUTH DISTANCE IS 6 MILES.  
 TOTAL ROAD MILEAGE IS 456 MILES.  
 THE NUMBER OF INTERSECTIONS IS 4800.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 9600.  
 THERE ARE 36 CARS IN THE FLEET.  
 AND THERE ARE 0 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 14  
 FIRST SHIFT MIN. 14  
 SECOND SHIFT MAX. 12  
 SECOND SHIFT MIN. 12  
 THIRD SHIFT MAX. 19  
 THIRD SHIFT MIN. 19  
 THE NUMBER OF DISPATCHERS IS 1  
 THE CITY WOULD REQUIRE 6 WIDE+BAND OR PULSE ANTENNA SITES AND 16 NARROW BAND ANTENNA SITES FOR 2 AND 3 MILE RADIUS COVERAGE.

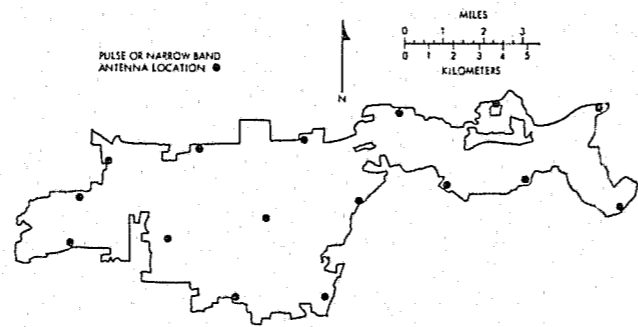


Figure 2-1. Anaheim, CA, AVM Pulse or Narrow-Band Antenna Locations

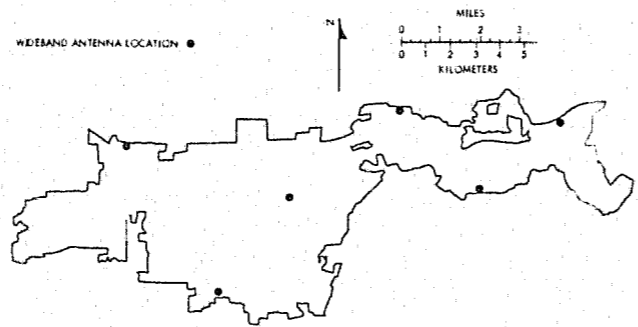


Figure 2-2. Anaheim, CA, AVM Wide-Band Antenna Locations

Table 2-2. Anaheim, CA, AVM Systems Cost Analyses

TECHNIQUE	THOUSANDS OF \$			TOTAL		
	CAPS	SITES	SHRE	INIT	YR	5YR
KEYBOARD	2	0	12	101	100	100
STYLUS MAP	2	0	12	101	100	100
2-ACCCELEROMETERS	50	0	14	104	251	251
LASER MEGALINTR	40	0	15	106	251	251
ULTRASONIC WELD	40	0	14	106	251	251
COMPASS ODOMETER	30	0	11	102	251	251
COMPASS LASER MEL	30	0	14	104	250	250
DIFF. OMEGA	30	0	15	105	250	250
LOFAN	101	0	15	105	250	250
DECCA	40	0	15	105	250	250
HI-STATIONS	10	0	15	105	250	250
DIFF. OMEGA	30	0	15	105	250	250
DIFF. LOFAN	101	0	15	105	250	250
DIFF. HI-STA.	10	0	15	105	250	250
RELAY OMEGA	19	0	15	104	251	251
RELAY LOFAN	21	0	15	104	250	250
CLASS II						
DUPLEXED PULS. LOOPS	10	2206	59	5496	101	3392
REFLECTING SIGNS	10	1056	59	532	187	1367
REFLECTING ROAD	5	116	59	704	677	1565
PHOTO POST	7	1104	59	228	173	1574
HI-TRAP POST	6	100	59	119	375	375
LF POST	6	600	59	228	173	1074
LIGHT I-R POST	6	100	59	277	321	1043
DUPLEXED MAGNETS	4	323	59	657	180	1149
ULTRASONIC POST	5	816	59	830	187	1315
TRAFFIC SENSOR	6	312	59	396	101	1478
CLASS III						
WIDE-BAND FM PHASE	4	76	103	18	109	310
PULSE T-O-RAPITAL	100	234	110	23	204	511
NOISE CORRELATION	30	29	57	19	173	519
DIRECTION FINDER	3	73	37	16	154	306
CLASS IV						
TRAFFIC LOOPS	3	2343	59	1215	216	4535
WIDE-BAND FM PHASE	3	2476	59	1097	341	3474
PHOTO I-R DETECT	3	1455	59	555	321	2293
ULTRASONIC DETECT	3	1503	59	555	321	2342

Table 2-3. Anaheim, CA, AVM Polling Cycle Min/Max Times

CLASS I TECHNIQUE	TOTAL FLEET	CALL TIME IN SECONDS TO POLL FROM AND MIN UNITS DEPLOYED.					
		SWIC	SIMPLE	PHOTO	SWIC	PHOTO	PHOTO
KEYBOARD	2-36	2-04	2-12	4-09	2-15	2-23	4-20
STYLUS MAP	4-03	2-13	2-20	4-18	2-26	2-31	4-26
2-ACCCELEROMETERS	3-34	2-00	2-15	2-64	1-44	1-53	2-30
LASER MEGALINTR	3-99	1-21	1-36	2-61	2-25	2-31	4-46
ULTRASONIC WELD	3-94	2-10	2-18	4-16	2-31	1-52	4-30
COMPASS ODOMETER	3-34	1-32	1-33	2-62	1-46	1-55	2-30
COMPASS LASER MEL	3-94	1-31	1-36	4-13	1-42	1-52	2-30
DIFF. O-MEGA MEL	3-34	2-08	2-15	4-13	2-25	2-31	4-46
LOFAN	4-25	1-21	1-26	2-61	1-42	1-52	2-30
DECCA	4-25	2-31	2-32	4-13	2-25	2-31	4-46
HI-STATIONS	2-24	1-24	1-43	2-74	1-29	1-39	2-30
DIFF. OMEGA	4-25	1-30	1-34	2-59	1-41	1-49	2-30
DIFF. LOFAN	4-25	1-42	1-46	4-29	2-29	2-34	4-46
DIFF. HI-STA.	4-25	2-21	2-30	2-71	1-29	1-39	2-30
DIFF. HI-STA.	4-25	1-46	1-50	2-75	1-31	1-41	2-30
RELAY OMEGA	15-60	2-23	2-28	4-20	2-25	2-31	4-46
RELAY LOFAN	15-60	2-23	2-21	10-29	14-57	14-72	15-30
CLASS II							
DUPLEXED PULS. LOOPS	2-34	2-03	2-15	4-13	2-25	2-31	4-46
REFLECTING SIGNS	2-34	2-03	2-15	4-13	2-25	2-31	4-46
REFLECTING ROAD	2-34	1-31	1-36	2-61	1-42	1-52	2-30
PHOTO POST	2-34	1-31	1-36	4-13	2-25	2-31	4-46
HI-TRAP POST	2-34	2-06	2-14	4-12	1-42	1-52	2-30
LF POST	2-34	1-30	1-35	2-60	1-41	1-50	2-30
LIGHT I-R POST	2-34	2-06	2-12	4-09	2-18	2-25	4-46
DUPLEXED MAGNETS	2-34	1-30	1-34	2-59	1-39	1-47	2-30
ULTRASONIC POST	2-34	2-06	2-14	4-12	1-41	1-50	2-30
TRAFFIC SENSOR	2-34	1-30	1-35	2-60	1-41	1-50	2-30

Table 2-4. Anaheim, CA, AVM Accuracies and Cost Benefits

TECHNIQUE	ESTIMATE ACCURACIES IN VEHICLES		ESTIMATED SAVING		ESTIMATED SAVING	
	PERCENT	VEHICLES SAVED	PERCENT	VEHICLES SAVED	PERCENT	VEHICLES SAVED
KEYBOARD	70	1	94	21	94	21
STYLUS MAP	70	1	93	20	93	20
2-ACCCELEROMETERS	70	1	96	23	96	23
LASER MEGALINTR	70	1	94	22	94	22
ULTRASONIC WELD	70	1	94	22	94	22
COMPASS ODOMETER	70	1	100	24	100	24
COMPASS LASER MEL	70	1	94	22	94	22
DIFF. O-MEGA MEL	70	1	94	22	94	22
LOFAN	1000	0	914	240	914	240
DECCA	1000	0	932	244	932	244
HI-STATIONS	200	1	92	22	92	22
DIFF. OMEGA	200	1	90	21	90	21
DIFF. LOFAN	200	1	91	22	91	22
DIFF. HI-STA.	200	0	100	24	100	24
RELAY OMEGA	500	0	500	125	500	125
RELAY LOFAN	100	0	100	24	100	24
CLASS III						
DUPLEXED PULS. LOOPS	10	1	73	17	73	17
REFLECTING SIGNS	10	1	73	17	73	17
REFLECTING ROAD	10	1	71	16	71	16
PHOTO POST	10	1	74	17	74	17
HI-TRAP POST	15	1	73	17	73	17
LF POST	100	1	75	17	75	17
LIGHT I-R POST	10	1	76	17	76	17
DUPLEXED MAGNETS	4	1	71	16	71	16
ULTRASONIC POST	10	1	74	17	74	17
TRAFFIC SENSOR	10	1	73	17	73	17
CLASS IV						
WIDE-BAND FM PHASE	1000	0	258	62	258	62
PULSE T-O-RAPITAL	1000	0	254	61	254	61
NOISE CORRELATION	100	1	177	42	177	42
DIRECTION FINDER	100	1	198	47	198	47
CLASS I						
TRAFFIC LOOPS	10	1	25	6	25	6
WIDE-BAND FM PHASE	100	1	213	51	213	51
PHOTO I-R DETECT	10	1	25	6	25	6
ULTRASONIC DETECT	10	1	25	6	25	6

**III. Long Beach, CA, City AVM Cost Benefit Analysis Tables**

Table 2-5. Long Beach, CA, City AVM Physical Parameters

AREA IS 50.2 SQUARE MILES.  
 EAST WEST DISTANCE IS 10 MILES.  
 NORTH SOUTH DISTANCE IS 3.6 MILES.  
 TOTAL ROAD MILEAGE IS 2000 MILES.  
 THE NUMBER OF INTERSECTIONS IS 8000.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 10000.  
 THERE ARE 61 CARS IN THE FLEET.  
 AND THERE ARE 51 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 16  
 FIRST SHIFT MIN. 15  
 SECOND SHIFT MAX. 16  
 SECOND SHIFT MIN. 16  
 THIRD SHIFT MAX. 16  
 THIRD SHIFT MIN. 16  
 THE NUMBER OF DISPATCHERS IS 2  
 THE CITY WOULD REQUIRE 7 WIDE+BAND OR PULSE ANTENNA SITES AND 21 NARROW BAND ANTENNA SITES FOR 2 AND 3 MILE RADIUS COVERAGE.

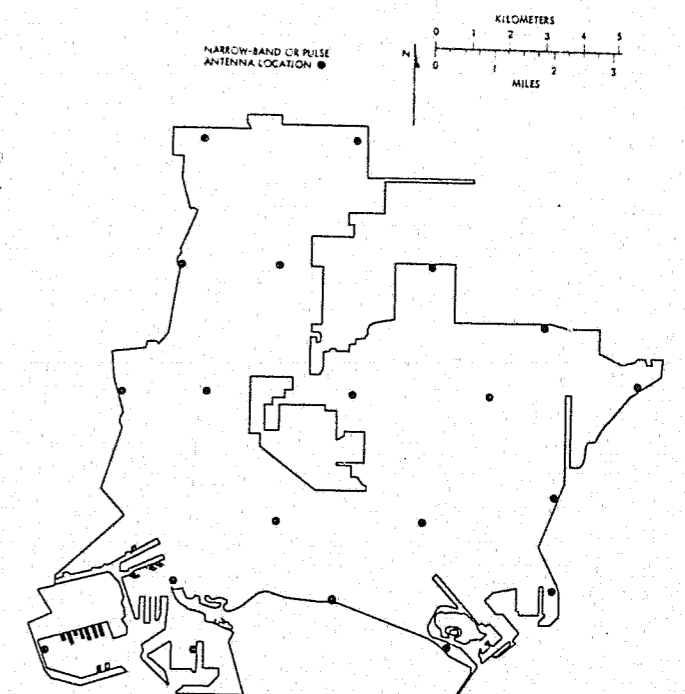


Figure 2-3. Long Beach, CA, AVM Pulse or Narrow-Band Antenna Locations

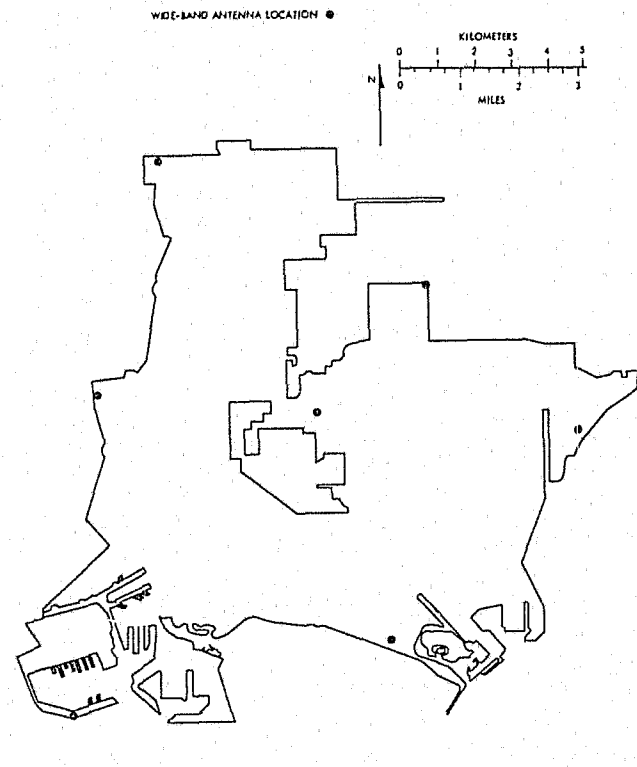


Figure 2-4. Long Beach, CA, AVM Wide-Band Antenna Locations

Table 2-6. Long Beach, CA, AVM Systems Cost Analyses

TECHNIQUE	CAPS	SITES	FARE	DIST	W-H	W-L	SYNC	PHRD	TOTAL
KEYBOARD	100	0	66	12	101	136	338	376	1001
STYLUS MAP	100	0	66	12	107	345	389	1001	
2-ACCELEROMETERS	40	0	34	14	110	295	327	744	
LASER VELOCIMTR	100	0	66	12	110	319	344	1001	
ULTRASONIC WELD	40	0	34	14	100	310	327	744	
COMPASS ODOMETER	100	0	66	12	106	297	325	1001	
COMPASS LASER WEL	114	0	72	17	106	327	341	1001	
COMPASS U-SONIC WEL	47	0	38	17	106	307	341	1001	
OMEGA	100	0	66	12	105	305	340	1001	
LOPHAN	171	0	114	19	105	305	341	1001	
DECCA	1	0	14	105	295	324	344	1001	
AM-STATIONS	100	0	66	12	105	305	340	1001	
DIFF. OMEGA	100	0	66	12	104	299	341	1001	
DIFF. LOPHAN	171	0	114	19	105	305	340	1001	
DIFF. AM-STA.	100	0	66	12	104	299	341	1001	
RELAY OMEGA	100	0	66	12	105	305	340	1001	
RELAY LOPHAN	171	0	114	19	105	305	341	1001	
CLASS II									
BURIED RES. LOOPS	100	1000	66	12	101	307	341	1001	
REFLECTING SIGNS	100	1000	66	12	100	298	340	1001	
REFLECTING ROAD	100	1000	66	12	101	307	341	1001	
X-BAND POST	100	1000	66	12	101	307	341	1001	
HF, UHF POST	100	1000	66	12	101	307	341	1001	
LF POST	100	1000	66	12	101	307	341	1001	
LIGHT I-R POST	100	1000	66	12	101	307	341	1001	
BURIED MAGNETS	100	1000	66	12	101	307	341	1001	
ULTRASONIC POST	100	1000	66	12	101	307	341	1001	
TRAFFIC SENSOR	100	1000	66	12	101	307	341	1001	
CLASS III									
WIDE-BAND FM PHASE	14	49	114	21	113	315	340	1001	
NAR-BAND FM PHASE	170	51	126	21	106	316	342	1001	
PULSE T-O-ARRIVAL	150	294	238	17	136	1000	1000	1001	
NOISE CORRELATION	40	40	240	21	179	1000	1000	1001	
DIRECTION FINDER	1	74	67	16	154	1000	1000	1001	
CLASS IV									
TRAFFIC LOOPS	1	1000	66	12	101	307	341	1001	
WIDE-BAND FM PHASE	1	1000	66	12	101	307	341	1001	
PULSE T-O-ARRIVAL	1	1000	66	12	101	307	341	1001	
NOISE CORRELATION	1	1000	66	12	101	307	341	1001	
DIRECTION FINDER	1	1000	66	12	101	307	341	1001	

Table 2-7. Long Beach, CA, AVM Polling Cycle Min/Max Times

CLASS I	TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED.					
			SYNC	SIMPLE UOL	PHRD	SYNC	REDUNDANT UOL	PHRD
CLASS I	KEYBOARD	12-02	1.72	1.79	3.47	1.83	1.98	3.73
	STYLUS MAP	12-54	1.79	1.87	3.54	1.93	2.13	3-30
	2-ACCELEROMETERS	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	LASER VELOCIMTR	12-48	1.77	1.85	3.52	1.94	2.09	3-34
	ULTRASONIC WELD	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	COMPASS ODOMETER	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	COMPASS LASER WEL	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	COMPASS U-SONIC WEL	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	OMEGA	13-22	1.89	1.96	3.64	2.18	2.33	4-07
	LOPHAN	13-59	1.94	2.02	3.69	2.23	2.43	4-16
	DECCA	13-44	1.92	1.99	3.67	2.24	2.39	4-14
	AM-STATIONS	12-18	1.73	1.80	3.48	1.86	2.01	3-75
CLASS II	DIFF. OMEGA	13-22	1.89	1.96	3.64	2.18	2.33	4-07
	DIFF. LOPHAN	13-59	1.94	2.02	3.69	2.23	2.43	4-16
	DIFF. AM-STA.	13-14	1.88	1.95	3.63	2.16	2.30	4-05
	RELAY OMEGA	1131-20	161-60	161-68	163-35	321-60	321-75	323-50
	RELAY LOPHAN	48-53	6-93	7-01	8-68	12-27	12-42	14-17
	BURIED RES. LOOPS	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	REFLECTING SIGNS	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	REFLECTING ROAD	12-25	1.75	1.82	3.50	1.90	2.05	3-30
	X-BAND POST	12-17	1.74	1.81	3.49	1.88	2.03	3-78
	HF, UHF POST	12-02	1.72	1.79	3.47	1.83	1.98	3-73
	LF POST	12-17	1.74	1.81	3.49	1.88	2.03	3-78
	LIGHT I-R POST	12-17	1.74	1.81	3.49	1.88	2.03	3-78
BURIED MAGNETS	12-25	1.75	1.82	3.50	1.90	2.05	3-30	
ULTRASONIC POST	12-17	1.74	1.81	3.49	1.88	2.03	3-78	
TRAFFIC SENSOR	12-17	1.74	1.81	3.49	1.88	2.03	3-78	

Table 2-8. Long Beach, CA, AVM Accuracies and Cost Benefits.

CLASS I	TECHNIQUE	VEHICLES	SYSTEM ACCURACIES IN PERCENT				ESTIMATED \$1000 SAVINGS		
			VEHICLES	VEHICLES	VEHICLES	VEHICLES	ESTIMATED	ESTIMATED	
CLASS I	KEYBOARD	100	100	100	100	100	100	100	
	STYLUS MAP	100	100	100	100	100	100	100	
	2-ACCELEROMETERS	100	100	100	100	100	100	100	
	LASER VELOCIMTR	100	100	100	100	100	100	100	
	ULTRASONIC WELD	100	100	100	100	100	100	100	
	COMPASS ODOMETER	100	100	100	100	100	100	100	
	COMPASS LASER WEL	100	100	100	100	100	100	100	
	COMPASS U-SONIC WEL	100	100	100	100	100	100	100	
	OMEGA	100	100	100	100	100	100	100	
	LOPHAN	100	100	100	100	100	100	100	
	DECCA	100	100	100	100	100	100	100	
	AM-STATIONS	100	100	100	100	100	100	100	
CLASS II	DIFF. OMEGA	100	100	100	100	100	100	100	
	DIFF. LOPHAN	100	100	100	100	100	100	100	
	DIFF. AM-STA.	100	100	100	100	100	100	100	
	RELAY OMEGA	100	100	100	100	100	100	100	
	RELAY LOPHAN	100	100	100	100	100	100	100	
	BURIED RES. LOOPS	100	100	100	100	100	100	100	
	REFLECTING SIGNS	100	100	100	100	100	100	100	
	REFLECTING ROAD	100	100	100	100	100	100	100	
	X-BAND POST	100	100	100	100	100	100	100	
	HF, UHF POST	100	100	100	100	100	100	100	
	LF POST	100	100	100	100	100	100	100	
	LIGHT I-R POST	100	100	100	100	100	100	100	
BURIED MAGNETS	100	100	100	100	100	100	100		
ULTRASONIC POST	100	100	100	100	100	100	100		
TRAFFIC SENSOR	100	100	100	100	100	100	100		
CLASS III	WIDE-BAND FM PHASE	1000	1000	1000	1000	1000	1000	1000	
	NAR-BAND FM PHASE	1000	1000	1000	1000	1000	1000	1000	
	PULSE T-O-ARRIVAL	1000	1000	1000	1000	1000	1000	1000	
	NOISE CORRELATION	1000	1000	1000	1000	1000	1000	1000	
	DIRECTION FINDER	1000	1000	1000	1000	1000	1000	1000	
	CLASS IV	TRAFFIC LOOPS	1000	1000	1000	1000	1000	1000	1000
		WIDE-BAND FM PHASE	1000	1000	1000	1000	1000	1000	1000
		PULSE T-O-ARRIVAL	1000	1000	1000	1000	1000	1000	1000
		NOISE CORRELATION	1000	1000	1000	1000	1000	1000	1000
		DIRECTION FINDER	1000	1000	1000	1000	1000	1000	1000

IV. Montclair, CA, City AVM Cost Benefit Analysis Tables

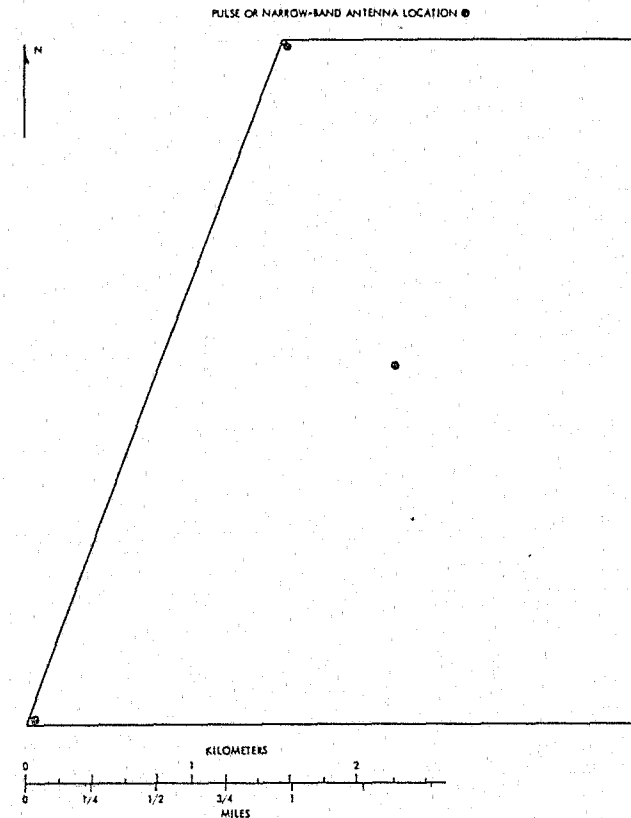


Figure 2-5. Montclair, CA, AVM Pulse or Narrow-Band Antenna Locations

Table 2-9. Montclair, CA, City AVM Physical Parameters

AREA IS 5.2 SQUARE MILES.  
 EAST WEST DISTANCE IS 2.3 MILES.  
 NORTH SOUTH DISTANCE IS 2.5 MILES.  
 TOTAL ROAD MILEAGE IS 67 MILES.  
 THE NUMBER OF INTERSECTIONS IS 330.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 506.  
 THERE ARE 10 CARS IN THE FLEET.  
 AND THERE ARE 0 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 5  
 FIRST SHIFT MIN. 4  
 SECOND SHIFT MAX. 5  
 SECOND SHIFT MIN. 4  
 THIRD SHIFT MAX. 7  
 THIRD SHIFT MIN. 7  
 THE NUMBER OF DISPATCHERS IS 1  
 THE CITY WOULD REQUIRE 3 WIDE-BAND OR PULSE ANTENNA SITES AND 5 NARROW BAND FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-10. Montclair, CA, AVM Systems Cost Analyses

CLASS I	TECHNIQUE	CAPS	SITES	FARE	DIST	W-H	W-L	SYNC	PHRD	TOTAL
CLASS I	KEYBOARD	100	0	66	12	101	136	338	376	1001
	STYLUS MAP	100	0	66	12	107	345	389	1001	
	2-ACCELEROMETERS	40	0	34	14	110	295	327	744	
	LASER VELOCIMTR	100	0	66	12	110	319	344	1001	
	ULTRASONIC WELD	40	0	34	14	100	310	327	744	
	COMPASS ODOMETER	100	0	66	12	106	297	325	1001	
	COMPASS LASER WEL	114	0	72	17	106	327	341	1001	
	COMPASS U-SONIC WEL	47	0	38	17	106	307	341	1001	
	OMEGA	100	0	66	12	105	305	340	1001	
	LOPHAN	171	0	114	19	105	305	341	1001	
	DECCA	1	0	14	105	295	324	344	1001	
	AM-STATIONS	100	0	66	12	105	305	340	1001	
CLASS II	DIFF. OMEGA	100	0	66	12	104	299	341	1001	
	DIFF. LOPHAN	171	0	114	19	105	305	340	1001	
	DIFF. AM-STA.	100	0	66	12	104	299	341	1001	
	RELAY OMEGA	100	0	66	12	105	305	340	1001	
	RELAY LOPHAN	171	0	114	19	105	305	341	1001	
	BURIED RES. LOOPS	100	1000	66	12	101	307	341	1001	
	REFLECTING SIGNS	100	1000	66	12	100	298	340	1001	
	REFLECTING ROAD	100	1000	66	12	101	307	341	1001	
	X-BAND POST	100	1000	66	12	101	307	341	1001	

Table 2-11. Montclair, CA, AVM Polling Cycle Min/Max Times

CLASS I TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED					
		SYNC	SIMPLE	FMOD	RESOUNDANT	FMOD	FMOD
KEYBOARD	1-07	0.75	0.77	1.49	0.88	0.84	1.56
STYLUS MAP	1-12	0.43	0.44	0.80	0.57	0.51	1.04
2-ACCELEROMETERS	1-09	0.45	0.46	0.87	0.50	0.52	1.01
LASER VELOCIMTR	1-11	0.44	0.45	0.86	0.48	0.50	0.96
ULTRASONIC WELD	1-09	0.73	0.79	1.51	0.95	0.89	1.66
COMPASS-ODOMETER	1-09	0.77	0.78	1.50	0.83	0.87	1.61
COMPASS-LASER WEL	1-09	0.44	0.45	0.86	0.48	0.50	0.96
GPS-U-SONIC WEL	1-09	0.44	0.45	0.86	0.48	0.50	0.96
ORIGA	1-13	0.44	0.45	0.86	0.48	0.50	0.96
LORAN	1-21	0.49	0.50	0.91	0.57	0.59	1.01
DECCA	1-20	0.84	0.86	1.53	0.93	1.02	1.75
RR-STATIONS	1-00	0.43	0.44	0.85	0.50	0.51	1.04
DIFF. ORIGA	1-13	0.43	0.44	0.85	0.50	0.51	1.04
DIFF. LORAN	1-21	0.49	0.50	0.91	0.57	0.59	1.01
DIFF. RR-STA.	1-17	0.43	0.44	0.85	0.50	0.51	1.04
RELAY ORIGA	101-00	70.70	70.70	141.40	140.70	141.40	141.40
RELAY LORAN	4-23	40.40	40.40	80.80	80.40	80.80	80.80
CLASS II BURIED RES. LOOPS	1-06	0.74	0.76	1.48	0.70	0.62	1.56
REFLECTING SIGNS	1-06	0.42	0.43	0.85	0.45	0.47	1.00
REFLECTING ROAD	1-06	0.42	0.43	0.85	0.45	0.47	1.00
X-BAND POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
HF, VHF POST	1-05	0.42	0.43	0.85	0.45	0.47	1.00
LF POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
LIGHT I-R POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
BURIED MAGNETS	1-06	0.42	0.43	0.85	0.45	0.47	1.00
ULTRASONIC POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
TRAFFIC SENSOR	1-06	0.42	0.43	0.85	0.45	0.47	1.00

Table 2-12. Montclair, CA, AVM Accuracies and Cost Benefits

CLASS I TECHNIQUE	TOTAL FLEET	ULTIMATE ACCURACY	VEHICLES SERVED	ESTIMATED \$1000 SAVINGS		
				VEHICLES	VEHICLES	VEHICLES
KEYBOARD	1-07	0.75	149	0.88	0.84	1.56
STYLUS MAP	1-12	0.43	80	0.57	0.51	1.04
2-ACCELEROMETERS	1-09	0.45	87	0.50	0.52	1.01
LASER VELOCIMTR	1-11	0.44	86	0.48	0.50	0.96
ULTRASONIC WELD	1-09	0.73	151	0.95	0.89	1.66
COMPASS-ODOMETER	1-09	0.77	150	0.83	0.87	1.61
COMPASS-LASER WEL	1-09	0.44	86	0.48	0.50	0.96
GPS-U-SONIC WEL	1-09	0.44	86	0.48	0.50	0.96
ORIGA	1-13	0.44	86	0.48	0.50	0.96
LORAN	1-21	0.49	91	0.57	0.59	1.01
DECCA	1-20	0.84	96	0.93	1.02	1.75
RR-STATIONS	1-00	0.43	85	0.50	0.51	1.04
DIFF. ORIGA	1-13	0.43	85	0.50	0.51	1.04
DIFF. LORAN	1-21	0.49	91	0.57	0.59	1.01
DIFF. RR-STA.	1-17	0.43	85	0.50	0.51	1.04
RELAY ORIGA	101-00	70.70	141.40	140.70	141.40	141.40
RELAY LORAN	4-23	40.40	80.80	80.40	80.80	80.80
CLASS II BURIED RES. LOOPS	1-06	0.74	148	0.70	0.62	1.56
REFLECTING SIGNS	1-06	0.42	85	0.45	0.47	1.00
REFLECTING ROAD	1-06	0.42	85	0.45	0.47	1.00
X-BAND POST	1-06	0.42	85	0.45	0.47	1.00
HF, VHF POST	1-05	0.42	85	0.45	0.47	1.00
LF POST	1-06	0.42	85	0.45	0.47	1.00
LIGHT I-R POST	1-06	0.42	85	0.45	0.47	1.00
BURIED MAGNETS	1-06	0.42	85	0.45	0.47	1.00
ULTRASONIC POST	1-06	0.42	85	0.45	0.47	1.00
TRAFFIC SENSOR	1-06	0.42	85	0.45	0.47	1.00

V. Monterey Park, CA, City Cost Benefit Analysis Tables

Table 2-13. Monterey Park, CA, City AVM Physical Parameters

AREA IS 7.3 SQUARE MILES.  
 EAST WEST DISTANCE IS 4.6 MILES.  
 NORTH SOUTH DISTANCE IS 3 MILES.  
 TOTAL ROAD MILEAGE IS 101 MILES.  
 THE NUMBER OF INTERSECTIONS IS 596.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 826.  
 THERE ARE 15 CARS IN THE FLEET.  
 AND THERE ARE 0 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 14  
 FIRST SHIFT MIN. 4  
 SECOND SHIFT MAX. 14  
 SECOND SHIFT MIN. 4  
 THIRD SHIFT MAX. 14  
 THIRD SHIFT MIN. 4  
 THE NUMBER OF DISPATCHES IS 1  
 THE CITY WOULD REQUIRE 3 WIDE-BAND OF PULSE ANTENNA SITES AND 5 NARROW BAND FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

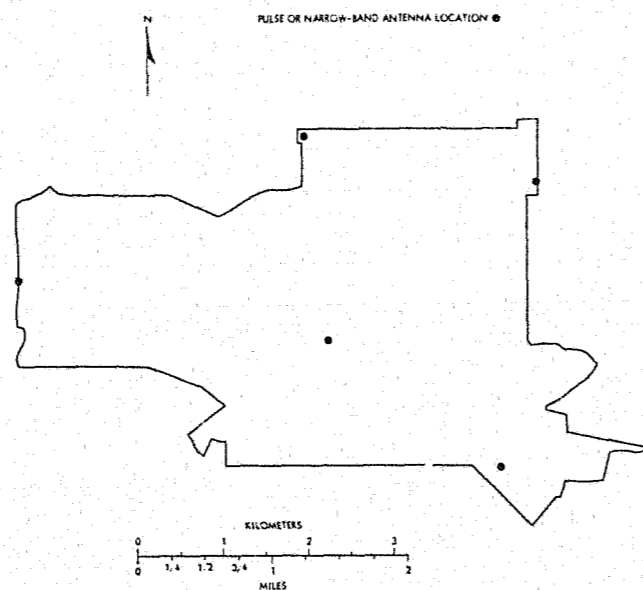


Figure 2-7. Monterey Park, CA, AVM Pulse or Narrow-Band Antennas

WIDE-BAND ANTENNA LOCATION

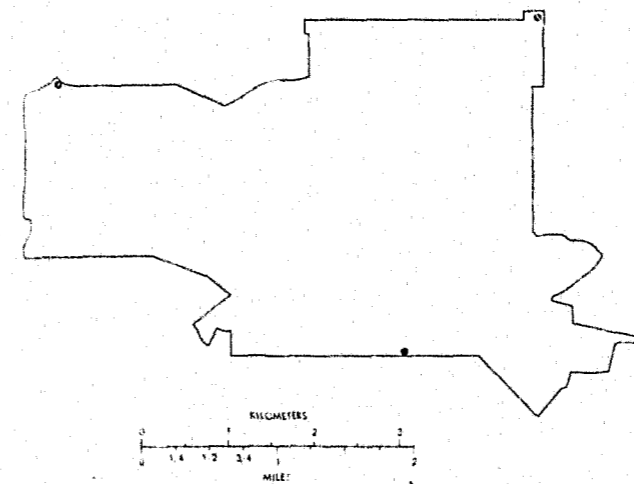


Figure 2-8. Monterey Park, CA, AVM Wide-Band Antenna Locations

Table 2-14. Monterey Park, CA, AVM Systems Cost Analyses

TECHNIQUE	TOTAL FLEET	SITE	RANGE	DIST	ON	TOTALS		
						VEHICLES	VEHICLES	VEHICLES
KEYBOARD	1-07	0	0	11	101	101	101	101
STYLUS MAP	1-12	0	0	12	100	100	100	100
2-ACCELEROMETERS	1-09	0	0	12	100	100	100	100
LASER VELOCIMTR	1-11	0	0	12	100	100	100	100
ULTRASONIC WELD	1-09	0	0	12	100	100	100	100
COMPASS-ODOMETER	1-09	0	0	12	100	100	100	100
COMPASS-LASER WEL	1-09	0	0	12	100	100	100	100
GPS-U-SONIC WEL	1-09	0	0	12	100	100	100	100
ORIGA	1-13	0	0	12	100	100	100	100
LORAN	1-21	0	0	12	100	100	100	100
DECCA	1-20	0	0	12	100	100	100	100
RR-STATIONS	1-00	0	0	12	100	100	100	100
DIFF. ORIGA	1-13	0	0	12	100	100	100	100
DIFF. LORAN	1-21	0	0	12	100	100	100	100
DIFF. RR-STA.	1-17	0	0	12	100	100	100	100
RELAY ORIGA	101-00	0	0	12	100	100	100	100
RELAY LORAN	4-23	0	0	12	100	100	100	100
CLASS II BURIED RES. LOOPS	1-06	199	4.6	340	101	299	701	499
REFLECTING SIGNS	1-06	41	0	62	100	119	161	161
REFLECTING ROAD	1-06	10	0	71	100	60	160	160
X-BAND POST	1-06	12	0	70	110	60	170	170
HF, VHF POST	1-05	10	0	70	100	10	110	110
LF POST	1-06	11	0	69	100	10	110	110
LIGHT I-R POST	1-06	11	0	69	100	10	110	110
BURIED MAGNETS	1-06	10	0	70	100	10	110	110
ULTRASONIC POST	1-06	11	0	69	100	10	110	110
TRAFFIC SENSOR	1-06	11	0	69	100	10	110	110
CLASS III WIDE-BAND FM PHASE	1-00	1	4.6	71	100	10	110	110
WIDE-BAND FM PHASE	1-00	1	4.6	71	100	10	110	110
PULSE T-O-METHOD	1-00	1	4.6	71	100	10	110	110
NOISE CORRELATION	1-00	1	4.6	71	100	10	110	110
DIRECTION FINDER	1-00	1	4.6	71	100	10	110	110
CLASS III TRAFFIC LOOPS	1-00	1	4.6	71	100	10	110	110
UNISIDE PARS	1-00	1	4.6	71	100	10	110	110
PHOTO I-R DETECT	1-00	1	4.6	71	100	10	110	110
ULTRASONIC DETECT	1-00	1	4.6	71	100	10	110	110

Table 2-15. Monterey Park, CA, AVM Polling Cycle Min/Max Times

CLASS I TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED					
		SYNC	SIMPLE	FMOD	RESOUNDANT	FMOD	FMOD
KEYBOARD	1-07	0.75	0.77	1.49	0.88	0.84	1.56
STYLUS MAP	1-12	0.43	0.44	0.80	0.57	0.51	1.04
2-ACCELEROMETERS	1-09	0.45	0.46	0.87	0.50	0.52	1.01
LASER VELOCIMTR	1-11	0.44	0.45	0.86	0.48	0.50	0.96
ULTRASONIC WELD	1-09	0.73	0.79	1.51	0.95	0.89	1.66
COMPASS-ODOMETER	1-09	0.77	0.78	1.50	0.83	0.87	1.61
COMPASS-LASER WEL	1-09	0.44	0.45	0.86	0.48	0.50	0.96
GPS-U-SONIC WEL	1-09	0.44	0.45	0.86	0.48	0.50	0.96
ORIGA	1-13	0.44	0.45	0.86	0.48	0.50	0.96
LORAN	1-21	0.49	0.50	0.91	0.57	0.59	1.01
DECCA	1-20	0.84	0.86	1.53	0.93	1.02	1.75
RR-STATIONS	1-00	0.43	0.44	0.85	0.50	0.51	1.04
DIFF. ORIGA	1-13	0.43	0.44	0.85	0.50	0.51	1.04
DIFF. LORAN	1-21	0.49	0.50	0.91	0.57	0.59	1.01
DIFF. RR-STA.	1-17	0.43	0.44	0.85	0.50	0.51	1.04
RELAY ORIGA	101-00	70.70	70.70	141.40	140.70	141.40	141.40
RELAY LORAN	4-23	40.40	40.40	80.80	80.40	80.80	80.80
CLASS II BURIED RES. LOOPS	1-06	0.74	0.76	1.48	0.70	0.62	1.56
REFLECTING SIGNS	1-06	0.42	0.43	0.85	0.45	0.47	1.00
REFLECTING ROAD	1-06	0.42	0.43	0.85	0.45	0.47	1.00
X-BAND POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
HF, VHF POST	1-05	0.42	0.43	0.85	0.45	0.47	1.00
LF POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
LIGHT I-R POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
BURIED MAGNETS	1-06	0.42	0.43	0.85	0.45	0.47	1.00
ULTRASONIC POST	1-06	0.42	0.43	0.85	0.45	0.47	1.00
TRAFFIC SENSOR	1-06	0.42	0.43	0.85	0.45	0.47	1.00

Table 2-16. Monterey Park, CA, AVM Accuracies and Cost Benefits

TECHNIQUE	TOTAL FLEET	SITE	RANGE	DIST	ON	TOTALS		
						VEHICLES	VEHICLES	VEHICLES
KEYBOARD	1-07	0	0	11	101	101	101	101
STYLUS MAP	1-12	0	0	12	100	100	100	100
2-ACCELEROMETERS	1-09	0	0	12	100	100	100	100
LASER VELOCIMTR	1-11	0	0	12	100	100	100	100
ULTRASONIC WELD	1-09	0	0	12	100	100	100	100
COMPASS-ODOMETER	1-09	0	0	12	100	100	100	100
COMPASS-LASER WEL	1-09	0	0	12	100	100	100	100
GPS-U-SONIC WEL	1-09	0	0	12	100	100	100	100
ORIGA	1-13	0	0	12	100	100	100	100
LORAN	1-21	0	0	12	100	100	100	100
DECCA	1-20	0	0	12	100	100	100	100
RR-STATIONS	1-00	0	0	12	100	100	100	100
DIFF. ORIGA	1-13	0	0	12	100	100	100	100
DIFF. LORAN	1-21	0	0	12	100	100	100	100
DIFF. RR-STA.	1-17	0	0	12	100	100	100	100
RELAY ORIGA	101-00	0	0	12	100	100	100	100
RELAY LORAN	4-23	0	0	12	100	100	100	100
CLASS II BURIED RES. LOOPS	1-06	199	4.6	340	101	299	701	499
REFLECTING SIGNS	1-06	41	0	62	100	119	161	161
REFLECTING ROAD	1-06	10	0	71	100	60	160	160
X-BAND POST	1-06	12	0	70	110	60	170	170
HF, VHF POST	1-05	10	0	70	100	10	110	110
LF POST	1-06	11	0	69	100	10	110	110
LIGHT I-R POST	1-06	11	0					



VI. Pasadena, CA, City AVM Cost Benefit Analysis Tables

Table 2-17. Pasadena, CA, City AVM Physical Parameters

AREA IS 23 SQUARE MILES.  
 EAST WEST DISTANCE IS 8 MILES.  
 NORTH-SOUTH DISTANCE IS 8 MILES.  
 TOTAL ROAD MILEAGE IS 350 MILES.  
 THE NUMBER OF INTERSECTIONS IS 1860.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 3720.  
 THERE ARE 35 CARS IN THE FLEET.  
 AND THERE ARE 0 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 10  
 FIRST SHIFT MIN. 10  
 SECOND SHIFT MAX. 10  
 SECOND SHIFT MIN. 10  
 THIRD SHIFT MAX. 10  
 THIRD SHIFT MIN. 10  
 THE NUMBER OF DISPATCHERS IS 1  
 THE CITY WOULD REQUIRE 3 WIDE-BAND OR PULSE ANTENNA SITES AND 7 NARROW BAND ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-18. Pasadena, CA, AVM Systems Cost Analyses

CLASS I	TECHNIQUE	QTY	UNIT PRICE	EST. COST	QTY	UNIT PRICE	EST. COST
KEYBOARD	1	100	100	100	1	100	100
STYLUS MAP	1	100	100	100	1	100	100
2-ACCELEROMETERS	1	100	100	100	1	100	100
LASER VELOCIMP	1	100	100	100	1	100	100
ULTRASONIC WELD	1	100	100	100	1	100	100
COMPASS ODOMETER	1	100	100	100	1	100	100
COMPASS-LASER VEL	1	100	100	100	1	100	100
DIFF. OMEGA	1	100	100	100	1	100	100
DIFF. LORAN	1	100	100	100	1	100	100
DIFF. RI-STA.	1	100	100	100	1	100	100
RELAY OMEGA	1	100	100	100	1	100	100
RELAY LORAN	1	100	100	100	1	100	100
CLASS II							
BURIED PEG. LOOPS	1	100	100	100	1	100	100
REFLECTING SIGNS	1	100	100	100	1	100	100
REFLECTING POND	1	100	100	100	1	100	100
W-BAND POST	1	100	100	100	1	100	100
HF. INF POST	1	100	100	100	1	100	100
LF POST	1	100	100	100	1	100	100
LIGHT I-R POST	1	100	100	100	1	100	100
SHIELDED MAGNETS	1	100	100	100	1	100	100
ULTRASONIC POST	1	100	100	100	1	100	100
TRAFFIC SENSOR	1	100	100	100	1	100	100
CLASS III							
IMP-BAND FM PHASE	1000	0	2411	2411	0	0	0
WID-BAND FM PHASE	1000	0	2264	2264	0	0	0
PULSE T-O-R ANTENNA	100	1	172	172	0	0	0
HOUSE CORRELATION	100	1	142	142	0	0	0
DIRECTION FINDER	700	0	1774	1774	0	0	0
CLASS IV							
TRAFFIC LOOPS	10	1	25	25	0	0	0
WIDE BAND RADIO	100	1	226	226	0	0	0
PHOTO I-R DETECT	30	1	66	66	0	0	0
ULTRASONIC DETECT	30	1	66	66	0	0	0

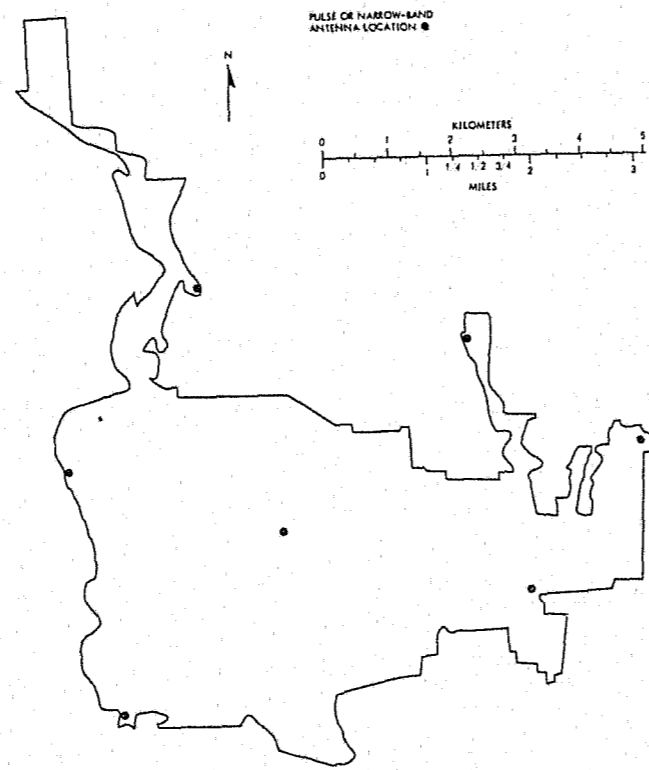


Figure 2-9. Pasadena, CA, AVM Pulse or Narrow-Band Antenna Locations

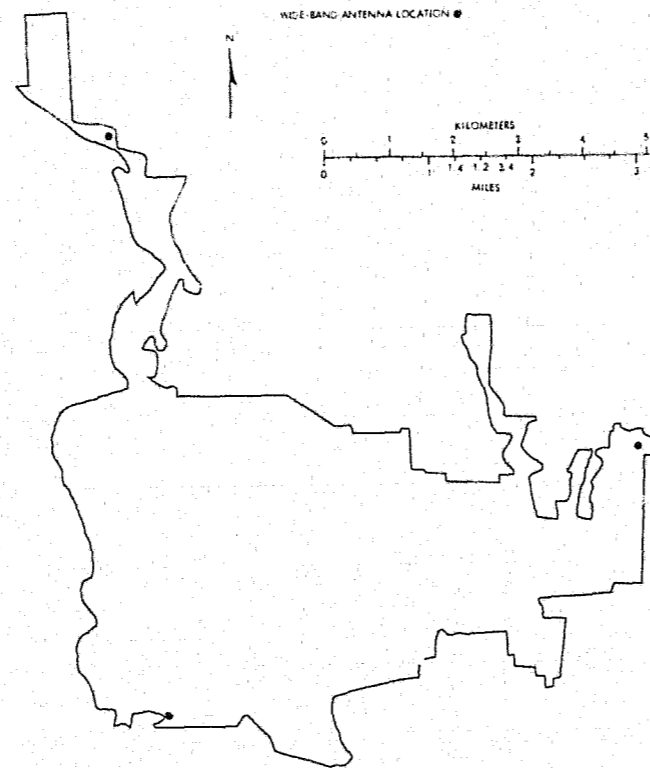


Figure 2-10. Pasadena, CA, AVM Wide-Band Antenna Locations

Table 2-19. Pasadena, CA, AVM Polling Cycle Min/Max Times

CLASS I	TECHNIQUE	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED.		REDUNDANT	
		SWC	SIMPLE	SWC	PRND
KEYBOARD	3.76	1.07	1.11	1.15	1.23
STYLUS MAP	3.92	1.12	1.16	1.19	1.24
2-ACCELEROMETERS	3.69	1.09	1.13	1.17	1.22
LASER VELOCIMP	3.87	1.11	1.15	1.19	1.23
ULTRASONIC WELD	3.83	1.11	1.15	1.19	1.23
COMPASS ODOMETER	3.62	1.09	1.13	1.17	1.22
COMPASS-LASER VEL	3.83	1.11	1.15	1.19	1.23
DIFF. OMEGA	3.69	1.09	1.13	1.17	1.22
DIFF. LORAN	4.25	1.21	1.25	1.29	1.34
DIFF. RI-STA.	4.11	1.17	1.21	1.25	1.30
RELAY OMEGA	353.50	101.00	101.04	102.08	201.00
RELAY LORAN	15.17	4.33	4.37	4.41	201.00
CLASS II					
BURIED PEG. LOOPS	3.78	1.08	1.12	1.16	1.21
REFLECTING SIGNS	3.70	1.03	1.07	1.11	1.16
REFLECTING POND	3.78	1.08	1.12	1.16	1.21
W-BAND POST	3.76	1.07	1.11	1.15	1.20
HF. INF POST	3.71	1.06	1.10	1.14	1.19
LF POST	3.76	1.07	1.11	1.15	1.20
LIGHT I-R POST	3.76	1.07	1.11	1.15	1.20
SHIELDED MAGNETS	3.72	1.06	1.10	1.14	1.19
ULTRASONIC POST	3.76	1.07	1.11	1.15	1.20
TRAFFIC SENSOR	3.76	1.07	1.11	1.15	1.20

Table 2-20. Pasadena, CA, AVM Accuracies and Cost Benefits

CLASS I	TECHNIQUE	QTY	EST. ACCURACIES IN VEHICLE AND ESTIMATED ROAD SHIFTS		EST. COST
			VEHICLES	ACCURACY	
KEYBOARD	1	100	100	100	100
STYLUS MAP	1	100	100	100	100
2-ACCELEROMETERS	1	100	100	100	100
LASER VELOCIMP	1	100	100	100	100
ULTRASONIC WELD	1	100	100	100	100
COMPASS ODOMETER	1	100	100	100	100
COMPASS-LASER VEL	1	100	100	100	100
DIFF. OMEGA	1000	0	2411	2411	2411
DIFF. LORAN	1000	0	2264	2264	2264
DIFF. RI-STA.	700	0	1774	1774	1774
RELAY OMEGA	100	0	2411	2411	2411
RELAY LORAN	100	0	2264	2264	2264
CLASS II					
BURIED PEG. LOOPS	10	1	25	25	25
REFLECTING SIGNS	10	1	25	25	25
REFLECTING POND	1	1	25	25	25
W-BAND POST	10	1	25	25	25
HF. INF POST	10	1	25	25	25
LF POST	10	1	25	25	25
LIGHT I-R POST	10	1	25	25	25
SHIELDED MAGNETS	10	1	25	25	25
ULTRASONIC POST	10	1	25	25	25
TRAFFIC SENSOR	10	1	25	25	25
CLASS III					
IMP-BAND FM PHASE	1000	0	2411	2411	2411
WID-BAND FM PHASE	1000	0	2264	2264	2264
PULSE T-O-R ANTENNA	100	1	172	172	172
HOUSE CORRELATION	100	1	142	142	142
DIRECTION FINDER	700	0	1774	1774	1774
CLASS IV					
TRAFFIC LOOPS	10	1	25	25	25
WIDE BAND RADIO	100	1	226	226	226
PHOTO I-R DETECT	30	1	66	66	66
ULTRASONIC DETECT	30	1	66	66	66

VII. San Diego, CA, City AVM Cost Benefit Analysis Tables

Table 2-21. San Diego, CA, City AVM Physical Parameters

AREA IS 331 SQUARE MILES.  
 EAST WEST DISTANCE IS 23.6 MILES.  
 NORTH-SOUTH DISTANCE IS 41.2 MILES.  
 TOTAL ROAD MILEAGE IS 1945 MILES.  
 THE NUMBER OF INTERSECTIONS IS 13700.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 27400.  
 THERE ARE 300 CARS IN THE FLEET  
 AND THERE ARE 52 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 66  
 FIRST SHIFT MIN. 66  
 SECOND SHIFT MAX. 95  
 SECOND SHIFT MIN. 95  
 THIRD SHIFT MAX. 60  
 THIRD SHIFT MIN. 60

THE CITY WOULD REQUIRE 23 WIDE-BAND OR PULSE T-O-R ANTENNA SITES AND 85 NARROW BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADII.



VIII. Los Angeles, CA, City AVM Cost Benefit Analysis Tables

Table 2-26. Los Angeles, CA, Central Bureau AVM Physical Parameters

AREA IS 37.5 SQUARE MILES.  
 DIST. NEXT DISTANCE IS 9 MILES.  
 NORTH-SOUTH DISTANCE IS 13 MILES.  
 TOTAL ROAD MILEAGE IS 1152 MILES.  
 THE NUMBER OF INTERSECTIONS IS 3570.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 14140.  
 THERE ARE 157 CARS IN THE FLEET.  
 AND THERE ARE 0 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT (MORNING) 60  
 SECOND SHIFT (MID.) 90  
 THIRD SHIFT (EVENING) 100  
 THE NUMBER OF DISPATCHERS IS 2.  
 THE CITY WOULD REQUIRE 2 WIDE-BAND OR PULSE ANTENNA SITES AND 14 NARROW-BAND ANTENNA SITES FOR 1 AND 3 MILE RADIUS COVERAGE.

Table 2-27. Los Angeles, CA, Central Bureau AVM Systems Cost Analyses

CLASS I TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	THEO. ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVING
KEYBOARD	10.95	10.95	10.95	10.95	10.95
STYLUS MAP	17.53	11.20	11.27	22.27	12.40
2-ACCELEROMETERS	17.17	11.20	11.47	22.00	12.40
LASER VELOCIMTR	17.30	11.20	11.60	22.00	12.40
ULTRASONIC WELD	17.17	10.93	11.47	22.00	12.40
COMPASS ODOMETER	17.17	10.93	11.47	22.00	12.40
COMPASS LASER WEL	17.17	10.93	11.47	22.00	12.40
COMPASS D-SOUND WEL	17.17	10.93	11.47	22.00	12.40
OMEGA	13.73	11.20	11.47	22.00	12.40
LORAN	14.05	11.20	11.47	22.00	12.40
DECCA	14.04	11.20	11.47	22.00	12.40
NAV-STATIONS	14.96	11.20	11.47	22.00	12.40
DIFF. OMEGA	14.53	11.20	11.47	22.00	12.40
DIFF. LORAN	14.05	11.20	11.47	22.00	12.40
DIFF. NAV-STN.	14.48	11.20	11.47	22.00	12.40
RELAY OMEGA	15.57	1010.00	1010.00	1010.00	1010.00
RELAY LORAN	14.05	42.22	42.22	42.22	42.22
CLASS II					
BURIED RES. LOOPS	17.27	11.00	11.27	22.00	12.40
REFLECTING SIGNS	17.27	11.00	11.27	22.00	12.40
REFLECTING ROAD	17.27	11.00	11.27	22.00	12.40
2-BAND POST	17.17	10.93	11.47	22.00	12.40
HF VHF POST	14.96	10.93	11.47	22.00	12.40
LF POST	17.17	10.93	11.47	22.00	12.40
LIGHT I-R POST	17.27	11.00	11.27	22.00	12.40
BURIED MAGNETS	17.27	11.00	11.27	22.00	12.40
ULTRASONIC POST	17.17	10.93	11.47	22.00	12.40
TRAFFIC SENSOR	17.17	10.93	11.47	22.00	12.40
CLASS III					
NAR-BAND FM PHASE	1000	0	2000	1000	1000
MID-BAND FM PHASE	1000	0	2000	1000	1000
PULSE T-D-NARROWBAND	100	4	100	100	100
NOISE CORRELATION	100	4	100	100	100
DIRECTION FINDER	100	4	100	100	100
CLASS IV					
TRAFFIC LOOPS	10	0	10	10	10
PHOTO I-R DETECT	10	0	10	10	10
ULTRASONIC DETECT	10	0	10	10	10

Table 2-28. Los Angeles, CA, Central Bureau AVM Polling Cycle Times

CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED.

CLASS I TECHNIQUE	TOTAL FLEET	SYNC. POL	PRND	SYNC. POL	PRND
KEYBOARD	16.95	10.73	11.27	11.47	12.53
STYLUS MAP	17.53	11.20	11.47	11.47	12.40
2-ACCELEROMETERS	17.17	11.20	11.47	11.47	12.40
LASER VELOCIMTR	17.30	11.20	11.60	11.47	12.40
ULTRASONIC WELD	17.17	10.93	11.47	11.47	12.40
COMPASS ODOMETER	17.17	10.93	11.47	11.47	12.40
COMPASS LASER WEL	17.17	10.93	11.47	11.47	12.40
COMPASS D-SOUND WEL	17.17	10.93	11.47	11.47	12.40
OMEGA	13.73	11.20	11.47	11.47	12.40
LORAN	14.05	11.20	11.47	11.47	12.40
DECCA	14.04	11.20	11.47	11.47	12.40
NAV-STATIONS	14.96	11.20	11.47	11.47	12.40
DIFF. OMEGA	14.53	11.20	11.47	11.47	12.40
DIFF. LORAN	14.05	11.20	11.47	11.47	12.40
DIFF. NAV-STN.	14.48	11.20	11.47	11.47	12.40
RELAY OMEGA	15.57	1010.00	1010.00	1010.00	1010.00
RELAY LORAN	14.05	42.22	42.22	42.22	42.22
CLASS II					
BURIED RES. LOOPS	17.27	11.00	11.27	11.47	12.40
REFLECTING SIGNS	17.27	11.00	11.27	11.47	12.40
REFLECTING ROAD	17.27	11.00	11.27	11.47	12.40
2-BAND POST	17.17	10.93	11.47	11.47	12.40
HF VHF POST	14.96	10.93	11.47	11.47	12.40
LF POST	17.17	10.93	11.47	11.47	12.40
LIGHT I-R POST	17.27	11.00	11.27	11.47	12.40
BURIED MAGNETS	17.27	11.00	11.27	11.47	12.40
ULTRASONIC POST	17.17	10.93	11.47	11.47	12.40
TRAFFIC SENSOR	17.17	10.93	11.47	11.47	12.40

Table 2-29. Los Angeles, CA, Central Bureau AVM Accuracies and Cost Benefits with One Radio Channel

CLASS I TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	THEO. ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVING
KEYBOARD	10.95	10.95	10.95	10.95	10.95
STYLUS MAP	17.53	11.20	11.47	22.27	12.40
2-ACCELEROMETERS	17.17	11.20	11.47	22.00	12.40
LASER VELOCIMTR	17.30	11.20	11.60	22.00	12.40
ULTRASONIC WELD	17.17	10.93	11.47	22.00	12.40
COMPASS ODOMETER	17.17	10.93	11.47	22.00	12.40
COMPASS LASER WEL	17.17	10.93	11.47	22.00	12.40
COMPASS D-SOUND WEL	17.17	10.93	11.47	22.00	12.40
OMEGA	13.73	11.20	11.47	22.00	12.40
LORAN	14.05	11.20	11.47	22.00	12.40
DECCA	14.04	11.20	11.47	22.00	12.40
NAV-STATIONS	14.96	11.20	11.47	22.00	12.40
DIFF. OMEGA	14.53	11.20	11.47	22.00	12.40
DIFF. LORAN	14.05	11.20	11.47	22.00	12.40
DIFF. NAV-STN.	14.48	11.20	11.47	22.00	12.40
RELAY OMEGA	15.57	1010.00	1010.00	1010.00	1010.00
RELAY LORAN	14.05	42.22	42.22	42.22	42.22
CLASS II					
BURIED RES. LOOPS	17.27	11.00	11.27	22.00	12.40
REFLECTING SIGNS	17.27	11.00	11.27	22.00	12.40
REFLECTING ROAD	17.27	11.00	11.27	22.00	12.40
2-BAND POST	17.17	10.93	11.47	22.00	12.40
HF VHF POST	14.96	10.93	11.47	22.00	12.40
LF POST	17.17	10.93	11.47	22.00	12.40
LIGHT I-R POST	17.27	11.00	11.27	22.00	12.40
BURIED MAGNETS	17.27	11.00	11.27	22.00	12.40
ULTRASONIC POST	17.17	10.93	11.47	22.00	12.40
TRAFFIC SENSOR	17.17	10.93	11.47	22.00	12.40
CLASS III					
NAR-BAND FM PHASE	1000	0	2000	1000	1000
MID-BAND FM PHASE	1000	0	2000	1000	1000
PULSE T-D-NARROWBAND	100	4	100	100	100
NOISE CORRELATION	100	4	100	100	100
DIRECTION FINDER	100	4	100	100	100
CLASS IV					
TRAFFIC LOOPS	10	0	10	10	10
PHOTO I-R DETECT	10	0	10	10	10
ULTRASONIC DETECT	10	0	10	10	10

Table 2-30. Los Angeles, CA, Central Bureau AVM Accuracies and Cost Benefits with Two Radio Channels

CLASS I TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	THEO. ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVING
KEYBOARD	10.95	10.95	10.95	10.95	10.95
STYLUS MAP	17.53	11.20	11.47	22.27	12.40
2-ACCELEROMETERS	17.17	11.20	11.47	22.00	12.40
LASER VELOCIMTR	17.30	11.20	11.60	22.00	12.40
ULTRASONIC WELD	17.17	10.93	11.47	22.00	12.40
COMPASS ODOMETER	17.17	10.93	11.47	22.00	12.40
COMPASS LASER WEL	17.17	10.93	11.47	22.00	12.40
COMPASS D-SOUND WEL	17.17	10.93	11.47	22.00	12.40
OMEGA	13.73	11.20	11.47	22.00	12.40
LORAN	14.05	11.20	11.47	22.00	12.40
DECCA	14.04	11.20	11.47	22.00	12.40
NAV-STATIONS	14.96	11.20	11.47	22.00	12.40
DIFF. OMEGA	14.53	11.20	11.47	22.00	12.40
DIFF. LORAN	14.05	11.20	11.47	22.00	12.40
DIFF. NAV-STN.	14.48	11.20	11.47	22.00	12.40
RELAY OMEGA	15.57	1010.00	1010.00	1010.00	1010.00
RELAY LORAN	14.05	42.22	42.22	42.22	42.22
CLASS II					
BURIED RES. LOOPS	17.27	11.00	11.27	22.00	12.40
REFLECTING SIGNS	17.27	11.00	11.27	22.00	12.40
REFLECTING ROAD	17.27	11.00	11.27	22.00	12.40
2-BAND POST	17.17	10.93	11.47	22.00	12.40
HF VHF POST	14.96	10.93	11.47	22.00	12.40
LF POST	17.17	10.93	11.47	22.00	12.40
LIGHT I-R POST	17.27	11.00	11.27	22.00	12.40
BURIED MAGNETS	17.27	11.00	11.27	22.00	12.40
ULTRASONIC POST	17.17	10.93	11.47	22.00	12.40
TRAFFIC SENSOR	17.17	10.93	11.47	22.00	12.40
CLASS III					
NAR-BAND FM PHASE	1000	0	2000	1000	1000
MID-BAND FM PHASE	1000	0	2000	1000	1000
PULSE T-D-NARROWBAND	100	4	100	100	100
NOISE CORRELATION	100	4	100	100	100
DIRECTION FINDER	100	4	100	100	100
CLASS IV					
TRAFFIC LOOPS	10	0	10	10	10
PHOTO I-R DETECT	10	0	10	10	10
ULTRASONIC DETECT	10	0	10	10	10

Table 2-31. Los Angeles, CA, Central Bureau AVM Accuracies and Cost Benefits with Three Radio Channels

CLASS I TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	THEO. ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVING
KEYBOARD	10.95	10.95	10.95	10.95	10.95
STYLUS MAP	17.53	11.20	11.47	22.27	12.40
2-ACCELEROMETERS	17.17	11.20	11.47	22.00	12.40
LASER VELOCIMTR	17.30	11.20	11.60	22.00	12.40
ULTRASONIC WELD	17.17	10.93	11.47	22.00	12.40
COMPASS ODOMETER	17.17	10.93	11.47	22.00	12.40
COMPASS LASER WEL	17.17	10.93	11.47	22.00	12.40
COMPASS D-SOUND WEL	17.17	10.93	11.47	22.00	12.40
OMEGA	13.73	11.20	11.47	22.00	12.40
LORAN	14.05	11.20	11.47	22.00	12.40
DECCA	14.04	11.20	11.47	22.00	12.40
NAV-STATIONS	14.96	11.20	11.47	22.00	12.40
DIFF. OMEGA	14.53	11.20	11.47	22.00	12.40
DIFF. LORAN	14.05	11.20	11.47	22.00	12.40
DIFF. NAV-STN.	14.48	11.20	11.47	22.00	12.40
RELAY OMEGA	15.57	1010.00	1010.00	1010.00	1010.00
RELAY LORAN	14.05	42.22	42.22	42.22	42.22
CLASS II					
BURIED RES. LOOPS	17.27	11.00	11.27	22.00	12.40
REFLECTING SIGNS	17.27	11.00	11.27	22.00	12.40
REFLECTING ROAD	17.27	11.00	11.27	22.00	12.40
2-BAND POST	17.17	10.93	11.47	22.00	12.40
HF VHF POST	14.96	10.93	11.47	22.00	12.40
LF POST	17.17	10.93	11.47	22.00	12.40
LIGHT I-R POST	17.27	11.00	11.27	22.00	12.40
BURIED MAGNETS	17.27	11.00	11.27	22.00	12.40
ULTRASONIC POST	17.17	10.93	11.47	22.00	12.40
TRAFFIC SENSOR	17.17	10.93	11.47	22.00	12.40
CLASS III					
NAR-BAND FM PHASE	1000	0	2000	1000	1000
MID-BAND FM PHASE	1000	0	2000	1000	1000
PULSE T-D-NARROWBAND	100	4	100	100	100
NOISE CORRELATION	100	4	100	100	100
DIRECTION FINDER	100	4	100	100	100
CLASS IV					
TRAFFIC LOOPS	10	0	10	10	10
PHOTO I-R DETECT	10	0	10	10	10
ULTRASONIC DETECT	10	0	10	10	10

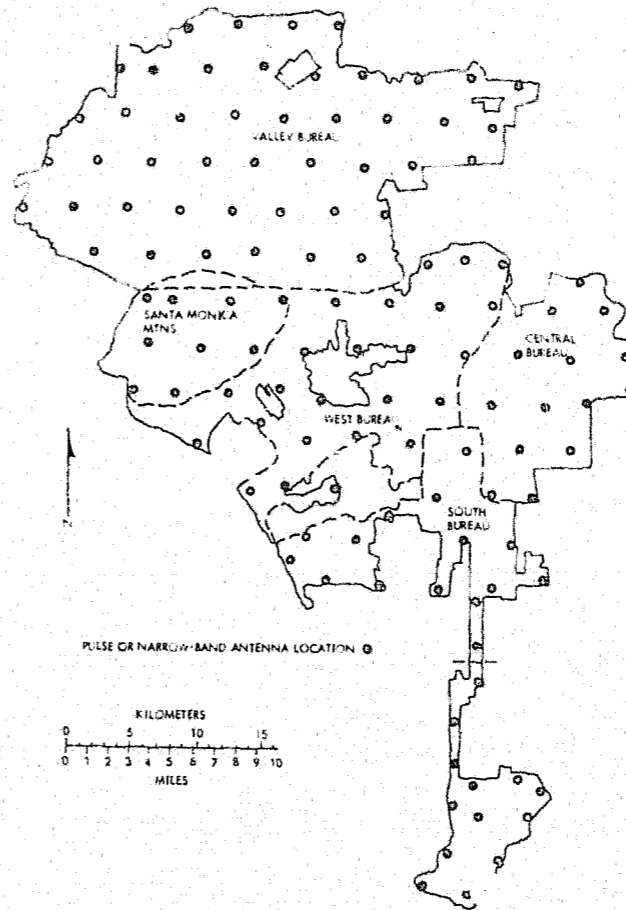


Figure 2-13. Los Angeles, CA, AVM Pulse or Narrow-Band Antennas

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Table 2-32. Los Angeles, South Bureau  
AVM Physical Parameters

AREA IS 55.2 SQUARE MILES.  
EAST WEST DISTANCE IS 9 MILES.  
NORTH SOUTH DISTANCE IS 23 MILES.  
TOTAL ROAD MILEAGE IS 978 MILES.  
THE NUMBER OF INTERSECTIONS IS 6090.  
THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 12180.  
THERE ARE 165 CARS IN THE FLEET.  
AND THERE ARE 0 MOTORCYCLES.  
THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
FIRST SHIFT MAX. 63  
FIRST SHIFT MIN. 53  
SECOND SHIFT MAX. 94  
SECOND SHIFT MIN. 84  
THIRD SHIFT MAX. 104  
THIRD SHIFT MIN. 84  
THE NUMBER OF DISPATCHERS IS 2  
THE CITY WOULD REQUIRE 5 WIDE-BAND OF  
PULSE ANTENNA SITES AND 23 NARROW BAND  
FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-34. Los Angeles, South Bureau  
AVM Polling Cycle Times

CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED.

CLASS I TECHNIQUE	TOTAL FLEET	SIMPLE				REDUNDANT				
		SYNC VOL	PRND	SYNC VOL	PRND	SYNC VOL	PRND	SYNC VOL	PRND	
KEYBOARD	17-71	11-72	22-67	11-93	13-84	24-34	11-55	6-88	6-64	12-51
STYLUS MAP	18-48	5-94	12-20	23-16	12-90	14-01	25-51	5-94	6-57	13-00
2-ACCELEROMETERS	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
LASER VELOCINTP	18-26	11-31	12-06	22-62	12-62	13-73	25-24	5-37	6-15	12-73
ULTRASONIC VELD	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
COMPASS/ODOMETER	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
COMPASS/LASER VEL	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
COMPASS-U-SONIC VEL	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
OMEGA	19-47	12-27	12-83	23-78	14-14	15-25	26-76	6-25	6-54	12-12
LORAN	20-02	12-62	13-17	24-13	14-84	15-95	27-46	6-43	6-71	12-30
DECCA	19-88	12-48	13-04	23-99	14-56	15-67	27-18	6-36	6-64	12-23
AM-STATIONS	17-02	11-23	11-79	22-74	12-86	13-17	24-68	5-72	6-01	11-52
DIFF. OMEGA	19-47	12-27	12-83	23-78	14-14	15-25	26-76	6-25	6-54	12-12
DIFF. LORAN	20-02	12-62	13-17	24-13	14-84	15-95	27-46	6-43	6-71	12-30
DIFF. AM-STA.	19-36	12-28	12-76	23-71	14-81	15-12	26-62	6-22	6-50	12-08
RELAY OMEGA	1666-58	1050-48	1050-95	1061-91	2090-48	2091-51	2103-02	45-87	45-87	56-58
RELAY LORAN	71-58	535-38	535-59	541-17	1065-38	1065-87	1071-73	22-97	23-25	23-25
CLASS II										
BURIED RES. LOOPS	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
REFLECTING SIGNS	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
REFLECTING ROAD	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
X-BAND POST	17-93	11-30	11-86	22-81	12-20	13-31	24-82	5-76	6-04	11-63
HF VHF POST	17-71	11-16	11-72	22-67	11-93	13-04	24-54	5-69	5-97	11-55
LF POST	17-93	11-30	11-86	22-81	12-20	13-31	24-82	5-76	6-04	11-63
LIGHT I-R POST	17-93	11-30	11-86	22-81	12-20	13-31	24-82	5-76	6-04	11-63
BURIED MAGNETS	18-04	11-37	11-93	22-88	12-34	13-45	24-96	5-79	6-88	12-72
ULTRASONIC POST	17-93	11-30	11-86	22-81	12-20	13-31	24-82	5-76	6-04	11-63
TRAFFIC SENSOR	17-93	11-30	11-86	22-81	12-20	13-31	24-82	5-76	6-04	11-63

Table 2-36. Los Angeles, South Bureau  
AVM Accuracies and Cost Benefits  
with Two Radio Channels

LA-SOUTH BUREAU

CLASS I TECHNIQUE	THOUSANDS OF \$ ESTIMATED SAVINGS	SYSTEM ACCURACIES IN VEHICLES AND ESTIMATED \$1000 SAVINGS			
		ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED
KEYBOARD	17-71	11-72	22-67	11-93	13-84
STYLUS MAP	18-48	5-94	12-20	23-16	12-90
2-ACCELEROMETERS	18-04	11-37	11-93	22-88	12-34
LASER VELOCINTP	18-26	11-31	12-06	22-62	12-62
ULTRASONIC VELD	18-04	11-37	11-93	22-88	12-34
COMPASS/ODOMETER	18-04	11-37	11-93	22-88	12-34
COMPASS/LASER VEL	18-04	11-37	11-93	22-88	12-34
COMPASS-U-SONIC VEL	18-04	11-37	11-93	22-88	12-34
OMEGA	19-47	12-27	12-83	23-78	14-14
LORAN	20-02	12-62	13-17	24-13	14-84
DECCA	19-88	12-48	13-04	23-99	14-56
AM-STATIONS	17-02	11-23	11-79	22-74	12-86
DIFF. OMEGA	19-47	12-27	12-83	23-78	14-14
DIFF. LORAN	20-02	12-62	13-17	24-13	14-84
DIFF. AM-STA.	19-36	12-28	12-76	23-71	14-81
RELAY OMEGA	1666-58	1050-48	1050-95	1061-91	2090-48
RELAY LORAN	71-58	535-38	535-59	541-17	1065-38
CLASS II					
BURIED RES. LOOPS	18-04	11-37	11-93	22-88	12-34
REFLECTING SIGNS	18-04	11-37	11-93	22-88	12-34
REFLECTING ROAD	18-04	11-37	11-93	22-88	12-34
X-BAND POST	17-93	11-30	11-86	22-81	12-20
HF VHF POST	17-71	11-16	11-72	22-67	11-93
LF POST	17-93	11-30	11-86	22-81	12-20
LIGHT I-R POST	17-93	11-30	11-86	22-81	12-20
BURIED MAGNETS	18-04	11-37	11-93	22-88	12-34
ULTRASONIC POST	17-93	11-30	11-86	22-81	12-20
TRAFFIC SENSOR	17-93	11-30	11-86	22-81	12-20

Table 2-38. Los Angeles, West Bureau  
AVM Physical Parameters

AREA IS 133.2 SQUARE MILES.  
EAST WEST DISTANCE IS 19 MILES.  
NORTH SOUTH DISTANCE IS 18 MILES.  
TOTAL ROAD MILEAGE IS 1677 MILES.  
THE NUMBER OF INTERSECTIONS IS 9400.  
THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 18800.  
THERE ARE 183 CARS IN THE FLEET.  
AND THERE ARE 0 MOTORCYCLES.  
THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
FIRST SHIFT MAX. 59  
FIRST SHIFT MIN. 39  
SECOND SHIFT MAX. 105  
SECOND SHIFT MIN. 94  
THIRD SHIFT MAX. 117  
THIRD SHIFT MIN. 90  
THE NUMBER OF DISPATCHERS IS 2  
THE CITY WOULD REQUIRE 7 WIDE-BAND OF  
PULSE ANTENNA SITES AND 44 NARROW BAND  
FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-33. Los Angeles, South Bureau  
AVM Systems Cost Analyses

LA-SOUTH BUREAU

CLASS I TECHNIQUE	THOUSANDS OF \$ ESTIMATED SAVINGS	SYSTEM ACCURACIES IN VEHICLES AND ESTIMATED \$1000 SAVINGS			
		ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED
KEYBOARD	17-71	11-72	22-67	11-93	13-84
STYLUS MAP	18-48	5-94	12-20	23-16	12-90
2-ACCELEROMETERS	18-04	11-37	11-93	22-88	12-34
LASER VELOCINTP	18-26	11-31	12-06	22-62	12-62
ULTRASONIC VELD	18-04	11-37	11-93	22-88	12-34
COMPASS/ODOMETER	18-04	11-37	11-93	22-88	12-34
COMPASS/LASER VEL	18-04	11-37	11-93	22-88	12-34
COMPASS-U-SONIC VEL	18-04	11-37	11-93	22-88	12-34
OMEGA	19-47	12-27	12-83	23-78	14-14
LORAN	20-02	12-62	13-17	24-13	14-84
DECCA	19-88	12-48	13-04	23-99	14-56
AM-STATIONS	17-02	11-23	11-79	22-74	12-86
DIFF. OMEGA	19-47	12-27	12-83	23-78	14-14
DIFF. LORAN	20-02	12-62	13-17	24-13	14-84
DIFF. AM-STA.	19-36	12-28	12-76	23-71	14-81
RELAY OMEGA	1666-58	1050-48	1050-95	1061-91	2090-48
RELAY LORAN	71-58	535-38	535-59	541-17	1065-38
CLASS II					
BURIED RES. LOOPS	18-04	11-37	11-93	22-88	12-34
REFLECTING SIGNS	18-04	11-37	11-93	22-88	12-34
REFLECTING ROAD	18-04	11-37	11-93	22-88	12-34
X-BAND POST	17-93	11-30	11-86	22-81	12-20
HF VHF POST	17-71	11-16	11-72	22-67	11-93
LF POST	17-93	11-30	11-86	22-81	12-20
LIGHT I-R POST	17-93	11-30	11-86	22-81	12-20
BURIED MAGNETS	18-04	11-37	11-93	22-88	12-34
ULTRASONIC POST	17-93	11-30	11-86	22-81	12-20
TRAFFIC SENSOR	17-93	11-30	11-86	22-81	12-20

Table 2-35. Los Angeles, South Bureau  
AVM Accuracies and Cost Benefits  
with One Radio Channel

LA-SOUTH BUREAU

CLASS I TECHNIQUE	THOUSANDS OF \$ ESTIMATED SAVINGS	SYSTEM ACCURACIES IN VEHICLES AND ESTIMATED \$1000 SAVINGS			
		ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED
KEYBOARD	17-71	11-72	22-67	11-93	13-84
STYLUS MAP	18-48	5-94	12-20	23-16	12-90
2-ACCELEROMETERS	18-04	11-37	11-93	22-88	12-34
LASER VELOCINTP	18-26	11-31	12-06	22-62	12-62
ULTRASONIC VELD	18-04	11-37	11-93	22-88	12-34
COMPASS/ODOMETER	18-04	11-37	11-93	22-88	12-34
COMPASS/LASER VEL	18-04	11-37	11-93	22-88	12-34
COMPASS-U-SONIC VEL	18-04	11-37	11-93	22-88	12-34
OMEGA	19-47	12-27	12-83	23-78	14-14
LORAN	20-02	12-62	13-17	24-13	14-84
DECCA	19-88	12-48	13-04	23-99	14-56
AM-STATIONS	17-02	11-23	11-79	22-74	12-86
DIFF. OMEGA	19-47	12-27	12-83	23-78	14-14
DIFF. LORAN	20-02	12-62	13-17	24-13	14-84
DIFF. AM-STA.	19-36	12-28	12-76	23-71	14-81
RELAY OMEGA	1666-58	1050-48	1050-95	1061-91	2090-48
RELAY LORAN	71-58	535-38	535-59	541-17	1065-38
CLASS II					
BURIED RES. LOOPS	18-04	11-37	11-93	22-88	12-34
REFLECTING SIGNS	18-04	11-37	11-93	22-88	12-34
REFLECTING ROAD	18-04	11-37	11-93	22-88	12-34
X-BAND POST	17-93	11-30	11-86	22-81	12-20
HF VHF POST	17-71	11-16	11-72	22-67	11-93
LF POST	17-93	11-30	11-86	22-81	12-20
LIGHT I-R POST	17-93	11-30	11-86	22-81	12-20
BURIED MAGNETS	18-04	11-37	11-93	22-88	12-34
ULTRASONIC POST	17-93	11-30	11-86	22-81	12-20
TRAFFIC SENSOR	17-93	11-30	11-86	22-81	12-20

Table 2-37. Los Angeles, South Bureau  
AVM Accuracies and Cost Benefits  
with Three Radio Channels

LA-SOUTH BUREAU

CLASS I TECHNIQUE	THOUSANDS OF \$ ESTIMATED SAVINGS	SYSTEM ACCURACIES IN VEHICLES AND ESTIMATED \$1000 SAVINGS			
		ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED
KEYBOARD	17-71	11-72	22-67	11-93	13-84
STYLUS MAP	18-48	5-94	12-20	23-16	12-90
2-ACCELEROMETERS	18-04	11-37	11-93	22-88	12-34
LASER VELOCINTP	18-26	11-31	12-06	22-62	12-62
ULTRASONIC VELD	18-04	11-37	11-93	22-88	12-34
COMPASS/ODOMETER	18-04	11-37	11-93	22-88	12-34
COMPASS/LASER VEL	18-04	11-37	11-93	22-88	12-34
COMPASS-U-SONIC VEL	18-04	11-37	11-93	22-88	12-34
OMEGA	19-47	12-27	12-83	23-78	14-14
LORAN	20-02	12-62	13-17	24-13	14-84
DECCA	19-88	12-48	13-04	23-99	14-56
AM-STATIONS	17-02	11-23	11-79	22-74	12-86

Table 2-40. Los Angeles, West Bureau  
AVM Polling Cycle Times

CYCLE TIME IN SECONDS TO POLL INR AND MIN UNITS DEPLOYED.

CLASS I TECHNIQUE	TOTAL FLEET	INR	MIN	REDUANT	FRID
KEYBOARD	33	459	157	0.0	0.0
STYLUS MAP	30	475	163	1.9	0.0
2-ACCELEROMETERS	34	467	160	1.9	0.0
LASER VELOCINTP	13	459	157	2.0	0.0
ULTRASONIC VELD	40	469	161	1.9	0.0
COMPASS/ODOMETER	20	460	157	2.0	0.0
COMPASS/LASER VEL	15	456	156	2.0	0.0
CHPSS-U-SONIC VEL	17	458	156	2.0	0.0
OMEGA	1600	4227	4037	0.0	0.0
LORAN	160	434	404	0.2	0.0
DECCA	200	510	487	0.5	0.0
AM-STATIONS	200	509	487	0.5	0.0
DIFF. OMEGA	160	421	404	0.2	0.0
DIFF. LORAN	400	1177	1113	0.0	0.0
DIFF. AM-STA.	200	623	539	0.0	0.0
RELAY OMEGA	500	40137	13525	0.0	0.0
RELAY LORAN	800	2164	2294	0.0	0.0

Table 2-41. Los Angeles, West Bureau  
AVM Accuracies and Cost Benefits  
with One Radio Channel

LA-NORTH BUREAU

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVINGS	ESTIMATED 5-YEAR SAVING
KEYBOARD	33	7	459	157	2.0	0.0
STYLUS MAP	30	7	475	163	1.9	0.0
2-ACCELEROMETERS	34	7	467	160	1.9	0.0
LASER VELOCINTP	13	8	459	157	2.0	0.0
ULTRASONIC VELD	40	7	469	161	1.9	0.0
COMPASS/ODOMETER	20	8	460	157	2.0	0.0
COMPASS/LASER VEL	15	8	456	156	2.0	0.0
CHPSS-U-SONIC VEL	17	8	458	156	2.0	0.0
OMEGA	1600	0	4227	4037	0.0	0.0
LORAN	160	4	534	404	0.2	0.0
DECCA	200	3	510	487	0.5	0.0
AM-STATIONS	200	3	509	487	0.5	0.0
DIFF. OMEGA	160	4	521	404	0.2	0.0
DIFF. LORAN	400	1	1177	1113	0.0	0.0
DIFF. AM-STA.	200	0	623	539	0.0	0.0
RELAY OMEGA	500	0	40137	13525	0.0	0.0
RELAY LORAN	800	0	2164	2294	0.0	0.0

Table 2-42. Los Angeles, West Bureau  
AVM Accuracies and Cost Benefits  
with Two Radio Channels

LA-NORTH BUREAU

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVINGS	ESTIMATED 5-YEAR SAVING
KEYBOARD	33	7	236	94	2.2	2.5
STYLUS MAP	30	7	244	80	2.3	2.3
2-ACCELEROMETERS	34	7	240	98	2.2	2.4
LASER VELOCINTP	13	8	236	77	2.3	2.5
ULTRASONIC VELD	40	7	241	108	2.2	2.4
COMPASS/ODOMETER	20	8	236	77	2.3	2.5
COMPASS/LASER VEL	15	8	234	77	2.3	2.5
CHPSS-U-SONIC VEL	17	8	235	77	2.3	2.5
OMEGA	1600	0	4106	3922	0.0	0.0
LORAN	160	4	411	393	0.9	0.0
DECCA	200	3	495	473	0.5	0.0
AM-STATIONS	200	3	493	471	0.5	0.0
DIFF. OMEGA	160	4	411	392	0.9	0.0
DIFF. LORAN	400	1	1140	1094	0.0	0.0
DIFF. AM-STA.	250	2	596	569	0.1	0.0
RELAY OMEGA	500	0	20440	6450	0.0	0.0
RELAY LORAN	800	0	2340	2218	0.0	0.0

Table 2-43. Los Angeles, West Bureau  
AVM Accuracies and Cost Benefits  
with Three Radio Channels

LA-NORTH BUREAU

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVINGS	ESTIMATED 5-YEAR SAVING
KEYBOARD	33	7	157	92	2.3	4.4
STYLUS MAP	30	7	163	81	2.3	4.3
2-ACCELEROMETERS	34	7	160	96	2.2	4.3
LASER VELOCINTP	13	8	157	54	2.4	4.4
ULTRASONIC VELD	40	7	161	106	2.2	4.3
COMPASS/ODOMETER	20	8	157	51	2.4	4.4
COMPASS/LASER VEL	15	8	156	54	2.4	4.4
CHPSS-U-SONIC VEL	17	8	156	54	2.4	4.4
OMEGA	1600	0	4937	3856	0.0	0.0
LORAN	160	4	404	336	0.9	0.0
DECCA	200	3	487	465	0.6	0.0
AM-STATIONS	200	3	485	463	0.6	0.0
DIFF. OMEGA	160	4	404	396	0.9	0.0
DIFF. LORAN	400	1	1113	1063	0.0	0.0
DIFF. AM-STA.	250	2	596	560	0.1	0.0
RELAY OMEGA	500	0	13565	4437	0.0	0.0
RELAY LORAN	800	0	2294	2175	0.0	0.0

Table 2-44. Los Angeles, Valley Bureau  
AVM Physical Parameters

AREA IS 217.3 SQUARE MILES.  
 EAST WEST DISTANCE IS 23 MILES.  
 NORTH SOUTH DISTANCE IS 13.5 MILES.  
 TOTAL ROAD MILEAGE IS 2661 MILES.  
 THE NUMBER OF INTERSECTIONS IS 15000.  
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 30000.  
 THERE ARE 189 CARS IN THE FLEET.  
 AND THERE ARE 0 MOTORCYCLES.  
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:  
 FIRST SHIFT MAX. 72  
 FIRST SHIFT MIN. 61  
 SECOND SHIFT MAX. 108  
 SECOND SHIFT MIN. 96  
 THIRD SHIFT MAX. 121  
 THIRD SHIFT MIN. 96  
 THE NUMBER OF DISPATCHERS IS 2  
 THE CITY WOULD REQUIRE 10 WIDE-BAND OR  
 NARROW BAND ANTENNA SITES AND 45 NARROW BAND  
 OR ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-46. Los Angeles, Valley Bureau  
AVM Polling Cycle Times

CYCLE TIME IN SECONDS TO POLL INR AND MIN UNITS DEPLOYED.

CLASS I TECHNIQUE	TOTAL FLEET	INR	MIN	REDUANT	FRID
KEYBOARD	33	459	157	0.0	0.0
STYLUS MAP	30	475	163	1.9	0.0
2-ACCELEROMETERS	34	467	160	1.9	0.0
LASER VELOCINTP	13	459	157	2.0	0.0
ULTRASONIC VELD	40	469	161	1.9	0.0
COMPASS/ODOMETER	20	460	157	2.0	0.0
COMPASS/LASER VEL	15	456	156	2.0	0.0
CHPSS-U-SONIC VEL	17	458	156	2.0	0.0
OMEGA	1600	4227	4037	0.0	0.0
LORAN	160	434	404	0.2	0.0
DECCA	200	510	487	0.5	0.0
AM-STATIONS	200	509	487	0.5	0.0
DIFF. OMEGA	160	421	404	0.2	0.0
DIFF. LORAN	400	1177	1113	0.0	0.0
DIFF. AM-STA.	200	623	539	0.0	0.0
RELAY OMEGA	500	40137	13525	0.0	0.0
RELAY LORAN	800	2164	2294	0.0	0.0

Table 2-45. Los Angeles, Valley Bureau  
AVM Systems Cost Analyses

LA-NORTH BUREAU

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVINGS	ESTIMATED 5-YEAR SAVING
KEYBOARD	33	7	236	94	2.2	2.5
STYLUS MAP	30	7	244	80	2.3	2.3
2-ACCELEROMETERS	34	7	240	98	2.2	2.4
LASER VELOCINTP	13	8	236	77	2.3	2.5
ULTRASONIC VELD	40	7	241	108	2.2	2.4
COMPASS/ODOMETER	20	8	236	77	2.3	2.5
COMPASS/LASER VEL	15	8	234	77	2.3	2.5
CHPSS-U-SONIC VEL	17	8	235	77	2.3	2.5
OMEGA	1600	0	4106	3922	0.0	0.0
LORAN	160	4	411	393	0.9	0.0
DECCA	200	3	495	473	0.5	0.0
AM-STATIONS	200	3	493	471	0.5	0.0
DIFF. OMEGA	160	4	411	392	0.9	0.0
DIFF. LORAN	400	1	1140	1094	0.0	0.0
DIFF. AM-STA.	250	2	596	569	0.1	0.0
RELAY OMEGA	500	0	20440	6450	0.0	0.0
RELAY LORAN	800	0	2340	2218	0.0	0.0

Table 2-47. Los Angeles, Valley Bureau  
AVM Accuracies and Cost Benefits  
with One Radio Channel

LA-NORTH BUREAU

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED	ESTIMATED \$1000 SAVINGS	ESTIMATED 5-YEAR SAVING
KEYBOARD	33	7	459	157	2.0	0.0
STYLUS MAP	30	7	475	163	1.9	0.0
2-ACCELEROMETERS	34	7	467	160	1.9	0.0
LASER VELOCINTP	13	8	459	157	2.0	0.0
ULTRASONIC VELD	40	7	469	161	1.9	0.0
COMPASS/ODOMETER	20	8	460	157	2.0	0.0
COMPASS/LASER VEL	15	8	456	156	2.0	0.0
CHPSS-U-SONIC VEL	17	8	458	156	2.0	0.0
OMEGA	1600	0	4227	4037	0.0	0.0
LORAN	160	4	534	404	0.2	0.0
DECCA	200	3	510	487	0.5	0.0
AM-STATIONS	200	3	509	487	0.5	0.0
DIFF. OMEGA	160	4	521	404	0.2	0.0
DIFF. LORAN	400	1	1177	1113	0.0	0.0
DIFF. AM-STA.	200	0	623	539	0.0	0.0
RELAY OMEGA	500	0	40137	13525	0.0	0.0
RELAY LORAN	800	0	2164	2294	0.0	0.0

Table 2-48. Los Angeles, Valley Bureau  
AVM Accuracies and Cost Benefits  
with Two Radio Channels

CLASS 1 TECHNIQUE	SYSTEM ACCURACIES IN VEHICLES		SYSTEM ACCURACIES IN VEHICLES		ESTIMATED \$1000 SAVINGS		ESTIMATED 5-YEAR SAVINGS
	ULTIMATE ACCURACY	VEHICLES SAVED	MIN	MAX	MIN	MAX	
TECHNIQUE	33	0	344	122	3.4	3.6	3125
RE-SONAR	34	0	353	126	3.3	3.4	3025
STYLUS MAP	34	0	348	124	3.3	3.5	3050
2-A ACCELEROMETERS	13	0	344	122	3.4	3.6	3050
LASER VELOCITY	40	0	349	125	3.3	3.5	1300
ULTRASONIC WELD	20	0	344	122	3.4	3.6	1160
COMPASS-ODOMETER	15	0	342	121	3.4	3.6	3110
COMPASS LASEP WEL	17	0	343	121	3.4	3.6	3110
COMPS U-SONIC WEL	1600	0	412	3936	0.0	0.0	0
OMEGA	100	0	412	400	1.4	0.0	470
LOFAR	200	0	496	482	0.0	0.0	25
DECCA	200	0	494	480	0.0	0.0	20
AN-STATION	100	0	411	400	1.4	0.0	470
DIFF. OMEGA	400	1	1142	1126	0.0	0.0	0
DIFF. LOFAR	250	1	547	530	0.1	0.0	745
DIFF. AN-STA.	500	1	1141	10516	0.0	0.0	0
RELAY OMEGA	500	0	1244	1227	0.0	0.0	0
RELAY LOFAR	10	0	241	120	3.4	3.7	1040
CLASS II	10	0	241	120	3.4	3.7	1040
SURFED RES. LOOPS	10	0	241	120	3.4	3.7	1040
REFLECTING SIGN	10	0	241	120	3.4	3.7	1040
REFLECTING ROAD	10	0	241	120	3.4	3.7	1040
RF-ROAD POST	10	0	241	120	3.4	3.7	1040
RF-TRIP POST	10	0	241	120	3.4	3.7	1040
LF POST	10	0	241	120	3.4	3.7	1040
LIGHT I-R POST	10	0	241	120	3.4	3.7	1040
SURFED MAGNET	4	0	241	120	3.4	3.7	1040
ULTRASONIC POST	10	0	241	120	3.4	3.7	1040
TRAFFIC SENSOR	10	0	241	120	3.4	3.7	1040
CLASS III	1000	0	2501	2545	0.0	0.0	0
IMP-SOUND FI PHASE	1000	0	2107	2020	0.0	0.0	0
IMP-SOUND FI PHASE	100	0	144	137	2.3	2.5	1040
PULSE T-U-APPRIAL	100	0	217	209	2.7	2.1	2165
NOISE CORRELATION	700	0	1372	1372	0.0	0.0	0
DICTION FINDER	10	0	42	23	4.1	4.0	3090
CLASS IV	100	0	200	207	2.8	2.5	1025
TRAFFIC LOOPS	100	0	200	207	2.8	2.5	1025
IRVISE RADIO	20	0	42	43	3.4	3.6	3010
PHOTO I-R DETECT	20	0	42	43	3.4	3.6	3010
ULTRASONIC DETECT	20	0	42	43	3.4	3.6	3010

Table 2-49. Los Angeles, Valley Bureau  
AVM Accuracies and Cost Benefits  
with Three Radio Channels

CLASS 1 TECHNIQUE	SYSTEM ACCURACIES IN VEHICLES		SYSTEM ACCURACIES IN VEHICLES		ESTIMATED \$1000 SAVINGS		ESTIMATED 5-YEAR SAVINGS
	ULTIMATE ACCURACY	VEHICLES SAVED	MIN	MAX	MIN	MAX	
TECHNIQUE	33	0	162	35	3.6	3.6	3025
RE-SONAR	34	0	168	35	3.6	3.4	3000
STYLUS MAP	34	0	165	34	3.5	3.4	3000
2-A ACCELEROMETERS	13	0	162	30	3.7	3.4	3000
LASER VELOCITY	40	0	166	108	3.5	3.4	1400
ULTRASONIC WELD	20	0	165	30	3.7	3.4	1300
COMPASS-ODOMETER	15	0	161	30	3.7	3.4	1310
COMPASS LASEP WEL	17	0	162	30	3.7	3.4	1310
COMPS U-SONIC WEL	1600	0	4042	3923	0.0	0.0	0
OMEGA	100	0	405	392	1.4	0.0	470
LOFAR	200	0	488	474	0.0	0.0	25
DECCA	200	0	486	472	0.0	0.0	20
AN-STATIONS	100	0	404	390	1.4	0.0	470
DIFF. OMEGA	400	1	1121	1080	0.0	0.0	0
DIFF. LOFAR	250	1	557	570	0.2	0.0	745
DIFF. AN-STA.	500	1	14046	13822	0.0	0.0	0
RELAY OMEGA	500	0	2242	2222	0.0	0.0	0
RELAY LOFAR	10	0	160	74	3.7	3.4	1040
CLASS II	10	0	160	74	3.7	3.4	1040
SURFED RES. LOOPS	10	0	160	74	3.7	3.4	1040
REFLECTING SIGN	10	0	160	74	3.7	3.4	1040
REFLECTING ROAD	10	0	160	74	3.7	3.4	1040
RF-ROAD POST	10	0	160	74	3.7	3.4	1040
RF-TRIP POST	10	0	160	74	3.7	3.4	1040
LF POST	10	0	160	74	3.7	3.4	1040
LIGHT I-R POST	10	0	160	74	3.7	3.4	1040
SURFED MAGNET	4	0	160	74	3.7	3.4	1040
ULTRASONIC POST	10	0	160	74	3.7	3.4	1040
TRAFFIC SENSOR	10	0	160	74	3.7	3.4	1040
CLASS III	1000	0	2530	2486	0.0	0.0	0
IMP-SOUND FI PHASE	1000	0	2025	2064	0.0	0.0	0
IMP-SOUND FI PHASE	100	0	174	167	2.3	2.5	1040
PULSE T-U-APPRIAL	100	0	217	209	2.7	2.1	2165
NOISE CORRELATION	700	0	1322	1322	0.0	0.0	0
DICTION FINDER	10	0	42	23	4.1	4.0	3090
CLASS IV	100	0	200	207	2.8	2.5	1025
TRAFFIC LOOPS	100	0	200	207	2.8	2.5	1025
IRVISE RADIO	20	0	42	43	3.4	3.6	3010
PHOTO I-R DETECT	20	0	42	43	3.4	3.6	3010
ULTRASONIC DETECT	20	0	42	43	3.4	3.6	3010

**PART THREE:**  
**ANALYTICAL TECHNIQUES**  
**FOR ESTIMATING AVM**  
**SYSTEM ACCURACY**

J.E. Fielding  
M. Perlman

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I. VEHICLE LOCATION ACCURACY FOR CLASS I AND III SYSTEMS

In this Section, an algorithm is described which can be used to determine the system accuracy of Class I and III automatic vehicle monitoring (AVM) systems as a function of the appropriate system parameters. Some of the resultant cumulative probability density functions (cdf) are also presented, which can be interpreted as the fraction of the fleet for which the error is less than or equal to y. The flow chart shown in Fig. 3-1 is a brief outline of the vehicle location accuracy program, while Fig. 3-2 expands on the methodology of the computation of the cumulative density function.

A. Parameters for AVM System Accuracy Analysis

The inherent error,  $\epsilon_0$ , is defined to be the distance between the vehicle's actual location and the location determined by the AVM system at the

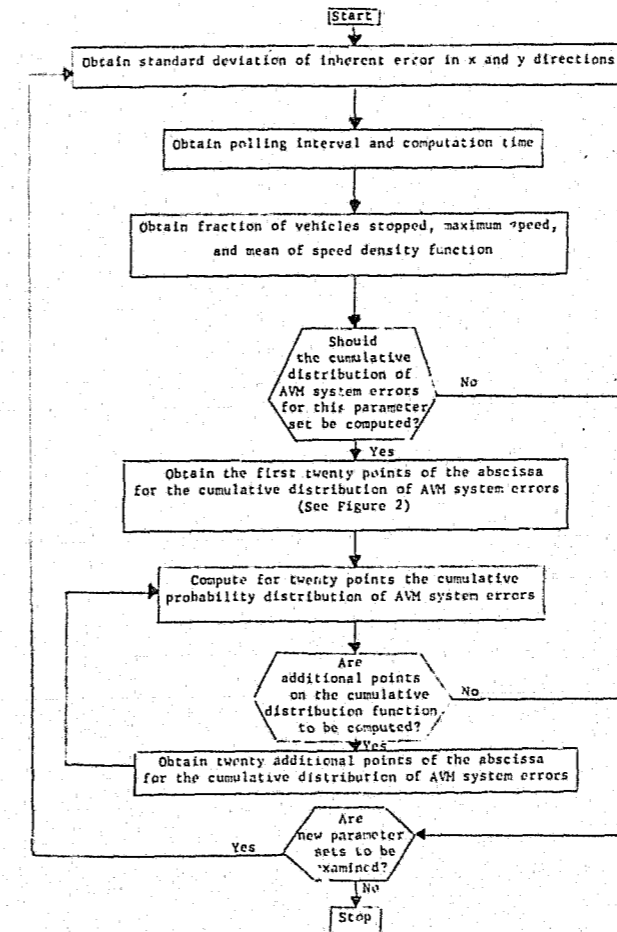


Fig. 3-1. Main AVM Accuracy Analysis Program

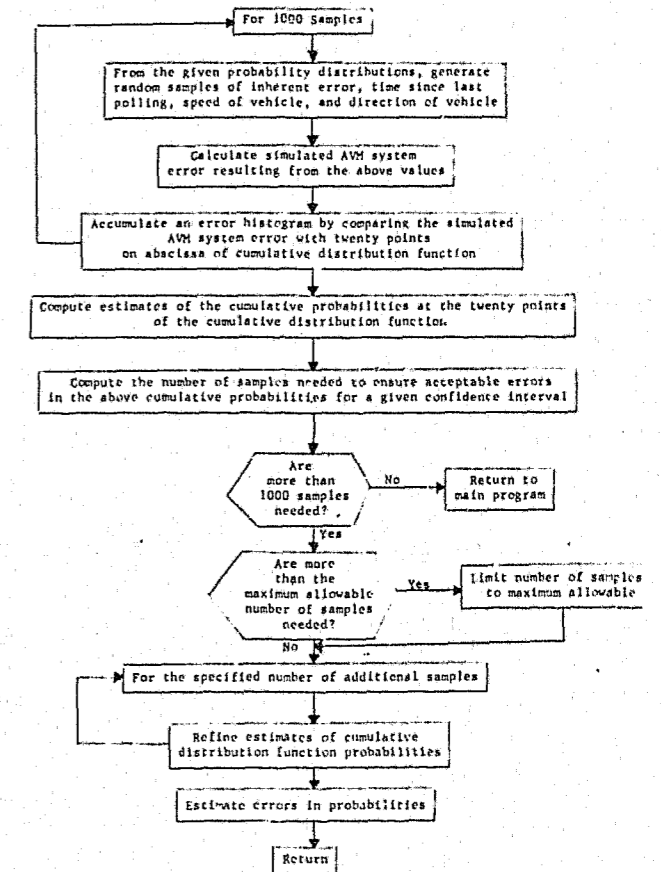


Fig. 3-2. Computation of Cumulative Distribution Function

instant of polling. Inherent error is assumed to be consistent with a Rayleigh distribution, i. e.,

$$\Phi(\epsilon_0) = \frac{\epsilon_0}{\sigma^2} e^{-1/2(\frac{\epsilon_0}{\sigma})^2}$$

As time passes, the vehicle's location changes by a distance of (s · t) and a direction  $\theta$ . (See Fig. 3-3.) The random variable  $\theta$  is assumed to be uniformly distributed. Its probability density function is denoted by  $p(\theta)$ , and is equal to  $1/(2\pi)$  between  $-\pi$  and  $\pi$ .

The speed of the vehicle is represented by the symbol s and is assumed to be described by the following distribution:

$$f(s) = \begin{cases} FO \cdot \delta & s=0 \\ \lambda e^{-\lambda s} & 0 < s < M \\ 0 & \text{otherwise} \end{cases}$$

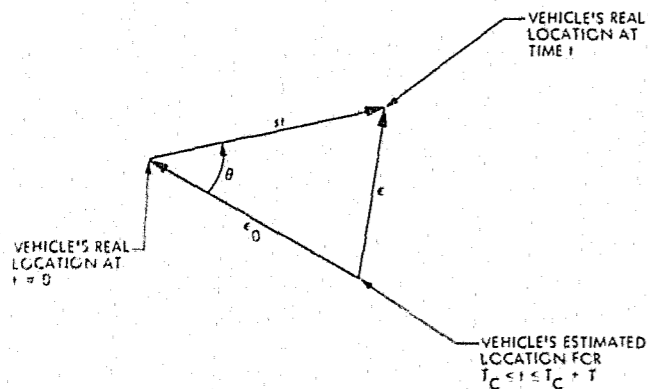


Fig. 3-3. Error in Knowledge of Vehicle's Location

There is a discrete probability FO, associated with zero speed. Between speeds zero and maximum M, the speed is distributed exponentially. The parameter lambda is set such that the fraction of vehicles stopped, FO, plus the fraction whose speed falls between 0 and maximum speed M sums to 0.99.

The last of the AVM system parameters is time. After the location of the vehicle is determined, there is a delay before the information becomes available. This delay is referred to as computation time, TC. Thus, if the symbol T denotes the polling interval, the probability density function g(t) is a uniform distribution over the time interval TC through TC + T.

#### B. Derivation of Accuracy Analysis Algorithm

Probability distribution functions have been defined for epsilon\_0, theta, s, and t, and from Fig 3-3 the actual error in the knowledge of the vehicle's location, epsilon, is:

$$\epsilon = \sqrt{\epsilon_0^2 + s^2 t^2 - 2\epsilon_0 s t \cos \theta}$$

The distribution of errors is given by:

$$cdfy = \text{Prob}(\epsilon \leq y) = \iiint\int_R \phi(\epsilon_0) g(t) \cdot$$

$$f(s) p(\theta) d\theta ds dt d\epsilon_0,$$

where R is the region such that epsilon <= y. Due to the complexity of R, it is not practical to evaluate this integral analytically or by numerical quadrature. Therefore a Monte Carlo integration of cdfy is used.

The Monte Carlo integration generates values for the four random variables, epsilon\_0, s, t, theta and uses these variables to calculate epsilon by the above formula. By checking whether epsilon <= yi for i=1, ..., 20, when the yi's are a pre-specified array of points on the abscissa, it is possible, if enough trials are run, to determine an accurate estimate of the cumulative distribution function.

The methodology used to generate the random variables epsilon\_0, s, t and theta involves generating four uniform variates on [0, 1]: r1, r2, r3, r4. Inverting the cumulative density functions leads to the expressions needed to calculate the desired variables:

$$\epsilon_0 = \sigma \sqrt{-2 \ln r_1}$$

$$t = T_C + r_2 T$$

$$s = \begin{cases} 0 & 0 \leq r_3 \leq FO \\ \frac{\ln(1-r_3)}{-\lambda} & FO < r_3 \leq 1 \end{cases}$$

$$\theta = \pi(2r_4 - 1)$$

Of prime concern in the Monte Carlo integration is the number of trials needed to ensure an acceptable estimate of the probabilities that epsilon <= yi. If pi denotes the real value of cdfy for a particular yi, then the process becomes a long sequence of Bernoulli trials with pi equal to the probability of success (i.e., that epsilon <= yi). Since the number of trials will be "large", the Bernoulli distribution can be well approximated by the Gaussian distribution with mean, mu = p Standard deviation,

$$\sigma = \sqrt{np(1-p)/n}$$

where n = number of trials, and pi has been replaced by p for simplicity.

Since the distribution of the number of trials for which epsilon exceeds any particular value of y is approximately gaussian, we can require the probability (of the event that the absolute error in the distribution function, cdfy, is less than some specified maximum value, E) to be at least C, the so-called "confidence level". That is, a fraction C of the distribution must be contained within the interval p - k\*sigma thru p + k\*sigma (Fig. 3-4). Thus, a value of C determines a value for k. In addition,

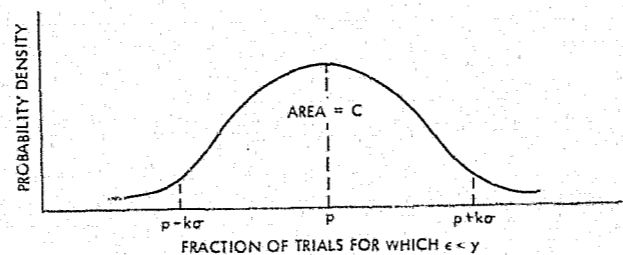


Fig. 3-4. Probability Density vs Fraction of Trials

to ensure an acceptable absolute error, E, it is required that the interval k\*sigma be less than or equal to E:

$$k\sigma \leq E.$$

Substituting the expression for the standard deviation sigma into this last equation gives

$$k \sqrt{np(1-p)/n} \leq E$$

which may be rewritten

$$n \geq k^2 p(1-p)/E^2$$

This value for n represents the minimum number of trials needed to ensure an absolute error of less than E with confidence C. A larger value of k implies that a larger fraction of the gaussian distribution will be contained within the interval p +/- k\*sigma, thus leading to a higher confidence C. However, a larger k requires an increased number of trials in order to satisfy the error criteria.

The accuracy algorithm specifies the maximum allowable error E, and the required confidence interval C. The program proceeds to run 1000 trials, and pi is then estimated as

$$(\text{number of times } \epsilon \leq y_i) / 1000 \text{ for } i=1, \dots, 20.$$

These approximate values of pi are used to calculate the required number of trials, n, needed to ensure (with confidence C) that none of the error terms will be greater than the maximum allowable error E. If n is found to be less than 1000, no more runs are required and the calculation of (yi, cdfy) is complete. However, if n is greater than 1000, additional trials are needed.

In order to prevent an excessive number of runs, in terms of computer time, a constant NMAX is introduced which serves as the maximum allowable number of trials. Thus, if it is determined that more than 1000 runs are needed, the algorithm will process additional trials until the error terms are sufficiently small or until the maximum allowable number of trials is reached, whichever comes first. In the case where the number of trials reaches NMAX, the resulting errors using the improved estimates of the pi's are calculated. In the actual execution of the program, the number of trials is almost always extended to NMAX with resulting errors on the order of 0.005.

The accuracy program is interactive, the user being free to set the system parameters of variance in inherent error, polling interval, computation time, fraction of vehicles stopped, and the "maximum" vehicle speed. The program then computes the mean of the exponential speed distribution such that 99% of the probability is included between speeds 0 and maximum speed M. The program specifies the 20 values to be used along the abscissa of the cumulative distribution function of AVM system errors. These values are determined as a

function of the variance of the inherent error as one can assume that the variance of system errors is somewhat correlated with this parameter. The intent is to cover the full range from 0.0 to 1.0 of the cumulative distribution function. As a safeguard against failure of full coverages, the program allows the user to calculate the cumulative distribution function for 20 additional values of y where the user specifies the initial point and the interval between points. This option for additional points can be repeated as many times as the user desires. After the cumulative distribution function is computed, the user may reset the system parameters, and the process of determining a new cumulative distribution function is repeated.

#### C. Results of AVM System Accuracy Analysis

The algorithm described in the previous section was exercised by running 42 cases, each one with a unique set of the input parameters, where

- SIGMA = Standard deviation of inherent error in x and y directions
- T = Polling interval
- TC = Computation time
- M = Maximum speed
- FO = Fraction stopped

Originally, all combinations of the following parameter values were to be run,

SIGMA (meters)	T (seconds)	TC (seconds)	M (meters/sec)	FO
0	2	0.01	40	0
100	10	0.1	60	
1000	60			
	120			
	300			

which would have required 60 cases. However, after the first 14 runs, it became evident that the AVM system error was stable for computation times in the range 0.01 to 0.1 second.

A value for the standard deviation of the inherent error of zero serves as a boundary condition for inherent accuracy of AVM hardware systems. Estimates of system error using SIGMA equal to zero represents the accuracy to be expected if one invests in extremely accurate hardware systems in terms of pinpointing location, assuming there is no motion. At first glance, a maximum speed of 60 meters/second (134 miles/hr) might seem a little high; however, the speed of the vehicles of the fleet is assumed to be distributed exponentially. Thus, a very small fraction of the fleet is traveling near maximum speeds; one-half of the fleet is traveling at a speed of less than (maximum speed/6) or 22.3 miles/hr. The fraction of cars stopped is set at 0 because the algorithm is designed to specifically test system accuracy assuming moving vehicles. Later, if individual users need results that reflect their mode of operation, they can supply a non-zero value for this parameter. The effects



of changes in the above variables on AVM system accuracy follows.

No modeling effort is necessary to determine whether system accuracy will improve or deteriorate given the direction of change of any input variable. As the variance in the inherent error, the polling interval, the computation time, and the maximum speed increase, system accuracy deteriorates. However, the designer requires a more detailed knowledge of the interaction between these system parameters and AVM system accuracy. He is faced with an accuracy constraint such as 80% of the vehicles must be located to within 150 meters. In order to satisfy this constraint, he must be aware of the combinations of system parameters that can meet his requirements. The above analysis provides this information. What it does not provide is information for the designers' next step, which is to determine the proper balance with respect to inherent accuracy, polling interval, and computation time so as to minimize cost as well as satisfy accuracy constraints.

The best accuracy results are obtained when SIGMA is set equal to zero. With SIGMA zero and polling interval equal to 2 seconds, 80% of the fleet is located to within 20 meters and this is not strongly dependent on maximum speed or computation time. As the polling interval is increased to 10 seconds, 80% of the fleet is located to within 65 meters at maximum speed of 40 meters/second and to within 105 meters at 60 meters/second. Thus, as polling interval increases, accuracy becomes more dependent on maximum speed. Again, the accuracy is not dependent on computation time. Table 3-1 presents similar results for the remainder of the cases with SIGMA equal to zero. The above trends continue, that is, as the polling interval increases, the 80% distance grows,

Table 3-1. Vehicle Location Accuracy at 80% Level for SIGMA = 0 Meters

T (sec)	TC (sec)	M (meters/sec)	Accuracy (meters)
2	.01	40	15
2	.01	60	20
2	.1	40	15
2	.1	60	22
10	.01	40	65
10	.01	60	105
10	.1	40	70
10	.1	60	105
60	.01	40	420
60	.01	60	620
60	.1	40	420
60	.1	60	620
120	.01	40	820
120	.01	60	1350
300	.01	40	2100
300	.01	60	3080

the dependence on maximum speed increases, and accuracy is not dependent on computation time.

Table 3-2 presents similar data for the case SIGMA equals 100 meters. With a polling interval of 2 seconds, 80% of the vehicles in the fleet are located to within 180 meters. The trends evident in the SIGMA equal zero cases can also be seen in Table 3-2. One major difference is that, in this case, the change in accuracy as polling interval increases from 2 to 10 seconds is rather insignificant. Thus, if the system hardware has a standard deviation for inherent accuracy in the x and y direction of 100 meters, then little would be gained by specifying a polling interval shorter than 10 seconds. In comparing the results of Table 3-1 and Table 3-2, it is apparent that the accuracy of a SIGMA = zero system is not significantly better than a SIGMA = 100 meters system when the polling interval is greater than 60 seconds. Thus, if a sophisticated hardware system in terms of inherent error is installed, it requires a short polling interval to realize significant benefits.

The most striking difference between the cases with inherent error equal to 0 and 100 meters and the case with inherent error equal to 1000 meters (Table 3-3) is that the interval between the minimum and maximum accuracies is much more compact in the 100 meter case. In general, one can conclude that as the resolution in inherent error deteriorates, the system is less dependent on the remaining parameters. The accuracy figure in Table 3-3 for polling intervals of 2, 10, 60 and 120 seconds are significantly higher than the corresponding values in Tables 3-1 and 3-2, while the accuracy at a polling interval of 300 seconds is of the same order over all three Tables.

These results presenting accuracy estimates for AVM system errors can serve as a tool to be used in AVM system design.

Table 3-3. Vehicle Location Accuracy at 80% Level for SIGMA = 1000 Meters

T (sec)	TC (sec)	M (meters/sec)	Accuracy (meters)
2	.01	40	1790
2	.01	60	1790
2	.1	40	1790
2	.1	60	1790
10	.01	40	1795
10	.01	60	1810
60	.01	40	1880
60	.01	60	1950
120	.01	40	2210
120	.01	60	2500
300	.01	40	2985
300	.01	60	3500
300	.1	40	2780
300	.1	60	3650

II. MARKOV CHAIN MODEL OF VEHICLE LOCATION BY MEANS OF PROXIMITY SENSORS FOR CLASS II AND IV SYSTEMS

Marvin Perlman

One approach to automatically locating specified vehicles in an urban area involves the employment of proximity sensors. The proximity sensors (which may be active or passive) are distributed throughout a given area. Once installed, the position of a sensor is fixed. A vehicle, properly equipped, will interact with a sensor when the distance between the vehicle and the sensor is within prescribed limits. Interaction results in communicating the identity of the vehicle and the location of the sensor to a central system. Not considered in this analysis are the proximity sensor's characteristics, the required equipment for the vehicle, or the means of communicating to the central system. This analysis presents a Markov chain model of the interaction of fixed proximity sensors with moving vehicles whose locations are to be monitored.

A. Classifications of Finite Markov Chains

1. Concepts and definitions. A stochastic process is any sequence of experiments amenable to probabilistic analysis. A stochastic process is said to be finite if the set of possible outcomes is finite. An independent process is a finite stochastic process where knowledge of the outcome of any preceding experiment in no way affects the prediction of the outcome of the present experiment.

A finite Markov chain process is a finite stochastic process where knowledge of the outcome of the immediate past experiment does affect the prediction of the outcome of the present experiment. Furthermore, the dependence of the outcome of each experiment on the outcome of the immediately preceding experiment only is the same at each stage of successive experiments. A finite Markov chain is characterized by a finite set of states  $\{s_1, s_2, \dots, s_n\}$ . The state of a Markov chain is the outcome of the last experiment. Thus a Markov chain is in one and only one state at a given time and advances from one state to another (or remains in the same state) in accordance with a priori transition probabilities. The transition probability  $p_{ij}$  is the probability that the (Markov chain) process will move from state  $s_i$  to  $s_j$ , and  $p_{ij}$  depends only on  $s_i$ . Associated with every ordered pair of states is a known transition probability. An  $n \times n$  transition probability matrix  $P$  contains as entries the transition probabilities corresponding to each of the respective  $n^2$  ordered pairs of states as follows:

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & \dots & s_n \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ \cdot \\ \cdot \\ \cdot \\ s_n \end{matrix} & \begin{bmatrix} p_{11} & p_{12} & \dots & p_{1n} \\ p_{21} & p_{22} & \dots & p_{2n} \\ \cdot & \cdot & \dots & \cdot \\ \cdot & \cdot & \dots & \cdot \\ \cdot & \cdot & \dots & \cdot \\ p_{n1} & p_{n2} & \dots & p_{nn} \end{bmatrix} \end{matrix}$$

Each row in  $P$  comprises a probability event space such that

$$P_{ij} \geq 0 \quad \text{for all } i, j$$

and

$$\sum_{j=1}^n P_{ij} = 1 \quad \text{for every } i$$

The transition probability matrix  $P$  and an initial (starting state completely describe a finite Markov chain process.

2. Regular Markov chains. A Markov chain is defined to be regular if and only if after  $n$  steps (i. e., experiments) for some  $n$ , it is possible for the process to be in any state regardless of the starting state. The entry  $p_{ij}^{(n)}$  in  $P^n$  (the  $n$ th power of the transition matrix) is the probability that the process is in state  $s_j$  after  $n$  steps given that it started in state  $s_i$ . A regular Markov chain has a regular transition matrix  $P$  such that  $P^n$  contains only positive entries (i. e.,  $p_{ij}^{(n)} > 0$  for all  $i, j$ ).  $P$  may be tested for regularity by noting whether or not the entries in  $P^2, (P^2)^2, (P^4)^2, \dots$  are positive assuming  $P$  has one or more 0 entry.

Example 1. Given the following (probability) matrix

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & s_3 & s_4 \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0.5 & 0.25 & 0 & 0.25 \\ 0 & 0 & 0.5 & 0.5 \end{bmatrix} \end{matrix}$$

Successive squaring of  $P, P^2, P^4, \dots$  quickly results in large powers of  $P$ . When testing for regularity, the actual values of the entries need not be determined. Denoting each positive entry by  $x$  and each zero entry 0 gives

$$P = \begin{bmatrix} 0 & x & 0 & 0 \\ 0 & 0 & x & 0 \\ x & x & 0 & x \\ 0 & 0 & x & x \end{bmatrix}$$

$P^2, P^4$  and  $P^8$  are, respectively

$$\begin{bmatrix} 0 & 0 & x & 0 \\ x & x & 0 & x \\ 0 & x & x & x \\ x & x & x & x \end{bmatrix}, \begin{bmatrix} 0 & x & x & x \\ x & x & x & x \\ x & x & x & x \\ x & x & x & x \end{bmatrix} \text{ and } \begin{bmatrix} x & x & x & x \\ x & x & x & x \\ x & x & x & x \\ x & x & x & x \end{bmatrix}$$

Thus  $P$  is a regular transition matrix.

3. Ergodic Markov chains. A Markov chain is defined to be ergodic if and only if it is possible for the process to go from every state to every other state. Clearly a regular Markov chain is always ergodic. However, an ergodic Markov chain is not necessarily regular. That is, for every  $n, P^n$  contains some 0 entries. However,  $P^n$  for different values of  $n$ , will contain zeros in different locations. As  $n$  increases, the positions of the zeros change cyclically. In this case, the chain is termed a cyclic Markov chain. Thus an ergodic Markov chain is either cyclic or regular but not both.

Example 2. Given the following transition matrix

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & s_3 & s_4 \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0.25 & 0 & 0.75 & 0 \\ 0 & 0.25 & 0 & 0.75 \\ 0 & 0 & 1 & 0 \end{bmatrix} \end{matrix}$$

or

$$P = \begin{bmatrix} 0 & x & 0 & 0 \\ x & 0 & x & 0 \\ 0 & x & 0 & x \\ 0 & 0 & x & 0 \end{bmatrix}$$

where  $x$  denotes a positive entry. For even  $n > 0,$

$$P^n = \begin{bmatrix} x & 0 & x & 0 \\ 0 & x & 0 & x \\ x & 0 & x & 0 \\ 0 & x & 0 & x \end{bmatrix}$$

For odd  $n > 1,$

$$P^n = \begin{bmatrix} 0 & x & 0 & x \\ x & 0 & x & 0 \\ 0 & x & 0 & x \\ x & 0 & x & 0 \end{bmatrix}$$

Starting in an odd-numbered state ( $s_1$  or  $s_3$ ), the process is in an even-numbered state ( $s_2$  or  $s_4$ ) after an odd number of steps, and in an odd-numbered state after an even number of steps.

$P$  in Example 2 is an ergodic transition matrix which is nonregular. The process characterized by  $P$  is a cyclic (ergodic) chain.

4. Absorbing Markov chains. An absorbing state in a Markov chain is one which cannot be left once entered. An absorbing Markov chain is a Markov chain that has at least one absorbing state, and from every nonabsorbing state it is possible to move to an absorbing state (in one or more steps). The nonabsorbing states (of an absorbing chain) are known as transient states. The transition matrix  $P$  of an absorbing chain has entries  $P_{ij} = 1$  for each  $s_j$  that is absorbing.

Example 3. The following transition matrix characterizes an absorbing chain

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & s_3 & s_4 & s_5 \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \\ s_5 \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0.5 & 0 & 0.5 & 0 & 0 \\ 0 & 0.5 & 0 & 0.5 & 0 \\ 0 & 0 & 0.5 & 0 & 0.5 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \end{matrix}$$

States  $s_1$  and  $s_5$  are absorbing; whereas, states  $s_2, s_3$  and  $s_4$  are transient states.

5. Classification of states. The states of any given Markov chain can be partitioned into equivalence classes. An equivalence class comprises either an ergodic set of states or a transient set of states. Once the process enters an ergodic set, it remains in the set. Once the process leaves a transient set, it never reenters the set.

If a chain has two or more ergodic sets of states but no transient sets, the chain in effect is a composite of two or more unrelated chains. Each of the unrelated chains consists of a single ergodic set and may be treated separately. Without any

loss in generality, every ergodic chain (regular and cyclic) consists of a single ergodic set.

An absorbing state is an ergodic set consisting of one and only one state. Such an ergodic set is referred to as a unit set. Thus an absorbing chain has one or more unit sets and one or more transient sets.

Every state of a given set whether it is ergodic or transient can "communicate" with every other state in the set. The process, however, moves toward the ergodic sets when the chain contains transient as well as ergodic sets.

### B. Properties of Absorbing Markov Chains

1. Canonical Form of P and P<sup>n</sup>. The transition matrix P of an absorbing chain can always be arranged to have the following canonical form (by relabeling states)

$$P = \begin{bmatrix} I & O \\ R & Q \end{bmatrix}$$

The submatrix I is an  $l \times l$  identity matrix whose entries are the transition probabilities for every ordered pair of absorbing states ( $s_i, s_j$ ) where

$$p_{ij} = \begin{cases} 0 & \text{if } i \neq j \\ 1 & \text{if } i = j \end{cases}$$

The submatrix Q is an  $m \times m$  matrix whose entries are the transition probabilities for every ordered pair of transient states. The submatrix R is an  $m \times l$  matrix whose entries are the transition probabilities for every ordered pair of states ( $s_i, s_j$ ) where  $s_i$  is a transient state and  $s_j$  is an absorbing state. The submatrix O is an  $l \times m$  matrix whose entries are zeros corresponding to the zero transition probabilities of moving from any absorbing state to any transient state. Powers of P have the canonical form

$$P^n = \begin{bmatrix} I & O \\ M & Q^n \end{bmatrix}$$

where

$$M = [I + Q + Q^2 + \dots + Q^{n-1}]R$$

Note that the expression for M is a matrix equation.

Theorem 1. In any finite Markov chain, regardless of the initial (starting) state, the probability that the process is in ergodic state after n steps approaches 1 as n approaches infinity. (A proof of Theorem 1 appears in Ref. 1.)

A Corollary to Theorem 1 is that are real numbers b and c where  $b > 0$  and  $0 < c < 1$  such that

$$p_{ij}^{(n)} \leq bc^n$$

for any ordered pair of transient states ( $s_i, s_j$ ). This gives the rate at which  $p_{ij}^{(n)}$  approaches 0.

Every entry in  $Q^n$  in the canonical form of  $P^n$  of an absorbing chain approaches 0 as n increases without limit.

2. Fundamental matrix. The fundamental matrix of an absorbing chain is defined as

$$N = [I - Q]^{-1} \quad (1)$$

Note that

$$\frac{I}{I - Q} - \frac{Q^n}{I - Q} = I + Q + Q^2 + \dots + Q^{n-1}$$

and since  $Q \neq I$  and  $\lim_{n \rightarrow \infty} Q^n = 0$

$$[I - Q]^{-1} = \lim_{n \rightarrow \infty} [I + Q + Q^2 + \dots + Q^{n-1}]$$

the inverse of  $I - Q$  (i.e., N) always exists.

The submatrix M in  $P^n$  as n approaches infinity may be expressed as

$$M = [I - Q]^{-1} R = NR \quad (2)$$

The fundamental matrix N has the following probabilistic interpretation.

Let  $u_{ij}^{(k)} = 1$  if the process starts in transient state  $s_i$  and is in transient state  $s_j$  after k moves. Otherwise  $u_{ij}^{(k)} = 0$ . Let  $t_{ij}^{(n)}$  denote the number of times the process is in transient state  $s_j$  starting and during n moves given that it started in transient state  $s_i$ . Thus

$$t_{ij}^{(n)} = u_{ij}^{(0)} + u_{ij}^{(1)} + \dots + u_{ij}^{(n)}$$

The probability that the process is in transient state  $s_j$  after the k<sup>th</sup> move is

$$p(u_{ij}^{(k)} = 1) = q_{ij}^{(k)}$$

given that  $s_i$  is transient and the starting state. The mean of  $u_{ij}^{(k)}$  is

$$m(u_{ij}^{(k)}) = 1 \cdot q_{ij}^{(k)} + 0 \cdot (1 - q_{ij}^{(k)}) = q_{ij}^{(k)}$$

The mean of  $t_{ij}^{(n)}$  is

$$m(t_{ij}^{(n)}) = q_{ij}^{(0)} + q_{ij}^{(1)} + \dots + q_{ij}^{(n)}$$

the i, j<sup>th</sup> entry of

$$Q^{(0)} + Q^{(1)} + \dots + Q^{(n)}$$

where  $Q^{(0)} = I$ .

Then

$$n_{ij} = \lim_{n \rightarrow \infty} m(t_{ij}^{(n)})$$

is the i, j<sup>th</sup> entry of the fundamental matrix expressed in (1). The value of  $n_{ij}$  is the mean number of times the chain is in transient state  $s_j$  given that it started in transient state  $s_i$  and continues until the process is absorbed (i.e., reaches an absorbing state).

3. Statistics on the number of times the process is in a transient state. Let  $v_i$  denote the number of steps (including the original position) before absorption, given the starting state is  $s_i$ . If  $s_i$  is in an absorbing state, then  $v_i = 0$ . Given that the absorbing chain contains a transient set denoted by T, and  $s_i$  is a transient state if and only if  $s_i \in T$  (i.e.,  $s_i$  is a member of T). Then

$$m(v_i) = \sum_{s_j \in T} n_{ij} \quad (3)$$

which is the i<sup>th</sup> row sum of the fundamental matrix N. Each row sum of N appears in the  $m \times 1$  column vector

$$\alpha = NC \quad (4)$$

where C is a  $m \times 1$  column vector whose entries are all 1's.

The variance of the function  $v_i$  is

$$\text{var}(v_i) = m(v_i^2) - (m(v_i))^2$$

where

$$m(v_i^2) = \sum_{s_j \notin T} p_{ij} \cdot 1 + \sum_{s_j \in T} p_{ij} m[(v_i + 1)^2]$$

(Note that the original position is necessarily included in the expression for  $m(v_i^2)$ .)

Continuing,

$$m(v_i^2) = \sum_{s_j \notin T} p_{ij} + \sum_{s_j \in T} p_{ij} m(v_i^2 + 2v_i) + p_{ij}$$

$$= \sum_{s_j \in T} p_{ij} [m(v_i^2) + 2m(v_i)] + 1$$

$$\{m(v_i^2)\} = \left\{ \sum_{s_j \in T} p_{ij} [m(v_i^2) + 2m(v_i)] + 1 \right\}$$

The braces denote a column vector where each entry corresponds to a different value of i.

Therefore,

$$\{m(v_i^2)\} = Q \{m(v_i^2)\} + 2Q\alpha + C$$

$$[I - Q] \{m(v_i^2)\} = 2Q\alpha + C$$

$$\{m(v_i^2)\} = [I - Q]^{-1} [2Q\alpha + C]$$

$$= 2NQ\alpha + NC$$

$$= 2NQ\alpha + \alpha$$

Since

$$N = \frac{I}{I - Q}$$

$$N - NQ = I \quad \text{and} \quad NQ = N - I$$

and

$$\{m(v_i^2)\} = 2[N - I]\alpha + \alpha$$

$$= [2N - I]\alpha$$

Finally, the variance of  $v_i$  for each i expressed as entries in  $m \times 1$  column vector is

$$\{\text{var}(v_i)\} = \{m(v_i^2) - (m(v_i))^2\} = [2N - I]\alpha - \alpha_{sq}$$

where  $\alpha_{sq}$  results from squaring each entry  $m(v_i)$  in  $\alpha$  shown in (4).

Example 4. A particle moves a unit distance along a straight line. Given that it is in  $s_1$ , it moves to  $s_{i+1}$ , one unit to the right, with probability 0.5, or to state  $s_{i-1}$ , one unit to the left, with probability 0.5. Two states are introduced, one at each end of the line, to serve as barriers. These are absorbing states such that the process is absorbed if it reaches either absorbing state. Assume there are five states where  $s_1$  and  $s_5$  are absorbing, and  $s_2, s_3,$  and  $s_4$  are transient. The probability matrix appears in Example 3. Reordering the rows and columns gives the following canonical form:

$$P = \begin{matrix} & \begin{matrix} s_1 & s_5 & s_2 & s_3 & s_4 \end{matrix} \\ \begin{matrix} s_1 \\ s_5 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0.5 & 0 \\ 0 & 0 & 0.5 & 0 & 0.5 \\ 0 & 0.5 & 0 & 0.5 & 0 \end{bmatrix} \end{matrix}$$

The fundamental matrix is

$$N = [I - Q]^{-1} = \begin{matrix} & s_2 & s_3 & s_4 \\ \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 1.5 & 1 & 0.5 \\ 1 & 2 & 1 \\ 0.5 & 1 & 1.5 \end{bmatrix} \end{matrix}$$

Thus, for example, if the process starts in state  $s_2$ , the mean number of time it is in state  $s_2$ ,  $s_3$  and  $s_4$  is 1.5, 1 and 0.5, respectively.

Furthermore,

$$\lim_{n \rightarrow \infty} P^n = \begin{bmatrix} I & 0 \\ NR & 0 \end{bmatrix}$$

since

$$\lim_{n \rightarrow \infty} Q^n = 0$$

and

$$\lim_{n \rightarrow \infty} M = NR$$

as shown in (1) and (2).

In example 4

$$R = \begin{matrix} & s_1 & s_5 \\ \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0.5 & 0 \\ 0 & 0 \\ 0 & 0.5 \end{bmatrix} \end{matrix}$$

and

$$NR = \begin{matrix} & s_1 & s_5 \\ \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0.75 & 0.25 \\ 0.5 & 0.5 \\ 0.25 & 0.75 \end{bmatrix} \end{matrix}$$

Hence, for example, if the process starts in state  $s_2$ , it will be absorbed in state  $s_1$  with probability 0.75 or in state  $s_5$  with probability 0.25. The row sums of NR are necessarily 1 in accordance with Theorem 1. The mean number of steps before absorption including the original position for each transient starting state appears in  $\alpha$  as shown in (4).

$$\alpha = NC = \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} \begin{bmatrix} 3 \\ 4 \\ 3 \end{bmatrix}$$

The mean number of steps before absorption is 3 if the process starts in  $s_2$  or  $s_4$ ; whereas, it is 4 if the process starts in  $s_3$ .

The variance of the number of steps (including the original position) before absorption for each starting state appears in the column vector

$$[2N - I]\alpha - \alpha_{sq}$$

from expression (5). In example (4)

$$2N - I = \begin{bmatrix} 2 & 2 & 1 \\ 2 & 3 & 2 \\ 1 & 2 & 2 \end{bmatrix}, \alpha = \begin{bmatrix} 3 \\ 4 \\ 3 \end{bmatrix} \text{ and } \alpha_{sq} = \begin{bmatrix} 9 \\ 16 \\ 9 \end{bmatrix}$$

Thus

$$[2N - I]\alpha - \alpha_{sq} = \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} \begin{bmatrix} 8 \\ 8 \\ 8 \end{bmatrix}$$

The mean number of steps before absorption is greatest for starting at  $s_3$ . However, the variance is the same for each starting transient state. (Note that when the variances are quite large compared to the corresponding entries in  $\alpha_{sq}$ , it indicates that the means are unreliable estimates for that particular chain.)

### C. Model of Absorbing Markov Chain for Class II and IV Systems

Consider a portion of an area to be monitored as shown in Fig. 3-5. Subareas are 5 x 5 square blocks, and each subarea has an identical sensor layout. A (monitored) vehicle entering a sensed intersection corresponds to an absorbing state. This is to be interpreted as updated information as to the vehicle's location. When the process is in an absorbing state, the location of the monitored vehicle is known (to within the detection radius of the sensor). A vehicle entering an unsensed intersection corresponds to a transient state. The absorbing Markov chain models a sequence of experiments for locating a vehicle to within prescribed limits of accuracy.

Given that a vehicle starts at any given intersection (sensed or unsensed), what is the mean and variance of the number of blocks the vehicle moves until being sensed? Once the vehicle is sensed, a new experiment begins. Thus, between sensings, an uncertainty exists as to the vehicle's location. This is reflected in the magnitude of the mean and variance of the number of blocks the vehicle moves between sensings.

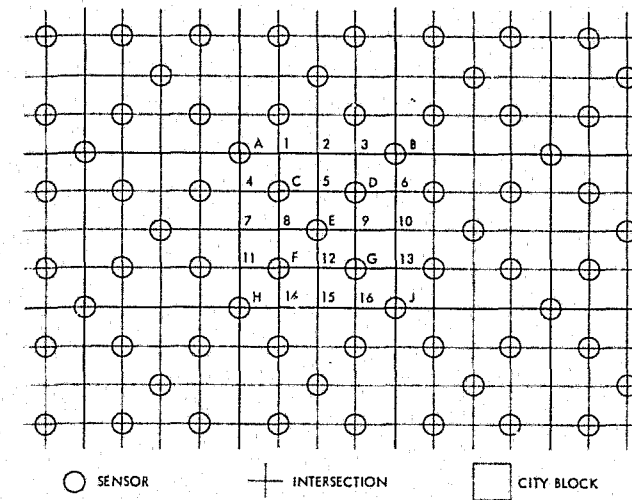


Fig. 3-5. Urban Distribution Pattern for Monitored Proximity Sensors

The number of sensors, their layout, and transition probabilities between orthogonally adjacent intersections is required a priori information. Uniformity of deployment of sensors assumes unbiased routes. Random movement of the vehicle corresponds to unbiased routing through the sensed area. Thus the direction of travel of a vehicle from an intersection will be in any one of four possible directions with equal probability.

If one were to incorporate a different transition probability for each of the four possible directions, the number of states in the Markov chain model would increase fourfold. Each state would be associated with a pair of labels. The intersection entered would be designated by one label and the direction from which it was entered by the other. Such a transition matrix would be meaningful if the transition probabilities were accurately known. That is, the probability that a vehicle upon leaving a particular intersection will go straight, make a left turn, a right turn or a U-turn is a priori information. Without this information, equiprobable direction of travel (to any of the four adjacent intersections) is assumed. The resulting statistical accuracy establishes achievable bounds on the system's accuracy.

Returning to Fig. 3-5, only the subarea with labeled intersections need be considered. Boundary intersections (of the subarea) act as reflecting boundaries in the Markov chain model. A vehicle in intersection 1 corresponds to the process being in transient state 1. The transition probability from state 1 to the intersection due North is 0.25. Since that intersection has the same relative location in its subarea as does intersection F in the subarea under discussion, an upward move (due North) is equivalent to a reflection to intersection F. Identical sensor layouts for all subareas is clearly required. This permits the use of a small transition matrix (25 x 25 in Fig. 3-5) for a Markov chain model of an entire area where fringe effects are neglected. Intersections labeled with characters are sensed and are associated with absorbing states. Unsensed intersections are labeled with numbers and are associated with transient states. The reflection properties of transient boundary intersections are apparent in the

submatrices Q and R in Figs. 3-6 and 3-7, respectively. (Note that states  $s_1$  and  $s_4$  are reflecting boundaries in Example 2.)

The matrix N and column vectors  $\alpha = NC$  and  $[2N - I]\alpha - \alpha_{sq}$  were computed on an IBM 360/65. The components of  $\alpha$  and  $\alpha_{sq}$  rounded to 3 decimal places are:

$$\alpha = NC = \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \\ 16 \end{matrix} \begin{bmatrix} 1.667 \\ 2.667 \\ 1.667 \\ 1.667 \\ 1.667 \\ 1.667 \\ 2.667 \\ 1.667 \\ 1.667 \\ 2.667 \\ 1.667 \\ 1.667 \\ 1.667 \\ 1.667 \\ 2.667 \\ 1.667 \end{bmatrix} \quad \alpha_{sq} = \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 13 \\ 14 \\ 15 \\ 16 \end{matrix} \begin{bmatrix} 2.778 \\ 7.111 \\ 2.778 \\ 2.778 \\ 2.778 \\ 2.778 \\ 7.111 \\ 2.778 \\ 2.778 \\ 7.111 \\ 2.778 \\ 2.778 \\ 2.778 \\ 2.778 \\ 7.111 \\ 2.778 \end{bmatrix}$$

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	0	.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	.25	0	.25	0	.25	0	0	0	0	0	0	.25	0	0	0	0
3	0	.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	.25	0	0	0	0	0	0	0	0	0
5	0	.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0	0	.25	0	0	0	0	0	0
7	0	0	0	.25	0	0	0	.25	.25	0	.25	0	0	0	0	0
8	0	0	0	0	0	0	.25	0	0	0	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0	.25	0	0	0	0	0	0
10	0	0	0	0	0	.25	0	.25	.25	0	0	0	.25	0	0	0
11	0	0	0	0	0	0	.25	0	0	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.25
13	0	0	0	0	0	0	0	0	0	.25	0	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.25	0
15	0	0	0	0	.25	0	0	0	0	0	0	.25	0	.25	0	.25
16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.25

Fig. 3-6. Submatrix Q of Absorbing Chain Model for Monitored Subarea in Fig. 3-5

	A	B	C	D	E	F	G	H	J
1	.25	0	.25	0	0	.25	0	0	0
2	0	0	0	0	0	0	0	0	0
3	0	.25	0	.25	0	0	.25	0	0
4	.25	0	.25	.25	0	0	0	0	0
5	0	0	.25	.25	.25	0	0	0	0
6	0	.25	.25	.25	0	0	0	0	0
7	0	0	0	0	0	0	0	0	0
8	0	0	.25	0	.25	.25	0	0	0
9	0	0	0	.25	.25	0	.25	0	0
10	0	0	0	0	0	0	0	0	0
11	0	0	0	0	0	.25	.25	.25	0
12	0	0	0	0	.25	.25	.25	0	0
13	0	0	0	0	0	.25	.25	0	.25
14	0	0	.25	0	0	.25	0	.25	0
15	0	0	0	0	0	0	0	0	0
16	0	0	0	.25	0	0	.25	0	.25

Fig. 3-7. Submatrix R of Absorbing Chain Model for Monitored Subarea in Fig. 3-5

Thus, starting in a transient state or an unsensed intersection, the mean number of blocks a vehicle moves before being sensed is 1.667 or 2.667. The variance of the number of moves for each starting state (1 through 16) is 1.778 which are the entries of

$$[2N - I]\alpha - \alpha_{sq}$$

Since 1.778 is a fraction of 2.778 and 7.111 (the distinct entries of  $\alpha_{sq}$ ), the means given in  $\alpha$  are reliable estimates for the layout in Fig. 3-5.

Note that the probability of being sensed cannot be computed. The probability of being sensed by a sensor in the same relative location as say B (Northeast corner of a subarea) can be determined from NR. See Example 4.

The ratio of sensed intersections to the total number of intersections in a monitored area is of interest. In Fig. 3-5, 4 sensors are each sharing 4 subareas. These are sensors at intersections A, B, H and J. Thus the total number of sensors per subarea for 5 (interior) + 4 (each shared by 4 subareas)/4 or 6. The total number of intersections per subarea is 9 (interior) + 4 (each shared by 4 subareas)/4 + 12 (each shared by 2 subareas)/2 or 16. Thus the ratio of sensed intersections to total intersections is 3/8.

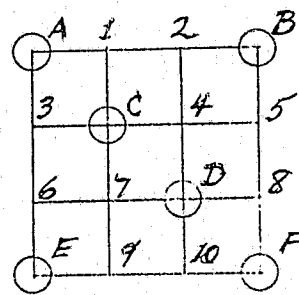


Fig. 3-8. Monitored Subarea with Sensor Density of 3/9

Consider a monitored area with identical subareas as shown in Fig. 3-8 where the ratio of sensed intersections to total intersections is 3/9. Its associated submatrices Q and R appear in Figs. 3-9 and 3-10, respectively. For completeness the fundamental matrix  $N = [I - Q]^{-1}$  corresponding to Fig. 3-8 appears in Fig. 3-11. The entries are rounded off to 3 decimal places.

The mean and variance of the number of blocks a vehicle moves before detection starting from each of the unsensed intersections is 2 and 2, respectively.

	1	2	3	4	5	6	7	8	9	10
1	0	.25	0	0	0	0	.25	0	0	0
2	.25	0	0	.25	0	0	0	0	0	0
3	0	0	0	.25	0	.25	0	0	0	0
4	0	.25	0	0	.25	0	0	0	0	0
5	0	0	0	.25	0	0	0	.25	0	0
6	0	0	.25	0	0	0	.25	0	0	0
7	0	0	0	0	0	.25	0	0	.25	0
8	0	0	0	0	.25	0	.25	0	0	0
9	0	0	0	0	0	0	.25	0	0	.25
10	0	0	0	.25	0	0	0	0	.25	0

Fig. 3-9. Submatrix Q of Absorbing Chain Model for Monitored Subarea in Fig. 3-8

	A	B	C	D	E	F
1	.25	0	.25	0	0	0
2	0	.25	0	.25	0	0
3	.25	0	.25	0	0	0
4	0	0	.25	.25	0	0
5	0	.25	.25	0	0	0
6	0	0	0	.25	.25	0
7	0	0	.25	.25	0	0
8	0	0	0	.25	0	.25
9	0	0	.25	0	.25	0
10	0	0	0	.25	0	.25

Fig. 3-10. Submatrix R of Absorbing Chain Model for Monitored Subarea in Fig. 3-8

	1	2	3	4	5	6	7	8	9	10
1	1.073	0.29	0.021	0.089	0.024	0.084	0.311	0.006	0.083	0.021
2	0.287	1.15	0.006	0.311	0.083	0.024	0.089	0.021	0.024	0.006
3	0.021	0.083	1.073	0.311	0.083	0.29	0.089	0.021	0.024	0.006
4	0.077	0.308	0.003	1.156	0.308	0.019	0.044	0.077	0.012	0.003
5	0.021	0.083	0.006	0.311	1.15	0.024	0.089	0.021	0.024	0.006
6	0.006	0.024	0.021	0.089	0.024	1.15	0.311	0.006	0.083	0.021
7	0.003	0.012	0.077	0.044	0.019	0.311	1.156	0.003	0.308	0.077
8	0.006	0.024	0.021	0.089	0.024	0.083	0.311	1.073	0.083	0.021
9	0.006	0.024	0.021	0.089	0.024	0.083	0.311	0.006	1.15	0.287
10	0.021	0.083	0.006	0.311	0.083	0.024	0.089	0.021	0.29	1.073

FIG. 7. The Fundamental Matrix N Corresponding to Fig. 4

Fig. 3-11. Fundamental Matrix N Corresponding to Fig. 3-8

#### REFERENCE

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**PART FOUR:  
AM BROADCAST AND BURIED  
LOOP FEASIBILITY ANALYSES  
FOR AVM USE**

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I. VEHICLE LOCATION BY MEANS OF AM BROADCASTING STATION CARRIER SIGNALS

Carrier signals of commercial AM broadcasting stations can be used as the source of vehicle location information. As in well-known navigation systems, the signals radiating from pairs of stations will form an hyperbolic grid or coordinate system, and vehicles which are equipped with phase-lock receivers and phase repetition counters can keep track of the location of the vehicle in this hyperbolic coordinate grid. This information is then periodically transmitted to a central command base where the transformation from hyperbolic to geographic coordinates is performed, and the actual location of the vehicle is determined and displayed.

A. Introduction

Most vehicle location and navigation systems require dedicated transmitter-receiving equipment combinations and frequency allocations for the location function. A particular advantage of the AM broadcast phase-difference monitoring system is that commercial station signals (0.53 to 1.60 MHz) are used to furnish the vehicle location information. Therefore, neither dedicated transmitters nor special frequency allocations are required.

Carrier signals from three AM stations located near the urban perimeter are used to form a coordinate system of hyperbolas of constant phase difference between the signals from pairs of stations (Fig. 4-1). Therefore, this vehicle location technique shares many of the characteristics of other hyperbolic navigation methods such as OMEGA, LORAN, and particularly DECCA. In this location method, however, the transmission frequencies from the AM stations need not be synchronized, in contrast to the established navigation systems. It is more akin to the differential versions of the foregoing systems. In the differential versions, mobile location equipment is utilized at fixed geographical sites for the purpose of improving the location accuracy of vehicles in the neighborhood by determining the signal phase or delay variance at the known site from that predicted, and this variance is used to correct the location data received by the vehicle.

The AM broadcast vehicle location technique relies on a frequency transformation method whereby the several frequencies of three AM broadcasting stations are separately normalized to a common frequency, and the relative phases of these common frequencies are compared to provide hyperbolic lines of position. An exact integral relationship between the carrier frequencies of the AM stations is not required, although harmonically related frequencies would result in a stationary "virtual hyperbolic pattern" and would somewhat simplify the location process.

Vehicle equipment consists of at least three phase-locked loop receivers to extract the carrier

\* U.S. Patent 3,889,264.

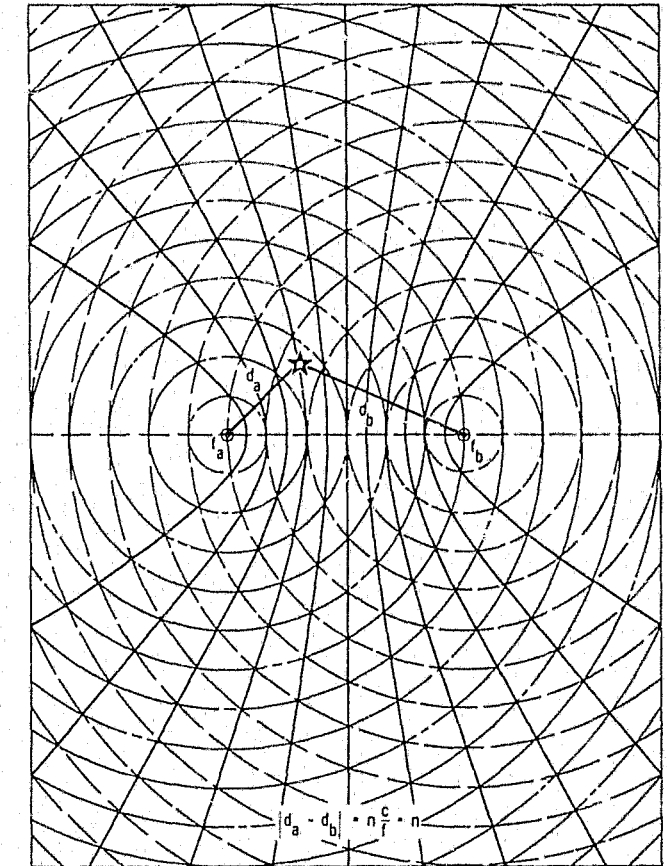


Fig. 4-1. Zero Degree Phase Difference Hyperbolic Contours Produced by Pair of Synchronized RF Signals

frequencies and also a second set of three phase-locked loop frequency multipliers to generate the common frequency. Phase comparators and digital counters are used to keep track of the vehicle location within the "virtual hyperbolic pattern." The hyperbolic coordinates are stored for subsequent transmission to a central command and control base.

Central equipment required consists of a limited arithmetic processor or table look-up computer which is needed to relate the hyperbolic pattern coordinate information to an actual geographical location

B. Hyperbolic Location Principles

If two separated and synchronized sources of radiation transmit signals in an isotropic medium, a receiver positioned midway between them, or on the locus of points which is equidistant from each transmitter, will detect no difference in the time-of-arrival or the phase of the signals from the separate sources. The locus is the perpendicular bisector of the connective between the two sources. (See Fig. 4-1.)

If the receiver is at one side or the other of the bisector, the signal from the nearer transmitter will arrive at some finite amount of time before the signal from the farther source. If the signals are continuously transmitted, the phase of the nearer will lead the phase of the farther. Another locus of constant time or phase difference can be generated by maintaining the same difference in distance from the receiver to each transmitter. The curves for constant time or phase difference will be confocal hyperbolas that are symmetric around the bisector (see Fig. 4-1).

A line-of-position (LOP) can be determined relative to a pair of RF transmitters by noting the time difference in the arrival of the signals, which corresponds to one of the hyperbolas. There will be ambiguity as to which branch of the hyperbola represents the true LOP. If the signals are continuous wave and only the phase differences are determined, the degree of LOP ambiguity increases many-fold since the phase pattern is repeated whenever the cumulative distance change to the two transmitters equals one wavelength. The resolution of the ambiguity is described later.

If the two stations are transmitting on slightly different frequencies, the relative phase between the carriers will change cyclically at a rate determined by the difference in frequency. This rate will be the same anywhere that the two signals can be received. If the locus of lines of constant phase difference are now considered, they again comprise a family of confocal hyperbolas, but instead of being stationary, they will sweep through the area covered by the two stations (Fig. 4-2). The hyperbolas, as a function of time, will tend to

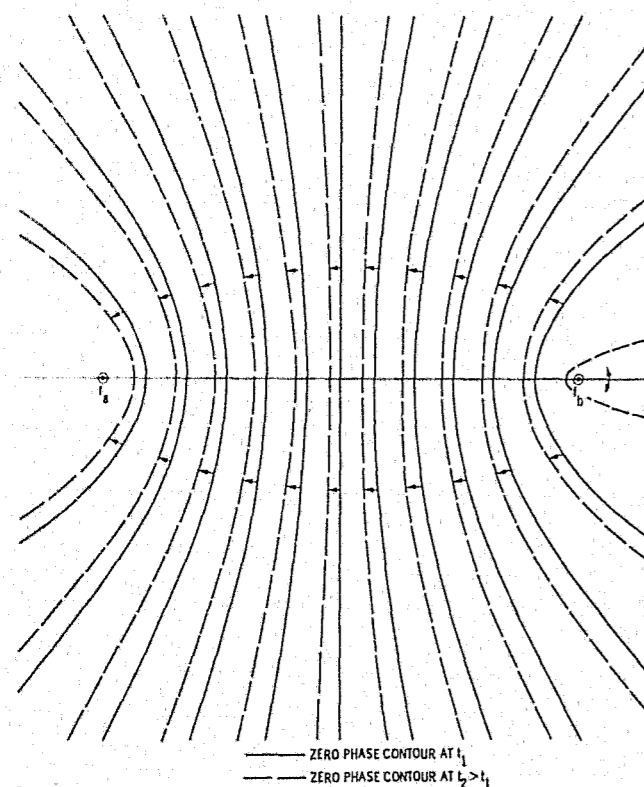


Fig. 4-2. Apparent Motion of Hyperbolas Due to Slight Difference in Two Signal Frequencies

form acutely around the station radiating the higher frequency and then move toward the lower frequency station; straightening as they reach the midpoint, then curving around the lower frequency station and then vanishing on the extension of the line joining the stations. A receiver capable of counting the passage of hyperbolas representing a particular phase difference will accumulate the same count in the same time interval regardless of the location within the service area of the two stations.

If the constant phase difference counting receiver is positioned in a stationary hyperbolic field, no counts will be accumulated as long as the receiver's location is fixed. If the receiver is moved in such a manner as to cause the difference in the distances to the two stations to change by one wavelength, then one count will be accumulated. Similarly, in a moving field, a one-unit difference in counts will be accumulated by a stationary receiver as compared to a receiver that is moved by a wavelength distance difference.

The AVM system based on AM broadcast signals is discrete as opposed to continuous location systems in that the intersections of hyperbolas form a grid which can be transformed into specific urban area locations corresponding to these intersections. Interpolation between grid lines is not used. Therefore it is somewhat like a proximity system with the hyperbolic intersections taking the place of physical devices or signposts located at intersections or at fixed points. Continuous systems provide somewhat uniform coverage of the service area and allow any geographical locations within this area to be determined to some limiting precision dictated by the technique. The grid described by the intersection of the hyperbolas allows the actual geographical location of the vehicle to be somewhere within the hyperbolic triangle described by the coordinates of a particular triad vertex. The dimensions of this triangle are a function of the distance to the foci of the two families of hyperbolas and also of the wavelength of the common frequency. In most continuous AVM systems, the precision diminishes with the distance from the fiducial points. In the AM Broadcast hyperbolic AVM system, the location precision can be adjusted in the principal service area by the choice of the common frequency.

Established navigation systems such as OMEGA, LORAN, and DECCA refer to the areas between adjacent hyperbolas of constant phase as lanes. These navigation lanes vary in width from 1.5 to 15 km, depending on the frequency used in the system, and the principal goal of these methods is to maintain a vehicle's location precisely within a selected lane. In contrast, the AM broadcast vehicle location method utilizes much narrower (e.g., 0.15 km) lanes and keeps track only of the ID number of the hyperbola of constant phase difference that the vehicle has crossed and in which direction the hyperbola was traversed. Therefore, the location precision is a function of the lane width and will vary with the distance from the AM station pair. This system is intended for use in metropolitan areas and adjacent suburbs of rather limited size compared to the much larger service areas of navigation systems. Since AM transmitting sites are usually located near the outskirts of the area they serve, the divergence of the hyperbolas and the consequent loss in location precision can be held to reasonable values.

In many prior studies and developments concerned with emergency vehicle location problems (see Bibliography), a general goal has been to provide a location capability to one city block, or roughly 0.16 km (0.1 mile). Lane widths of this size can be generated with a frequency of 1 MHz.

In order to generate a hyperbolic coordinate system from AM station signals, these signals must be transformed to a common frequency which is phase coherent to the AM carrier. To be useful without restraints requires that this common frequency be a multiple of the highest common divisor of the available AM carriers. The common frequency should therefore be a multiple of 10 kHz.

The individual AM carrier signals are received by the vehicle receivers, and these signals in turn are each used to separately synthesize the common frequency. The common frequencies are therefore phase-coherent with the original AM carriers and effectively change the radiation from each of the AM stations to the common frequency. A virtual hyperbolic pattern is generated from each pair of AM stations received; and if the AM signals were phase coherent, the pattern will be stationary in space. It is then only necessary to measure the phase differences and count the number of times the phase pattern has repeated as the vehicle travels in order to determine a new location from a known starting point. Three pairs of signals (three station) are sufficient to remove any ambiguity in the determination of the new location from the old location (Fig. 4-3). Since the

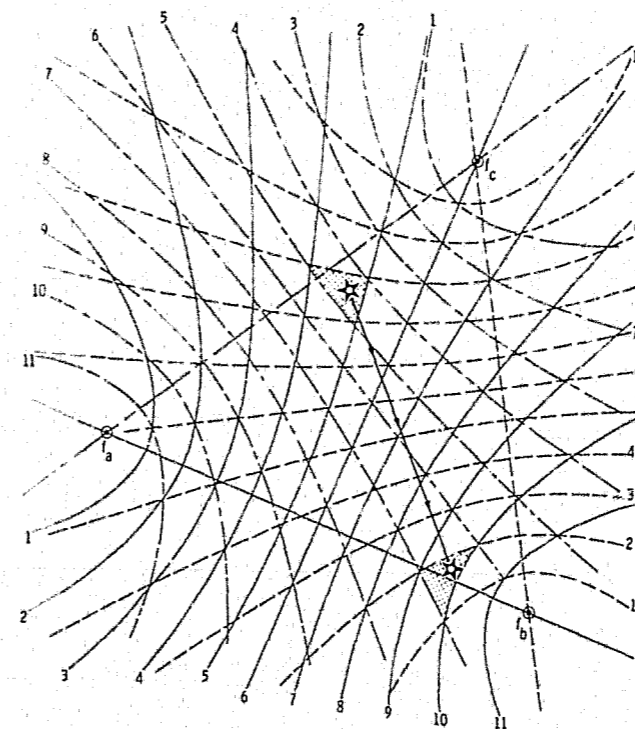


Fig. 4-3. Change in Receiver Location from Hyperbolic Area 5-9-5 to 10-2-7

spacing of the hyperbolic patterns is a function of the distance from the station pair, the relationship between the phase pattern counts and actual distances traveled would have to be computed. In this AVM system, the computational ability need not be

placed in each vehicle. The computation of locations is reserved for the central command base where the location information is desired.

It is immaterial whether the hyperbolic grid pattern is fixed or moving as far as the location process is concerned. If fixed, then only the counts accumulated by moving receivers are necessary to determine the new positions from the old. If the grid is moving, then the difference in counts between the moving receivers and a stationary receiver is all that is required. Besides the magnitude of the counts, it is also necessary to know the "direction" of passage of the hyperbola of constant phase difference. The hyperbolas always move from the higher frequency source toward the lower frequency. If the hyperbolas are stationary, the vehicle's movement toward one source will tend to increase the apparent frequency from that source while decreasing the frequency of the other. Therefore an assignment can be made as to which direction is to be called a positive count and which a negative count.

### C. Vehicle Equipment Requirements

A block diagram of one of the receivers to be installed in the vehicles is shown in Fig. 4-4.

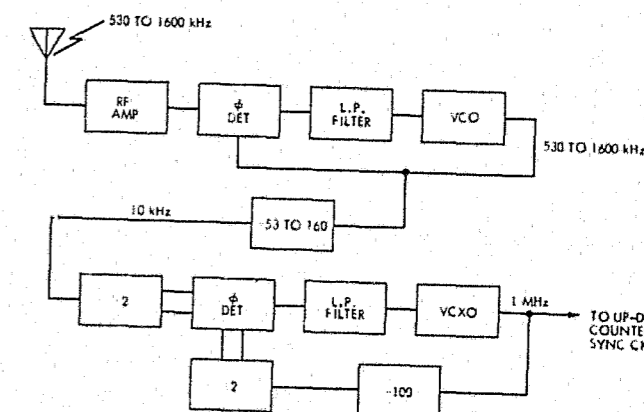


Fig. 4-4. Phase-Locked Loop AM Receiver on Vehicle for Hyperbolic AVM Technique

Three of these receivers are required for each vehicle. A conventional RF amplifier is used to provide selectivity and gain of the desired AM signal applied to the phase detector of the phase-locked loop (PLL). The voltage-controlled oscillator frequency in the PLL is adjusted to run at the same frequency as the AM station carrier. The oscillator output is divided by a variable modulus counter ( $\div 53$  to  $160$ ) so as to produce an output frequency of 10 kHz. The 10 kHz signal is applied to a flip-flop which provides a square-wave of 5 kHz used as the reference input to the phase detector of the frequency multiplying PLL. A 1 MHz voltage-controlled crystal oscillator is phase-locked to the 5 kHz reference by dividing the oscillator frequency by 200 to produce a second 5 kHz signal which is compared to the reference. Therefore, the 1 MHz signal is phase-locked to the AM carrier frequency so that the phase relationship between the 1 MHz and the carrier is repeated at least every 53 to 160 cycles of the AM carrier.

Three such receivers, each tuned to a different AM station, will produce three separate 1 MHz



signals, each phase-coherent with the appropriate AM carrier.

The problem then remains to determine the ID number and direction of the hyperbola that is either traversing or being traversed by the vehicle. As stated previously, the measurement of the frequency difference and the determination of which is the greater frequency are required. The technique selected to determine the frequency difference and also to yield information as to which is the higher or lower frequency is to use an up-down counter in which one frequency provides incrementing pulses and the other decrementing pulses. The state of the counter should then indicate the integrated frequency difference between the two frequencies which is the algebraic sum of the hyperbola of constant phase difference traversed.

The up-down counter must respond to every incrementing and decrementing pulse because any pulse missed will displace the measured location by one unit in the hyperbolic grid. In order to prevent the uncertainty in the up-down counter which could be caused by the simultaneous arrival of up and down pulses, resynchronization of the 1 MHz pulses was required. A synchronizing frequency at least four times the frequency to be counted is required to assure that no pulse is lost or split. The logic for resynchronizing to 4.192 MHz is shown in Fig. 4-5. The logic discards both incrementing and decrementing pulses which are inputs to the same up-down counter and arrive in the same synchronizing interval.

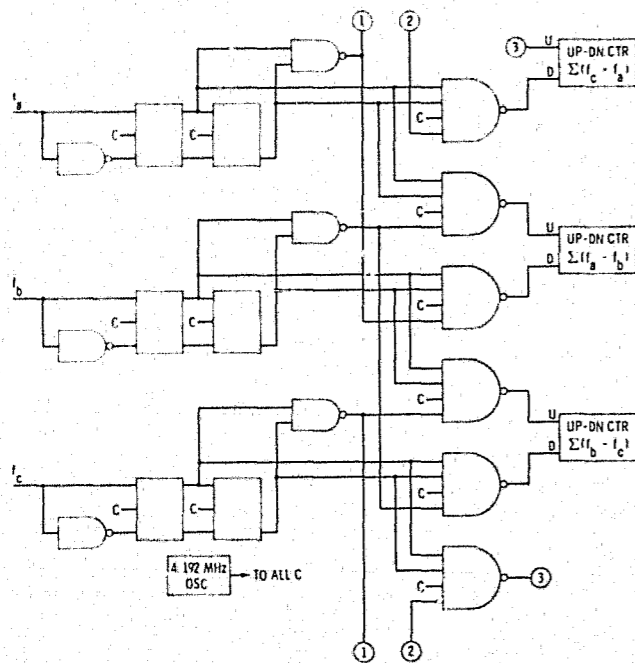


Fig. 4-5. Up-Down Counters Sync Logic for Hyperbolic AVM Technique

Each of the three counters in the receiver maintains a count which is the integrated algebraic sum of the apparent frequency difference between a pair of AM stations each nominally radiating at the common frequency. Part of this frequency difference is due to the AM stations not being phase coherent

(i. e., not exactly on the assigned frequency) and part is due to vehicular motion.

#### D. Vehicle Location Method

If three AM stations, A, B, and C, are monitored (Fig. 4-3) and the transformation of the carriers yields three common frequencies  $f_a$ ,  $f_b$ , and  $f_c$ , then the three counters in the vehicles will accumulate counts  $N$  in a time  $t$  in accordance with:

$$N_a = (f_a - f_b)t + V_{ab} (f)t \times F(x, y) \div C$$

$$N_b = (f_b - f_c)t + V_{bc} (f)t \times G(x, y) \div C$$

$$N_c = (f_c - f_a)t + V_{ca} (f)t \times H(x, y) \div C$$

$$C = 3 \times 10^9 \text{ m/sec}$$

where  $f$  is the common frequency,  $V$  is the vehicle velocity component parallel to the baseline of the station pair, and  $F$ ,  $G$ , and  $H$  are general equations of the second degree (describing the three families of hyperbolas) in terms of  $X$  and  $Y$  which are the geographical location of the vehicle in an arbitrary orthogonal coordinate system. This system of equations does not yield an explicit analytic solution for the location in terms of  $X$  and  $Y$ . It does indicate the separability of the counts due to slight differences in the common frequency and the counts caused by vehicle motion. Counting is negligibly influenced by the difference in frequency of  $f_a$ ,  $f_b$ , or  $f_c$ .

At the base, the location process is initialized by first receiving the actual geographical location (in  $X$  and  $Y$ ) of the vehicle and the initial content of the three counters (called  $N_{ai}$ ,  $N_{bi}$ , and  $N_{ci}$ , respectively). The coordinates in  $X$  and  $Y$  and the counter states are stored. The counter states of the stationary receiver are also stored at the same instant. An explicit calculation is then made using the  $X$ - $Y$  location and the coordinates of the AM stations which yield the location of the vehicle in terms of the parametric families of the hyperbolas. Each hyperbola in each family is numbered, and the results of this calculation give the location in three integers which represent the nearest hyperbola of each family.

Subsequent locations are determined by receiving the current state of the three counters from the vehicle. First, the initial state of the vehicle counters is subtracted from the current state, and second, the change in the state of the stationary receiver counters (from the initializing time to the current time) is determined and subtracted to yield the change in each of the hyperbolic coordinates caused by vehicle motion. The new  $X$ - $Y$  coordinates of the vehicle location are then calculated with an iterative least-squares algorithm. The algorithm uses the old  $X$ - $Y$  location and develops the required changes in  $X$  and  $Y$  so that the calculated new position will have the same hyperbolic coordinates as those determined for the vehicle from the current counter states. This method was chosen over an analytic technique as it yields a "most likely" solution in less time than an analytic method which has the additional disadvantage of having several pairs of coordinates as solutions.

Only two of the three available hyperbolic coordinates are necessary in all of the calculations

as the third coordinate is not independent. The third coordinate does provide a check in that the sum of the hyperbolic coordinates should be a constant plus or minus one. Additionally, for locations near the vertex (the one AM station common to each hyperbolic family), the algorithm may become divergent and another set of coordinates should be used.

#### E. Accuracy Analysis

All AM broadcast stations in the United States operate on assigned carrier frequencies which are multiples of 10 kHz in the frequency region between 530 and 1600 kHz. The FCC requires that the actual carrier frequency be within 20 Hz of the assigned frequency. If all the AM stations within a given geographical area were exactly on the assigned frequency, the relationship between any two stations could be expressed as:

$$(1) f_1/f_2 = (n + p)/n, \text{ where } n \text{ and } p \text{ are both integers.}$$

The carriers could be said to be phase-coherent in that the phase relationships between the two carriers are repeated every  $n + p$  cycles for one carrier and every  $n$  cycles for the other. If this condition is maintained, it is then possible to synthesize another frequency, which is also a multiple of 10 kHz which is phase-coherent to each of the carriers within the area.

The 10 kHz can be multiplied to another frequency, say 1 MHz, which will be phased coherent with the original carrier. Since the FCC allows a frequency tolerance of 20 Hz, the synthesized 1 MHz signal will have a tolerance of:

$$(2) \pm X \text{ Hz} = \pm 20 \text{ Hz} (10^6 \text{ Hz})/f \text{ Hz, where } f \text{ is the AM carrier frequency.}$$

Therefore  $X$  can vary between 39 and 12 Hz, depending upon the frequency of the AM broadcasting carrier. It is therefore possible that a pair of AM stations could cause a beat frequency between the two "normalized" carriers approaching 80 Hz. The impact of the frequency difference is principally upon the equipment design, the sampling rate for location purposes, and the amount of information that must be transmitted from the vehicle. These effects will be discussed later.

A secondary effect of the AM carrier being off frequency and thereby causing the 1 MHz to be slightly off is that the location process will be reduced in precision. A wavelength of the actual frequency will be slightly shorter or longer than expected by up to 39 parts per million. This error would be on the order of 1 meter on the baseline connecting a station pair with a separation of 30 km and up to 2 meters some 60 km away from either station and therefore negligible.

#### F. System Data Requirements and Polling Intervals

System considerations determine how much information is needed from each vehicle and how often it should be sent. Prior work in automatic vehicle monitoring has usually emphasized the fixed-rate polling method of interrogating vehicles

to determine locations. If the polling method allows any or all vehicles to travel at maximum speed and still be located to the ultimate precision, the information flow is maximized from each vehicle. If an average speed is assumed for the fleet of vehicles, then high-speed vehicles will not be located to the precision available, and parked or slowly moving vehicles will be transmitting much redundant data. Volunteer methods wherein the vehicle initiates a data transmission whenever a significant change in location has occurred require means to avoid contention and must also send additional data to identify which vehicle is transmitting. An adaptive polling technique whereby high-speed vehicles are interrogated at much shorter intervals and where average and slowly moving or parked vehicles are infrequently sampled is quite easily mechanized. The simplest polling technique requires that the central control transmit incrementing pulses (tones, or tone bursts) to all vehicles which count and accumulate these incremental signals. When the number of signals received matches the number assigned to the vehicle, a data transmission is initiated from the vehicle. The inclusion of a respond or do-not-respond pulse, tone, or burst with the incrementing signal will tell the vehicle whether data is required or not. Conversely, a vehicle which had been immobile could request inclusion in the next polling sequence by responding with an appropriate signal regardless of the command not to send data.

The amount that the AM carriers are off frequency together with the sampling intervals of the vehicles determines the number of bits required to be sent to the central command for location purposes. The length of each of the up-down counters is therefore determined by this number of bits. As stated before, two low-end of the band AM stations could cause an 80 Hz beat frequency in the synthesized 1 MHz signals which would cause a total count of about 288,000 per hour to be accumulated. A vehicle cruising at 30 km/hr along the baseline of a station pair would accumulate a count of 200 per hour due to a stationary pattern. A recent Department of Transportation requirement for vehicle monitoring required that 25% of the vehicle fleet be located each 15 sec and the remainder located each minute. The total counts for each station pair under these requirements would be 1200 for 15 sec and about 5000 for the minute interval. To accommodate this requirement, the length of the up-down counters would have to be 13 bits each. Some 40 to 50 bits per interrogation would have to be transmitted from each vehicle if a preamble, parity checks, or error detection information was added to the basic 39 bits of location data. Assuming the higher number over a voice channel from the vehicle which could conservatively accommodate 1200 bit/sec, then 24 vehicles could be interrogated and located each second. Again using the DOT requirement, 820 vehicles could be located each minute, with 205 of the vehicles being located each 15 seconds, or four times each minute for a total of 1435 locations each minute (1440 maximum). It should be realized that these are theoretical maximum numbers and neglect the practical realities of turn-on stabilization time of mobile transmitters and also assumes another channel for interrogation purposes.

The amount of data required from each vehicle could be reduced by about two-thirds if the AM

stations being utilized for location maintained phase coherency. A stationary location pattern would be generated, and the up-down counter lengths could be reduced substantially as only counts due to vehicle motion would be accumulated. Only a relatively small amount of equipment would be necessary at each AM station to maintain the carriers coherent to one another. This could be done by either a common synchronizing signal or with each station referencing the carrier frequency to the other two carriers by counting and phase-locked loop techniques. In either case, the control range of the added equipment must not allow the carrier to be pulled outside of the 20 cycle FCC tolerance limit.

Some operational difficulties that might occur with this type of vehicle location system could be caused by momentary outages of one of the AM carriers, or transmitter switchover when power is increased or reduced. In some smaller metropolitan areas it may be difficult to find three "24-hr" broadcast stations with appropriate geometry, and different configurations may have to be used for day and night operation.

### G. Computer Simulation Programs

Two computer programs, a location simulator called LOCATE (Table 4-1), and a vehicle count

Table 4-1. Vehicle Location Simulator Program, LOCATE

```

*LOCATE(1)
*LOCATE
[1] X0=X0,X3[1]
[2] Y0=Y0,Y3[1]
[3] D=300
[4] X=X1[1]
[5] Y=Y2[2]
[6] HP=L-1
[7] D=((X-X0)*2)+((Y-Y0)*2)+0.5
[8] D=D,D[1]
[9] CR=300
[10] RE=L-((X-X0[L])*D[L])-((X-X0[1])*D[1])
[11] CR=((CR[1]-LAP[1]),(CR[3]-CR[3]))*300
[12] H[L]=((Y-Y0[L])*D[L])-((Y-Y0[1])*D[1])
[13] CR[L]=D[L]-D[1]-D[1],CR[L]
[14] RE=L-((2*L-L+1))
[15] DEH=((A+2)*(D+2))-((A+3)*2)
[16] AX=((A+CR)*D+2)-((A+CR)*D+2)
[17] AY=((A+2)*(D+2))-((A+2)*D+2)
[18] X=X-AX
[19] Y=Y-AY
[20] IF ((|AX|>10) OR (|AY|>10))
[21] OLD=X,Y
[22] NEW=X AND Y ARE: OLD
[23] AX AND AY ARE: (X-X),(Y-Y)

```

generator called PIG (Table 4-2) were written to test the location method. A SETAUP program (Table 4-3) was also written which stores the locations of the AM stations in the arbitrary coordinate system and determines the lengths of the baselines connecting the stations.

In order to make the simulation more realistic, three AM stations in the Los Angeles, CA, metropolitan area were chosen: KFI (640 kHz) located in the Buena Park-La Mirada area southwest of the Los Angeles Civic Center; KNX (1070 kHz) in Torrance which is south and slightly west of the Civic Center; and KMPC (710 kHz) with transmitter in North Hollywood which is northwest of the Civic Center. The baseline distances are: KFI-KNX 31 km; KNX-KMPC 35 km; and KMPC-KFI 51 km.

Table 4-2. Vehicle Hyperbolic Lane Count Generator Program, PIG

```

*PIG(1)
*PIG
[1] X0=X0,X3[1]
[2] Y0=Y0,Y3[1]
[3] D=300
[4] X=X1[1]
[5] Y=Y2[2]
[6] HP=L-1
[7] D=((X-X0)*2)+((Y-Y0)*2)+0.5
[8] D=D,D[1]
[9] CR=300
[10] RE=L-((X-X0[L])*D[L])-((X-X0[1])*D[1])
[11] CR=((CR[1]-LAP[1]),(CR[3]-CR[3]))*300
[12] H[L]=((Y-Y0[L])*D[L])-((Y-Y0[1])*D[1])
[13] CR[L]=D[L]-D[1]-D[1],CR[L]
[14] RE=L-((2*L-L+1))
[15] DEH=((A+2)*(D+2))-((A+3)*2)
[16] AX=((A+CR)*D+2)-((A+CR)*D+2)
[17] AY=((A+2)*(D+2))-((A+2)*D+2)
[18] X=X-AX
[19] Y=Y-AY
[20] IF ((|AX|>10) OR (|AY|>10))
[21] OLD=X,Y
[22] NEW=X AND Y ARE: OLD
[23] AX AND AY ARE: (X-X),(Y-Y)

```

Table 4-3. AM Broadcast Station Locations and Baseline Lengths Program, SETAUP

```

*SETAUP(1)
*SETAUP
[1] Q=0,X AND Y FOR EACH OF THREE AM STATIONS IN METERS.
[2] Q=0
[3] X1=C[1]
[4] X2=C[2]
[5] X3=C[3]
[6] Y1=C[4]
[7] Y2=C[5]
[8] Y3=C[6]
[9] A=((X2+X1)*2)+((X3+X2)*2)+((X1+X3)*2)
[10] B=((Y2+Y1)*2)+((Y3+Y2)*2)+((Y1+Y3)*2)
[11] E=((X2-X1)*(X3-X2)+(X1-X3))
[12] F=((Y2-Y1)*(Y3-Y2)+(Y1-Y3))
[13] L=1
[14] RE=L-((E[L]*2)+((F[L]*2))+0.5)

```

An arbitrary origin for the coordinate system was located some 8 km (5 miles) in the Pacific west of the Palos Verdes peninsula such that most of the area of interest for location purposes would be in the first quadrant of the X-Y system. The origin is at 118°30'W and 33°45'N.

The location (LOCATE) program and the vehicle count generator (PIG) program were written in APL computer language. The vehicle count generator requires two input variables. These are the initial and terminal values in meters of the X-Y coordinates representing each change of position of the vehicle. The hyperbolic coordinates of each location are calculated and the integral difference determined. The difference represents the counts that would be accumulated by a vehicle in traveling from the initial to the terminal location of each leg of travel. The count difference and the initial location are the inputs to the LOCATE routine which determines the new location. The new location is determined by a reiterative technique whereby the deltas of X and Y which would satisfy

the change in counts of the hyperbolic coordinates are calculated and added to the initial location.

### H. Conclusions

A vehicle location method for use in metropolitan areas is available, which uses the carrier signal information from three currently operating AM broadcasting stations located near the urban perimeters. Two advantages of the method are that (1)

dedicated transmitters for location purposes are not required and that (2) the phase-lock-loop counting receivers installed in the vehicles are inexpensive. The mathematical technique for vehicle location is relatively simple and requires only that the initial location be known. While the technique is not explicit, location can be determined with adequate accuracy to the precision implied by the geometric configurations of the AM stations used and the frequency of the synthesized signal used for phase comparison.

## II. VEHICLE LOCATION BY MEANS OF BURIED LOOPS\*

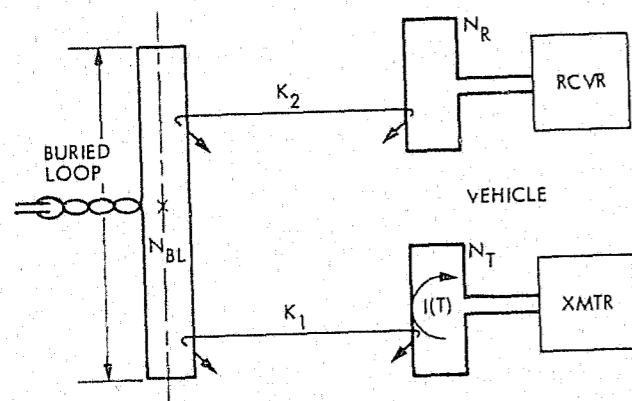
Lawrence J. Zottarelli

With the exception of the cut-to-fit development method, the evaluation of the buried loop\* AVM system requires as a basis some mathematically analytic relations. Since such relations do not seem readily available in the open literature, an analytic approach was developed to determine the effects of loop spacings, dimensions, and height above roadway on RF signal detection and on identification of the vehicle's location.

### A. Relationships of Three-Loop Vehicle Location System

The approach is to find the mutual inductance of the vehicle's transmitter and receiver loops through the intermediary of the passive buried loop. A typical three-loop configuration is shown in Fig. 4-6. The assumptions are:

1. The XMTR and RCVR are sufficiently remote from each other so that direct mutual inductance is of secondary importance.
2. The buried loop is tuned with a capacitor to the vehicle transmitter frequency, and the buried loop resistance is directly proportional to the number of turns.
3. The loops are in an isotropic medium.



$I(T)$  = XMTR CURRENT  
 $K_1$  = XMTR/BL COUPLING  
 $K_2$  = RCVR/BL COUPLING  
 $N_R$  = RCVR TURNS  
 $N_T$  = XMTR TURNS  
 $N_{BL}$  = BURIED LOOP TURNS  
 $R_{BL}$  = BL RESISTANCE

Fig. 4-6. Configuration of Vehicle's Transmitting and Receiving Loops Relative to Buried Loop

### 1. Analytic Relations of Loop Mutual Inductances

- (1) The magnetic flux lines  $\Phi$  coupling the buried loop (BL) due to the XMTR current  $I(T)$  at point P is

$$\Phi_{BL} = K_1 \cdot N_T \cdot I(T)$$

where

$$I(T) = I_P \sin(\omega t), K_1 = \text{XMTR/BL}$$

coupling, and  $N_T = \text{XMTR turns}$ .

- (2) The voltage  $E$  coupled to the buried loop with width  $W$  is

$$E_{BL}(T) = N_{BL} \frac{d\Phi_{BL}}{dt} = W \cdot K_1 \cdot N_T \cdot N_{BL} \cdot I_P \cdot \cos(\omega t)$$

- (3) The current in the buried loop (which is at resonance), with resistance  $R$ , is

$$I_{BL}(T) = E_{BL}(T) / R_{BL} = \frac{[K_1 \cdot N_T \cdot N_{BL} \cdot W \cdot I_P \cdot \cos(\omega t)]}{R_{BL}}$$

- (4) The flux lines coupling  $K_2$  the RCVR due to the buried loop is

$$\Phi_{RCVR}(T) = K_2 \cdot N_{BL} \cdot I_{BL}(T)$$

substituting

$$\Phi_{RCVR}(T) = \frac{[-K_1 \cdot K_2 \cdot N_T \cdot (N_{BL})^2 \cdot W \cdot I_P \cdot \cos(\omega t)]}{R_{BL}}$$

- (5) The voltage at the RCVR due to the buried loop is

$$E_{RCVR} = N_R \frac{d\Phi_{RCVR}}{dt} = \frac{[-K_1 \cdot K_2 \cdot N_T \cdot N_{BL} \cdot N_R \cdot (W I_P)^2 \cdot \sin(\omega t)]}{R_{LOOP}}$$

allowing now the resistance per turn (R/turn)

$$R_{loop} = (R/\text{turn}) \cdot N_{BL}$$

$$\text{QED: } E_{RCVR} = \frac{[-K_1 \cdot K_2 \cdot N_T \cdot N_{BL} \cdot N_R \cdot (W I_P)^2 \cdot \sin(\omega t)]}{(R/\text{turn})}$$

2. Comments. The reasoning involved in deriving the relationship permit the geometrical and electrical aspects of the solution to be separable and simply multiplicative. If  $E_{RCVR}$  is to be of the form  $M dI/dt$  then:

$$M_{\text{equivalent}} \text{ becomes } \frac{[K_1 \cdot K_2 \cdot N_T \cdot N_R \cdot N_{BL} \cdot (W I_P)]}{(R/\text{turn})}$$

and

$$I(t) \text{ becomes } I_P \cos(\omega t)$$

### B. Magnetic Field Generated by Rectangular Loop of Wire

1. Development of Flux Density Equations. It is desired to find the flux intensity  $B$  at a point  $P(x, y, z)$  generated by the rectangular loop of wire, with the X-axis direction across the lane width and the Y-axis in the direction of roadway travel.

Given:

- (1) A rectangular loop of wire of length  $L$  and width  $W$ , with the lane width equal to the buried loops length.
- (2) The loop is in a free-space plane (of  $x, y, z$  rectangular coordinates) having equations  $z = 0$ .
- (3) The loop has a DC current of  $I$ .
- (4) The coordinate space has its origin at  $(0, 0, 0)$ , which is the center of the loop wire.
- (5) The linkage or mutual inductance of two parallel planar loops (not necessarily coplanar) lying in  $x, y$ -plane uses only the  $z$ -component of flux density.

Method:

- (1) Decompose the loop into four linear segments
- (2) Apply the Biot Savart law from each segment to the point of interest

$$|B_p| = \left(\frac{\mu}{4\pi}\right) \cdot \left(\frac{I}{a}\right) \cdot (\cos\gamma - \cos\alpha)$$

- (3) Decompose the flux density into its vector components, and sum the components.

The complete mathematical analysis is presented in Ref. 1.

### C. Computer Programs for Calculating Mutual Inductance

Two programs are used to generate the mutual inductance of rectangular wire loops. The programs LOOPS and CARCUP are written in the Stanford Artificial Intelligence Language, "SAIL," which is an extended ALGOL 60.

#### 1. "LOOPS" and "CARCUP" Programs.

The "LOOPS" program is used to find (1) the XMTR/RCVR direct mutual coupling, (2) the self inductance of a loop, and (3) the direct coupling

between the Buried Loop and the XMTR or between the Buried Loop and the RCVR or between two Buried Loops. The "CARCUP" program is used to find the mutual coupling between the XMTR and the RCVR via the Buried Loop, the inner workings of the two programs are similar; the program "CARCUP" is, in effect, the program "LOOPS" run twice. Both of the programs have Input/Output in common.

a. **LOOPS Program.** This program (Table 4-4) asks the user: (1) if he wants more detailed information, (2) to specify "how many steps," or data points, (3) where is the starting point of the pickup loop and what size is the loop (in terms of XMIN, XMAX, YMIN, YMAX) and how high above the buried loop (in terms of Z), (4) to specify the aspect ratio of the buried loop, K.

The LOOPS program calculates and prints out the mutual inductance for the number of data points specified. Each successive data point represents the mutual inductance of the buried loop and pickup loop moving along the positive Y-direction (along the roadway lane) by 1/10 of its length (i. e.,  $(YMAX - YMIN)/10$ ). The mutual inductance is in relative units. To find the answer in henrys, multiply the answer by half the lane width (in meters), by  $10^{-7}$ , by the number of turns of the buried loop, and by the number of turns of the pickup loop.

b. **CARCUP Program.** This program (Table 4-5) asks the user: (1) if he wants more detailed information, (2) to specify "how many steps," or data point, (3) where is the starting point of the XMTR loop, and what is its size and how high above the buried loop (in terms of XMIN, XMAX, YMIN, YMAX, ZT); also where is the starting point of the RCVR loop and

Table 4-4. LOOPS Program for Mutual Inductance of Buried/Pickup Loops, and Sample Run

```
.TYPE LOOPS.SAI
00100 BEGIN "LOOPS"
00150 INTERNAL INTEGER EXIT, NFOREF, I
00200 INTEGER I, J, IERR
00300 DEFINE FF=1E-11
00400 REAL XMIN, XMAX, YMIN, YMAX, Z, X, Y, ZT, XMINX, XMAXX, YMINY, YMAXX, ZT, IERR
00500 SHAR, L, W, G, F, R, T, D, E, Z, X, Y, ZT, XMINX, XMAXX, YMINY, YMAXX, ZT, IERR
00550 STRING STI
00600 OUTSTR "DO YOU WANT NOTES (TYPE IN EITHER YES OR NO FOLLOWED BY
CAP RET) "
00700
00800 IF INCHLINES THEN OUTTR "
00900 THE PURPOSE OF THIS PROGRAM IS TO CALCULATE THE FREE SPACE
RELATIVE COUPLING BETWEEN TWO FLAT BUT NON-COPLANAR RECTANGULAR
LOOPS OF WIRE THE SIDES OF WHICH ARE PARALLEL TO THE COORDINATE
AXES OF REFERENCE. IT IS TO BE APPLIED IN AUTOMOTIVE VEHICLE
LOCATION HENCE THE TENDR OF THE FOLLOWING INFORMATION.
01400 THE LANE WIDTH IS THE DIMENSION OF THE LANE LENGTH IS
01500 THE Y DIMENSION THE VERTICAL DISTANCE BETWEEN LOOPS IS THE
Z DIMENSION. THE CENTER OF THE BURIED LOOP IS AT COORDINATES
01600 0,0,0. THE WIDTH OF THE BURIED LOOP IS THE LANE WIDTH.
01700 K IS THE ASPECT RATIO OF THE BURIED LOOP (WIDTH DIVIDED BY
LENGTH).
01900 XMIN, XMAX, YMIN, YMAX DETERMINE THE SIDES AND LOCATION OF THE
PICKUP LOOP.
02100 ALL INPUT DIMENSIONS ARE TO BE NORMALIZED TO HALF THE LANE
WIDTH.
02400 HOW MANY STEPS REFERS TO MOVING THE PICKUP LOOP ALONG
THE LANE LENGTH GENERALLY AWAY FROM ABOVE THE BURIED LOOP BY
02500 1/10 OF THE PICKUP LOOP LENGTH AND THEN CALCULATING ITS
NORMALIZED Z DIRECTION COUPLING FROM THE BURIED LOOP.
02700 THE PRINTOUT IS THE CALCULATED FLUX IN RELATIVE FLUX UNITS
02800 AND OF SUCCESSIBLE STEPS IN HENRY.
02900 TO FIND THE ACTUAL FLUX IN VOLT SECONDS, MULTIPLY THE DATA
BY THE FOLLOWING FACTOR:
03000 (1) * (LANE WIDTH / 2) * (10^-7)
03300 WHERE I IS THE BURIED LOOP CURRENT IN AMPS
03400 WHERE THE LANE WIDTH IS IN METERS * (10^-7)
03500 OUTSTR "HOW MANY STEPS "
03600 I=10+REAL(CAN) * (1+INCHLINES) * FF * IERR * IERR * IERR
03700 BEGIN
03750 REAL ARRAY V(1:10)
03800 OUTSTR "XMIN=" XMIN REALSCAN (ST+INCHML) * ERK * IERR * IERR * IERR
03900 OUTSTR "XMAX=" XMAX REALSCAN (ST+INCHML) * ERK * IERR * IERR * IERR
04000 OUTSTR "YMIN=" YMIN REALSCAN (ST+INCHML) * ERK * IERR * IERR * IERR
04100 OUTSTR "YMAX=" YMAX REALSCAN (ST+INCHML) * ERK * IERR * IERR * IERR
04200 X=XMIN+X*(XMAX-XMIN)/10
```

\*U. S. Patent 3,772,691, "Automatic Vehicle Location System."

Table 4-4. (Continued)

```

04300 Y=YMIN:YR*(XMIN-YMIN)/L
04400 YEND=YMIN+YR*L
04500 T=0:1:10:0
04600 OUTSTR="REAL COUPLING INCHES" IF K=1 OUTSTR="FEET"
04700 E=2:2:1:1:1:1
04800 OUTSTR="REAL COUPLING INCHES" IF K=1 OUTSTR="FEET"
04900 E=1:1:0:0:0:0
04950 BEGIN
05000 PROCEDURE BIZ
05100 BEGIN
05200 A=C*(1+ID)/(1+ID+L)
05300 C=C*(1+ID)/(1+ID+L)
05400 AA=C*(1+ID)/(1+ID+L)
05500 BB=C*(1+ID)/(1+ID+L)
05600 F=C*(1+ID)/(1+ID+L)
05700 H=C*(1+ID)/(1+ID+L)
05800 P=C*(1+ID)/(1+ID+L)
05900 R=C*(1+ID)/(1+ID+L)
06000 M=C*(1+ID)/(1+ID+L)
06100 B=C*(1+ID)/(1+ID+L)
06200 END
06300 PROCEDURE FLUXCUP
06400 BEGIN
06500 SETFORMAT(13,3)
06600 WHILE Y GEO YMIN AND Y LEO (YEND-(.9999)*YR) DO
06700 BEGIN
06800 BIZ T=2:2:1:1:1:1
06900 END
07000 Y=C*(1+ID)/(1+ID+L)
07100 YEND=YMIN+YR*L
07200 Y=C*(1+ID)/(1+ID+L)
07300 YEND=YMIN+YR*L
07400 END
07500 WHILE J LEO (1:10) DO
07600 BEGIN
07700 WHILE (J+10) I DO
07800 D=D+(V(I)/I)+1
07900 END
08000 OUTSTR="VOLTAGE"
08100 D=D+(V(I)/I) IF (I MOD 5) = 0 THEN OUTSTR="FEET"
08200 END
08300 END
08400 END
08500 FLUXCUP
08600 ENDE
08700 END LOOP

```

DO YOU WANT NOTES (TYPE IN EITHER YES OR NO FOLLOWED BY CARPET) YES

THE PURPOSE OF THIS PROGRAM IS TO CALCULATE THE FREE SPACE RELATIVE COUPLING BETWEEN TWO FLUX LOOPS OF ANY RECTANGULAR CROSS SECTION. THE SIZE OF EACH LOOP IS PARALLEL TO THE COORDINATE AXES OF REFERENCE. IT IS TO BE APPLIED IN AUTOMOTIVE VEHICLE LOCATION WHERE THE VERTICAL DIMENSION IS THE LANE LENGTH IS THE LANE WIDTH IS THE HORIZONTAL DISTANCE BETWEEN LOOPS IS THE 2-DIMENSION. THE CENTER OF THE BURIED LOOP IS AT COORDINATED 0,0. THE WIDTH OF THE BURIED LOOP IS THE LANE WIDTH. K IS THE ASPECT RATIO OF THE BURIED LOOP (WIDTH DIVIDED BY LENGTH).

XMIN, XMAX, YMIN, YMAX DETERMINE THE SIZE AND LOCATION OF THE PICKUP LOOP.

ALL INPUT DIMENSIONS ARE TO BE NORMALIZED TO HALF THE LANE WIDTH.

HOW MANY STEPS REFERS TO MOVING THE PICKUP LOOP ALONG THE LANE LENGTH (GENERALLY AWAY FROM THE BURIED LOOP) BY 1/10 OF THE PICKUP LOOP LENGTH AND THEN CALCULATING IT. NORMALIZED 2-DIRECTION COUPLING FROM THE BURIED LOOP. THE PRINTOUT IS THE CALCULATED FLUX IN RELATIVE FLUX UNITS AND OF COURSE THE EFFECTIVE.

TO FIND THE ACTUAL FLUX IN VOLT SECONDS MULTIPLY THE DATA BY THE FOLLOWING FACTORS:

WHERE 1 IS THE BURIED LOOP CURRENT IN AMPERE  
 WHERE THE LANE WIDTH IS IN METERS  
 HOW MANY STEPS = 10

XMIN=1				
YMIN=0.001:0.01				
YMAX=1				
F=1				
.2473	.1033	.1033	.1033	.1033
.1029	.1033	.1033	.1033	.1033
.1025	.1033	.1033	.1033	.1033
.1021	.1033	.1033	.1033	.1033
.1017	.1033	.1033	.1033	.1033
.1013	.1033	.1033	.1033	.1033
.1009	.1033	.1033	.1033	.1033
.1005	.1033	.1033	.1033	.1033
.1001	.1033	.1033	.1033	.1033
.9997	.1033	.1033	.1033	.1033
.9993	.1033	.1033	.1033	.1033
.9989	.1033	.1033	.1033	.1033
.9985	.1033	.1033	.1033	.1033
.9981	.1033	.1033	.1033	.1033
.9977	.1033	.1033	.1033	.1033
.9973	.1033	.1033	.1033	.1033
.9969	.1033	.1033	.1033	.1033
.9965	.1033	.1033	.1033	.1033
.9961	.1033	.1033	.1033	.1033
.9957	.1033	.1033	.1033	.1033
.9953	.1033	.1033	.1033	.1033
.9949	.1033	.1033	.1033	.1033
.9945	.1033	.1033	.1033	.1033
.9941	.1033	.1033	.1033	.1033
.9937	.1033	.1033	.1033	.1033
.9933	.1033	.1033	.1033	.1033
.9929	.1033	.1033	.1033	.1033
.9925	.1033	.1033	.1033	.1033
.9921	.1033	.1033	.1033	.1033
.9917	.1033	.1033	.1033	.1033
.9913	.1033	.1033	.1033	.1033
.9909	.1033	.1033	.1033	.1033
.9905	.1033	.1033	.1033	.1033
.9901	.1033	.1033	.1033	.1033
.9897	.1033	.1033	.1033	.1033
.9893	.1033	.1033	.1033	.1033
.9889	.1033	.1033	.1033	.1033
.9885	.1033	.1033	.1033	.1033
.9881	.1033	.1033	.1033	.1033
.9877	.1033	.1033	.1033	.1033
.9873	.1033	.1033	.1033	.1033
.9869	.1033	.1033	.1033	.1033
.9865	.1033	.1033	.1033	.1033
.9861	.1033	.1033	.1033	.1033
.9857	.1033	.1033	.1033	.1033
.9853	.1033	.1033	.1033	.1033
.9849	.1033	.1033	.1033	.1033
.9845	.1033	.1033	.1033	.1033
.9841	.1033	.1033	.1033	.1033
.9837	.1033	.1033	.1033	.1033
.9833	.1033	.1033	.1033	.1033
.9829	.1033	.1033	.1033	.1033
.9825	.1033	.1033	.1033	.1033
.9821	.1033	.1033	.1033	.1033
.9817	.1033	.1033	.1033	.1033
.9813	.1033	.1033	.1033	.1033
.9809	.1033	.1033	.1033	.1033
.9805	.1033	.1033	.1033	.1033
.9801	.1033	.1033	.1033	.1033
.9797	.1033	.1033	.1033	.1033
.9793	.1033	.1033	.1033	.1033
.9789	.1033	.1033	.1033	.1033
.9785	.1033	.1033	.1033	.1033
.9781	.1033	.1033	.1033	.1033
.9777	.1033	.1033	.1033	.1033
.9773	.1033	.1033	.1033	.1033
.9769	.1033	.1033	.1033	.1033
.9765	.1033	.1033	.1033	.1033
.9761	.1033	.1033	.1033	.1033
.9757	.1033	.1033	.1033	.1033
.9753	.1033	.1033	.1033	.1033
.9749	.1033	.1033	.1033	.1033
.9745	.1033	.1033	.1033	.1033
.9741	.1033	.1033	.1033	.1033
.9737	.1033	.1033	.1033	.1033
.9733	.1033	.1033	.1033	.1033
.9729	.1033	.1033	.1033	.1033
.9725	.1033	.1033	.1033	.1033
.9721	.1033	.1033	.1033	.1033
.9717	.1033	.1033	.1033	.1033
.9713	.1033	.1033	.1033	.1033
.9709	.1033	.1033	.1033	.1033
.9705	.1033	.1033	.1033	.1033
.9701	.1033	.1033	.1033	.1033
.9697	.1033	.1033	.1033	.1033
.9693	.1033	.1033	.1033	.1033
.9689	.1033	.1033	.1033	.1033
.9685	.1033	.1033	.1033	.1033
.9681	.1033	.1033	.1033	.1033
.9677	.1033	.1033	.1033	.1033
.9673	.1033	.1033	.1033	.1033
.9669	.1033	.1033	.1033	.1033
.9665	.1033	.1033	.1033	.1033
.9661	.1033	.1033	.1033	.1033
.9657	.1033	.1033	.1033	.1033
.9653	.1033	.1033	.1033	.1033
.9649	.1033	.1033	.1033	.1033
.9645	.1033	.1033	.1033	.1033
.9641	.1033	.1033	.1033	.1033
.9637	.1033	.1033	.1033	.1033
.9633	.1033	.1033	.1033	.1033
.9629	.1033	.1033	.1033	.1033
.9625	.1033	.1033	.1033	.1033
.9621	.1033	.1033	.1033	.1033
.9617	.1033	.1033	.1033	.1033
.9613	.1033	.1033	.1033	.1033
.9609	.1033	.1033	.1033	.1033
.9605	.1033	.1033	.1033	.1033
.9601	.1033	.1033	.1033	.1033
.9597	.1033	.1033	.1033	.1033
.9593	.1033	.1033	.1033	.1033
.9589	.1033	.1033	.1033	.1033
.9585	.1033	.1033	.1033	.1033
.9581	.1033	.1033	.1033	.1033
.9577	.1033	.1033	.1033	.1033
.9573	.1033	.1033	.1033	.1033
.9569	.1033	.1033	.1033	.1033
.9565	.1033	.1033	.1033	.1033
.9561	.1033	.1033	.1033	.1033
.9557	.1033	.1033	.1033	.1033
.9553	.1033	.1033	.1033	.1033
.9549	.1033	.1033	.1033	.1033
.9545	.1033	.1033	.1033	.1033
.9541	.1033	.1033	.1033	.1033
.9537	.1033	.1033	.1033	.1033
.9533	.1033	.1033	.1033	.1033
.9529	.1033	.1033	.1033	.1033
.9525	.1033	.1033	.1033	.1033
.9521	.1033	.1033	.1033	.1033
.9517	.1033	.1033	.1033	.1033
.9513	.1033	.1033	.1033	.1033
.9509	.1033	.1033	.1033	.1033
.9505	.1033	.1033	.1033	.1033
.9501	.1033	.1033	.1033	.1033
.9497	.1033	.1033	.1033	.1033
.9493	.1033	.1033	.1033	.1033
.9489	.1033	.1033	.1033	.1033
.9485	.1033	.1033	.1033	.1033
.9481	.1033	.1033	.1033	.1033
.9477	.1033	.1033	.1033	.1033
.9473	.1033	.1033	.1033	.1033
.9469	.1033	.1033	.1033	.1033
.9465	.1033	.1033	.1033	.1033
.9461	.1033	.1033	.1033	.1033
.9457	.1033	.1033	.1033	.1033
.9453	.1033	.1033	.1033	.1033
.9449	.1033	.1033	.1033	.1033
.9445	.1033	.1033	.1033	.1033
.9441	.1033	.1033	.1033	.1033
.9437	.1033	.1033	.1033	.1033
.9433	.1033	.1033	.1033	.1033
.9429	.1033	.1033	.1033	.1033
.9425	.1033	.1033	.1033	.1033
.9421	.1033	.1033	.1033	.1033
.9417	.1033	.1033	.1033	.1033
.9413	.1033	.1033	.1033	.1033
.9409	.1033	.1033	.1033	.1033
.9405	.1033	.1033	.1033	.1033
.9401	.1033	.1033	.1033	.1033
.9397	.1033	.1033	.1033	.1033
.9393	.1033	.1033	.1033	.1033
.9389	.1033	.1033	.1033	.1033
.9385	.1033	.1033	.1033	.1033
.9381	.1033	.1033	.1033	.1033
.9377	.1033	.1033	.1033	.1033
.9373	.1033	.1033	.1033	.1033
.9369	.1033	.1033	.1033	.1033
.9365	.1033	.1033	.1033	.1033
.9361	.1033	.1033	.1033	.1033
.9357	.1033	.1033	.1033	.1033
.9353	.1033	.1033	.1033	.1033
.9349	.1033	.1033	.1033	.1033
.9345	.1033	.1033	.1033	.1033
.9341	.1033	.1033	.1033	.1033
.9337	.1033	.1033	.1033	.1033
.9333	.1033	.1033	.1033	.1033
.9329	.1033	.1033	.1033	.1033
.9325	.1033	.1033	.1033	.1033
.9321	.1033	.1033	.1033	.1033
.9317	.1033	.1033	.1033	.1033
.9313	.1033	.1033	.1033	.1033
.9309	.1033	.1033	.1033	.1033
.9305	.1033	.1033	.1033	.1033
.9301	.1033	.1033	.1033	.1033
.9297	.1033	.1033	.1033	.1033
.9293	.1033	.1033	.1033	.1033
.9289	.1033	.1033	.1033	.1033
.9285	.1033	.1033	.1033	.1033
.9281	.1033	.1033	.1033	.1033
.9277	.1033	.1033	.1033	.1033
.9273	.1033	.1033	.1033	.1033
.9269	.1033	.1033	.1033	.1033
.9265	.1033	.1033	.1033	.1033
.9261	.1033	.1033		

4. Comments. The direct coupling of the transmitter and receiver produces a voltage at the receiver of constant peak amplitude, having the transmitter frequency and shifted in phase by

+90 degrees. The three-loop system response envelope is a function of the vehicle speed. The output frequency is shifted 180 degrees with respect to the input current frequency.

#### REFERENCE

1. Zottarelli, L. J., "Buried Loops," JPL Interoffice Memo addressed to G. R. Hansen, 1974.

**END**